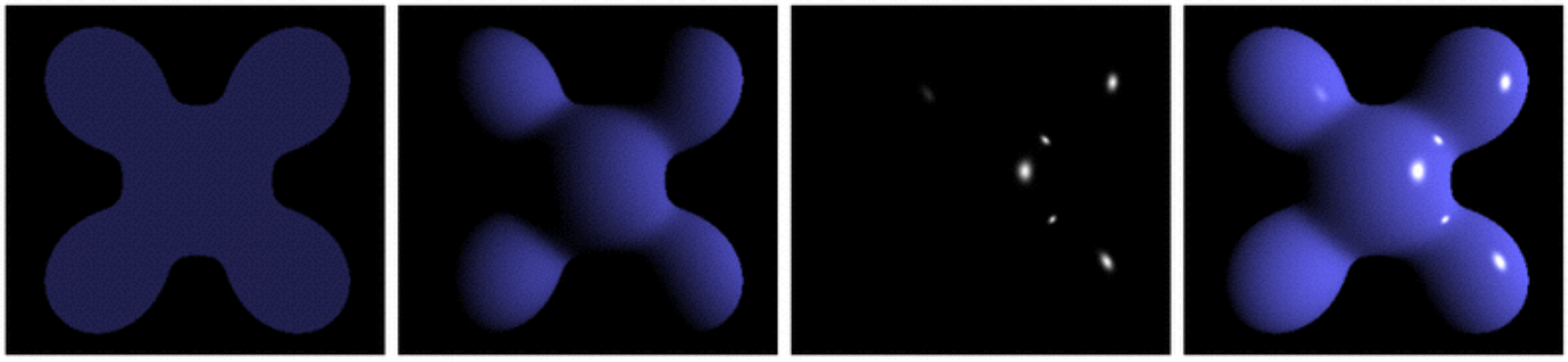
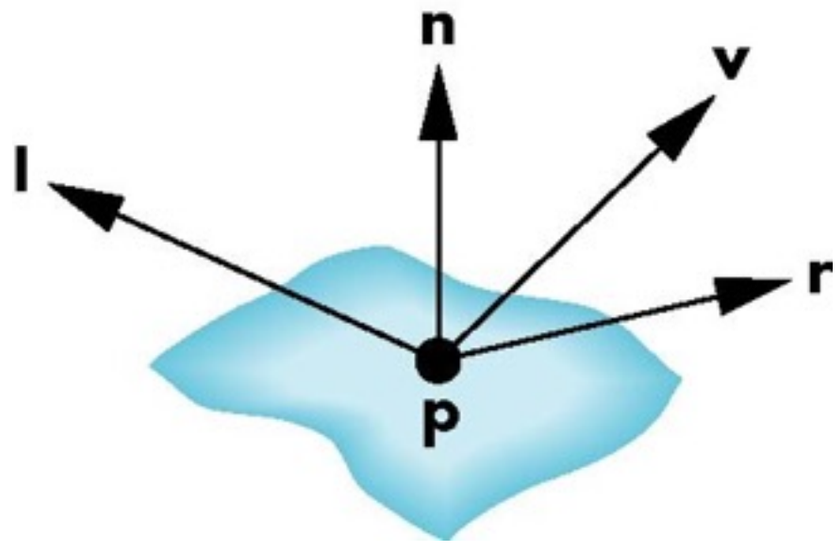
Shading Polygonal Geometry

Phong Reflection Model



Ambient + Diffuse + Specular = Phong Reflection

[Brad Smith, Wikimedia Commons]



$$I = I_a + I_d + I_s$$

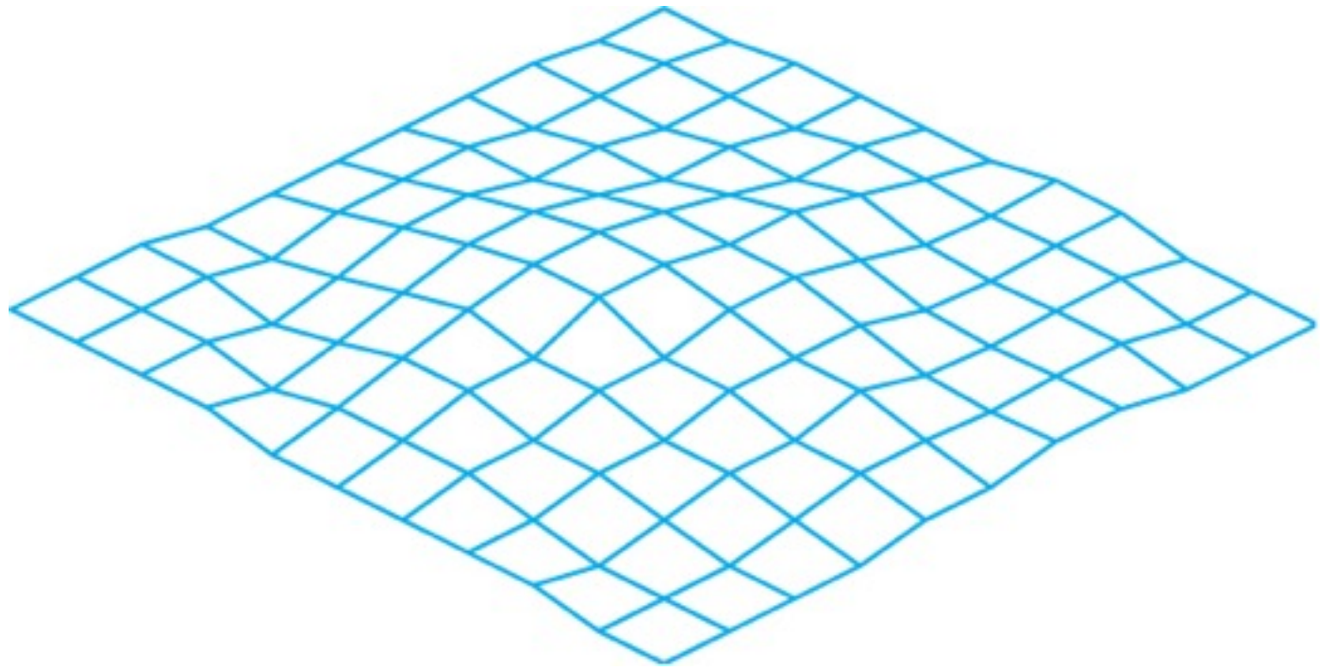
$$= R_a L_a + R_d L_d \max(0, \mathbf{l} \cdot \mathbf{n}) + R_s L_s \max(0, \mathbf{v} \cdot \mathbf{r})^{\alpha}$$

Ambient Diffuse Specular

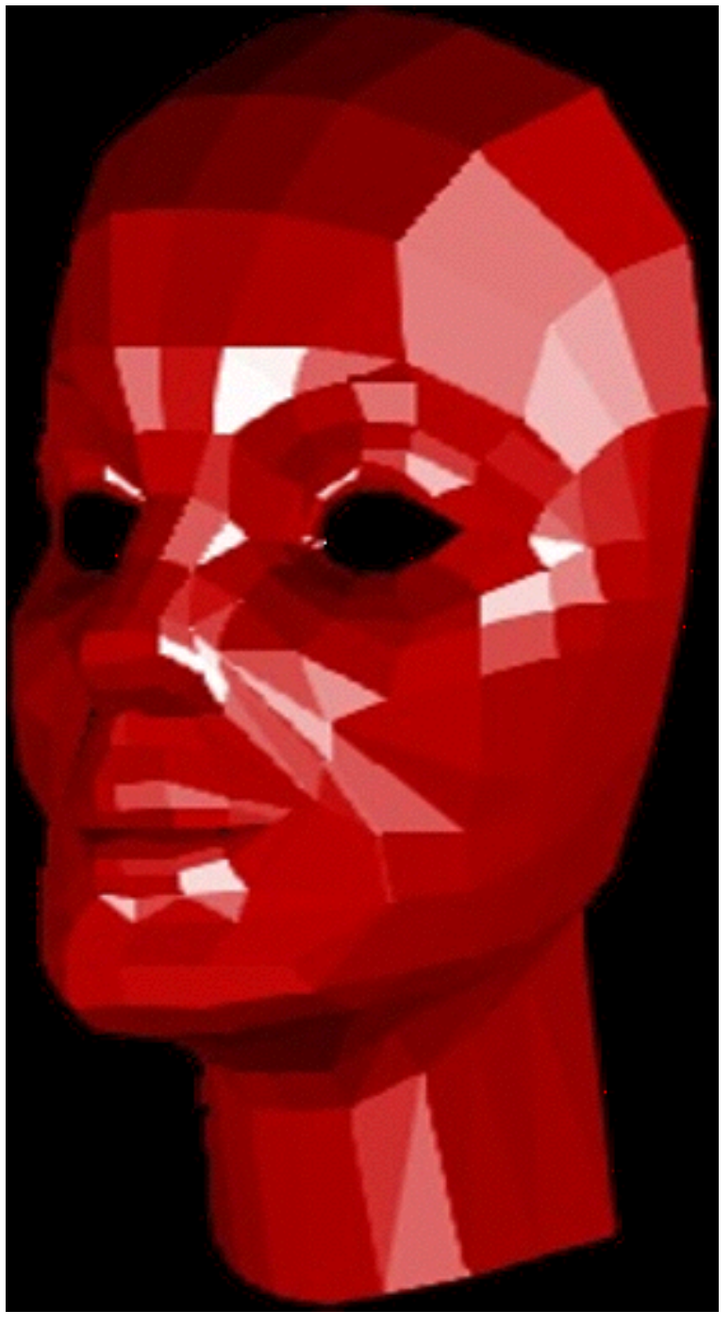
Smooth surfaces are often approximated by polygons

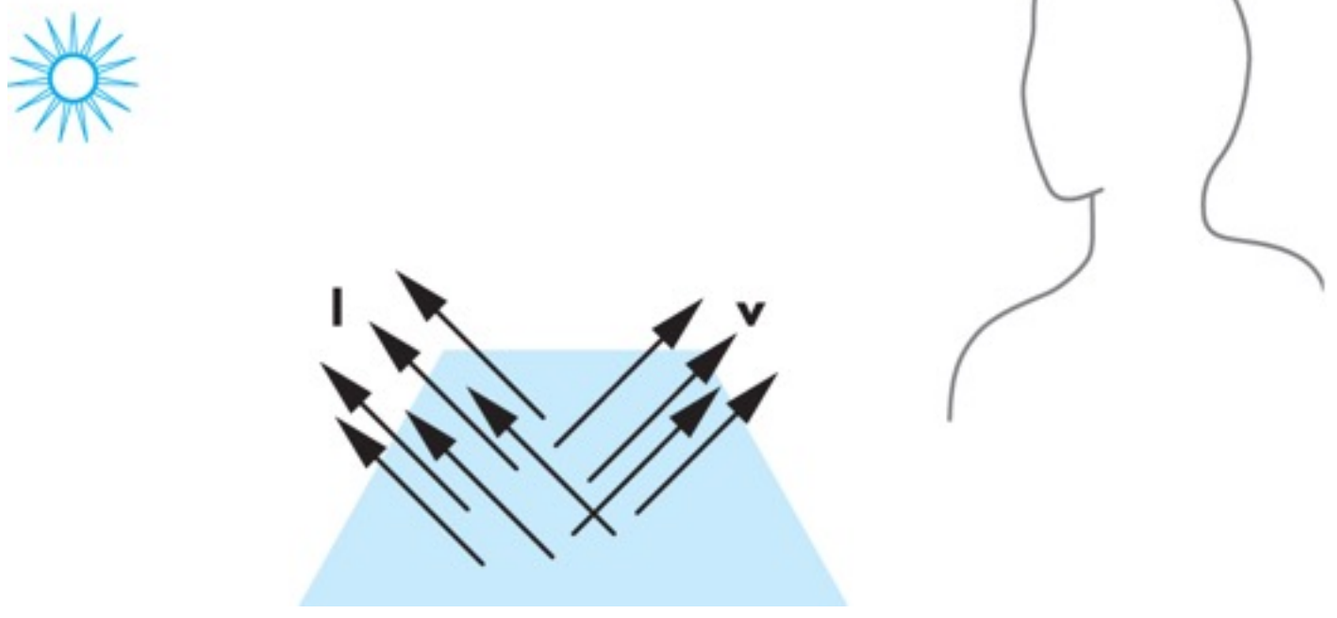
Shading approaches:

1. Flat
2. Smooth (Gouraud)
3. Phong



Flat Shading

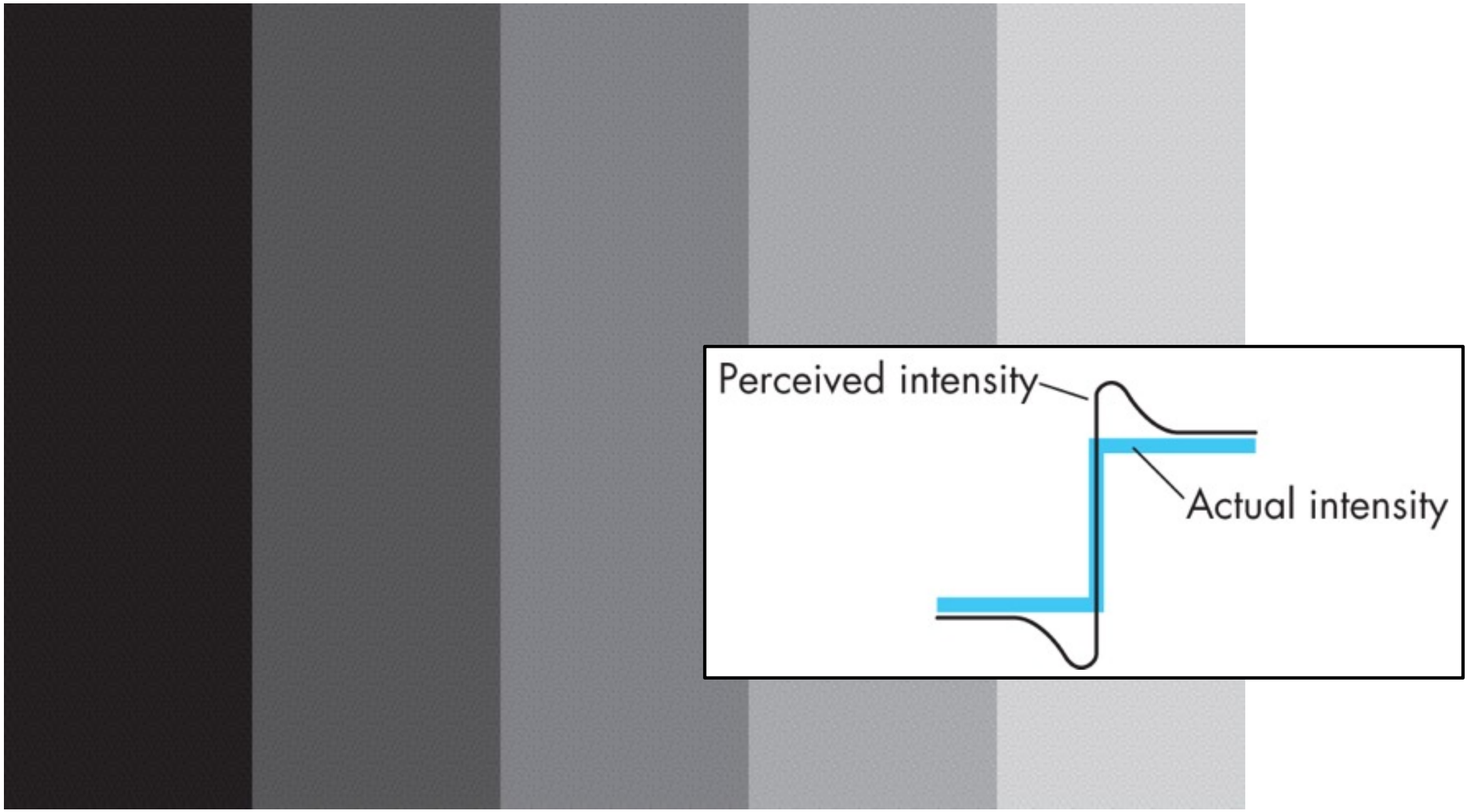




do the shading calculation once per **polygon**

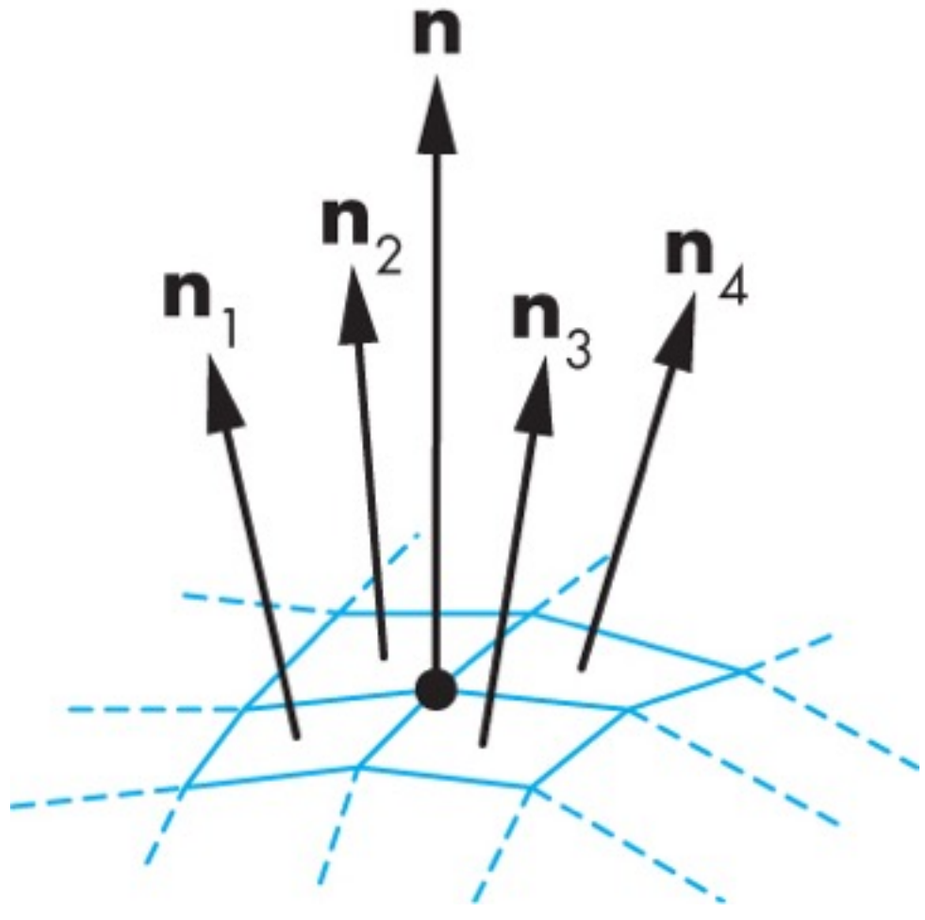
valid for light at ∞
and viewer at ∞
and faceted surfaces

Mach Band Effect



Smooth Shading

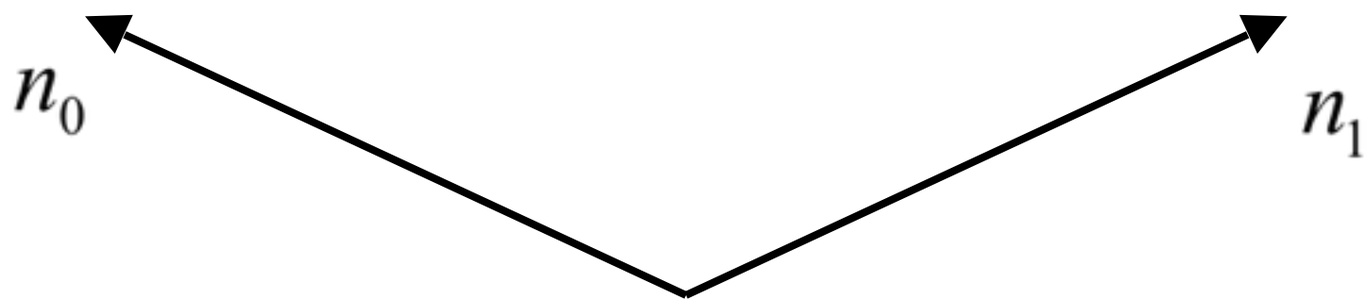
$$\mathbf{n} = \frac{\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4}{||\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4||}$$



do the shading calculation once per **vertex**

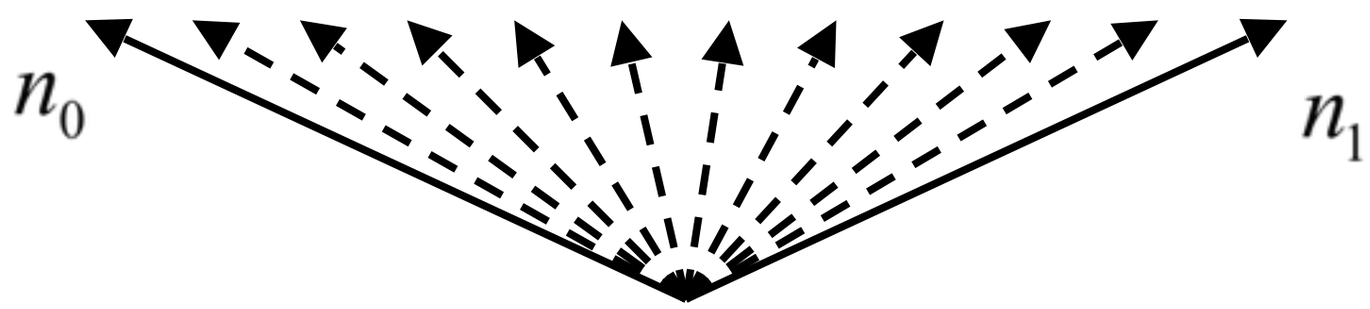
Interpolating Normals

- Must renormalize



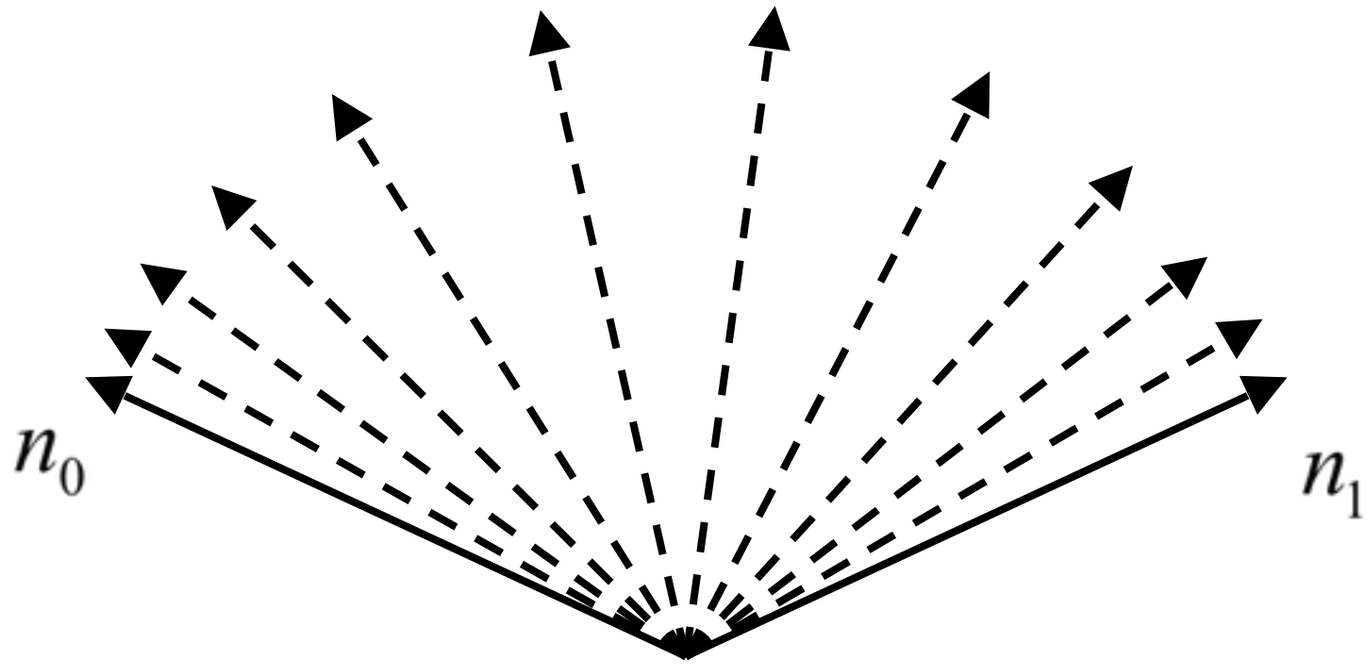
Interpolating Normals

- Must renormalize



Interpolating Normals

- Must renormalize

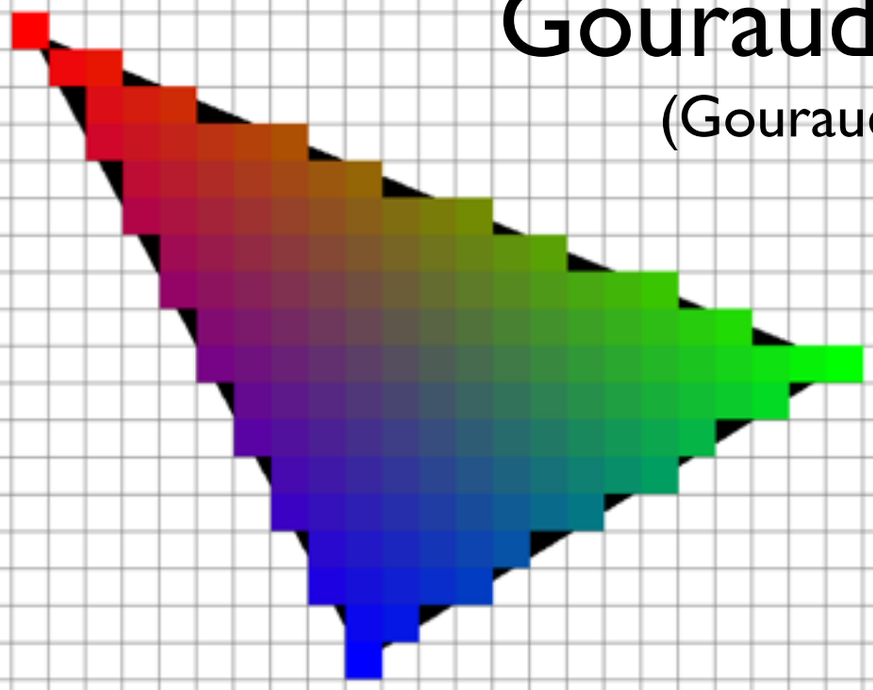


We can interpolate attributes using barycentric coordinates

$$\mathbf{c} = \alpha\mathbf{c}_0 + \beta\mathbf{c}_1 + \gamma\mathbf{c}_2$$

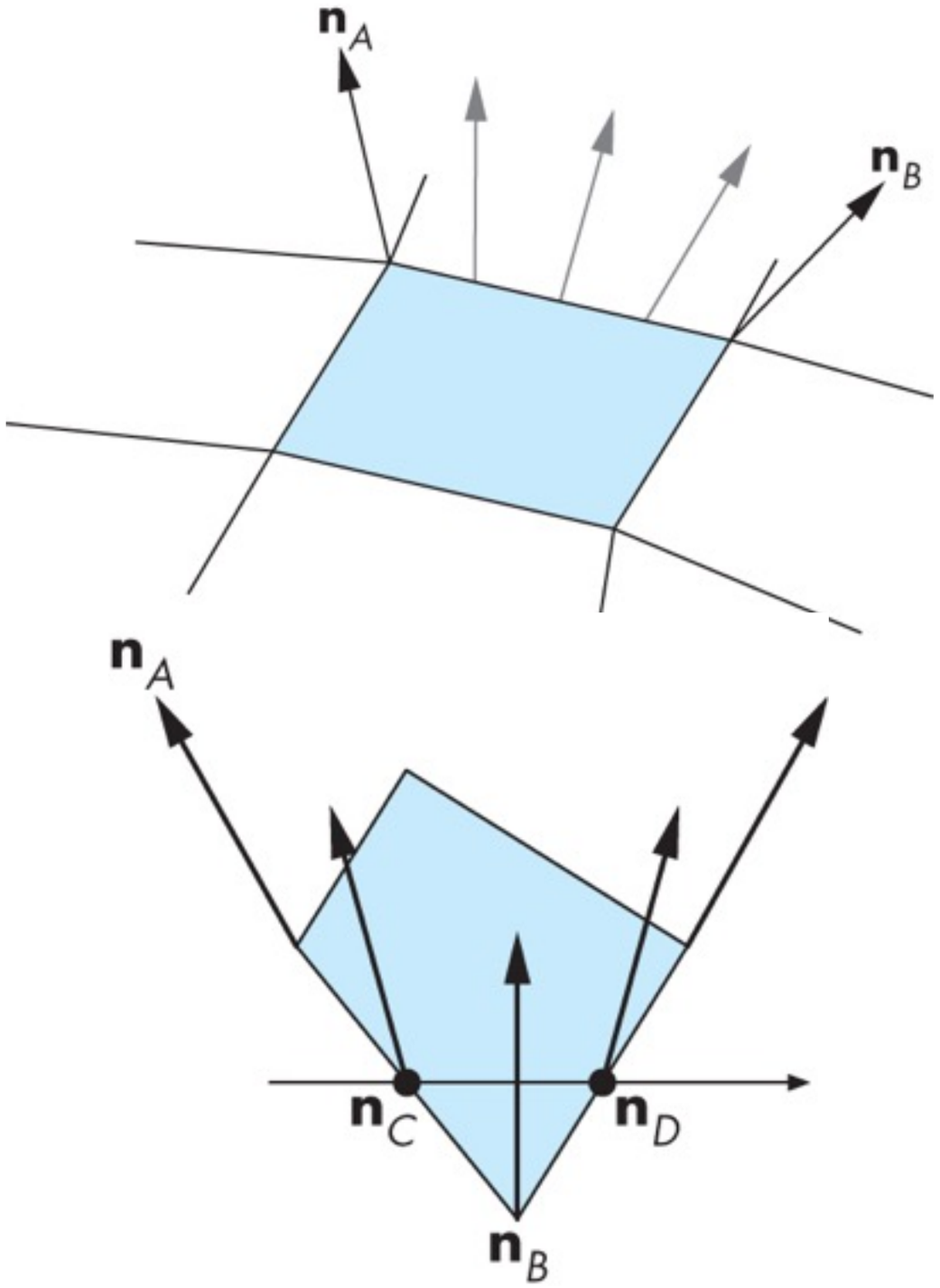
Gouraud shading

(Gouraud, 1971)



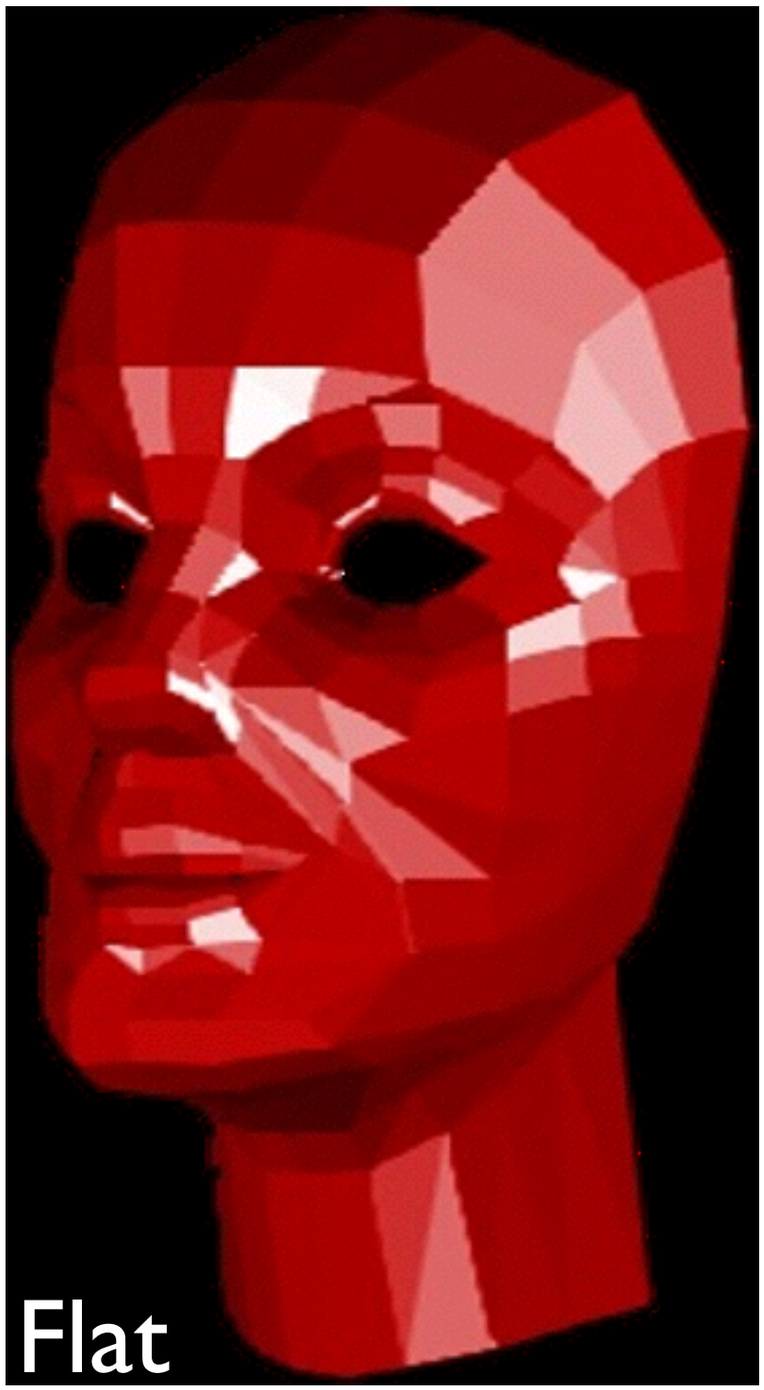
http://jtibble.dyndns.org/graphics/eecs487/eecs487.html

Phong Shading



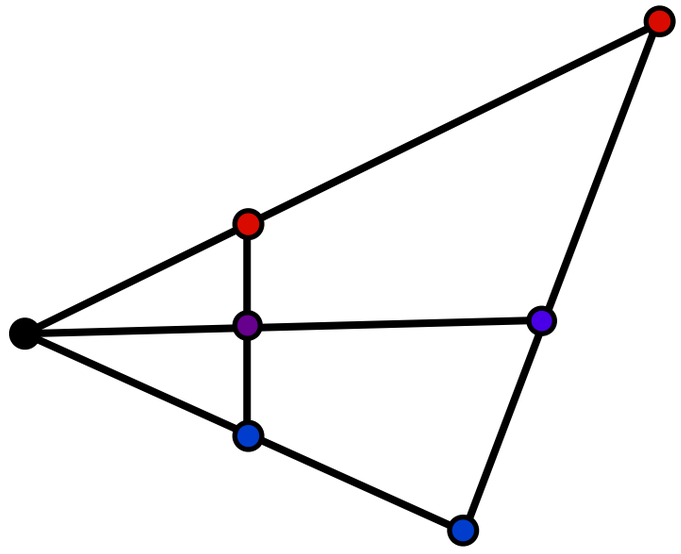
do the shading calculation once per **fragment**

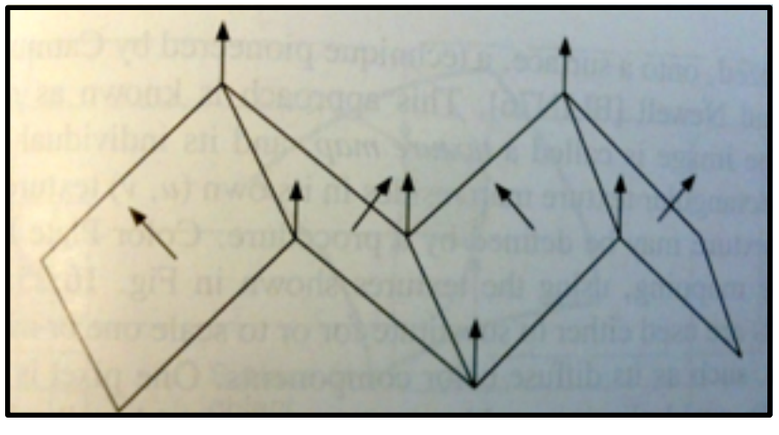
Comparison

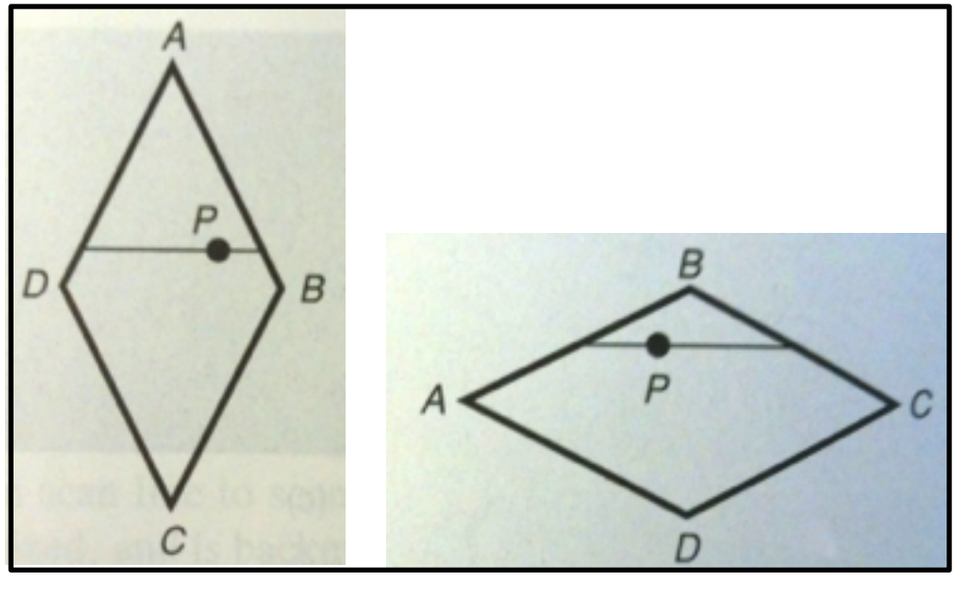


Problems with Interpolated Shading

- Polygonal silhouette
- Perspective distortion
- Orientation dependence
- Unrepresentative surface normals



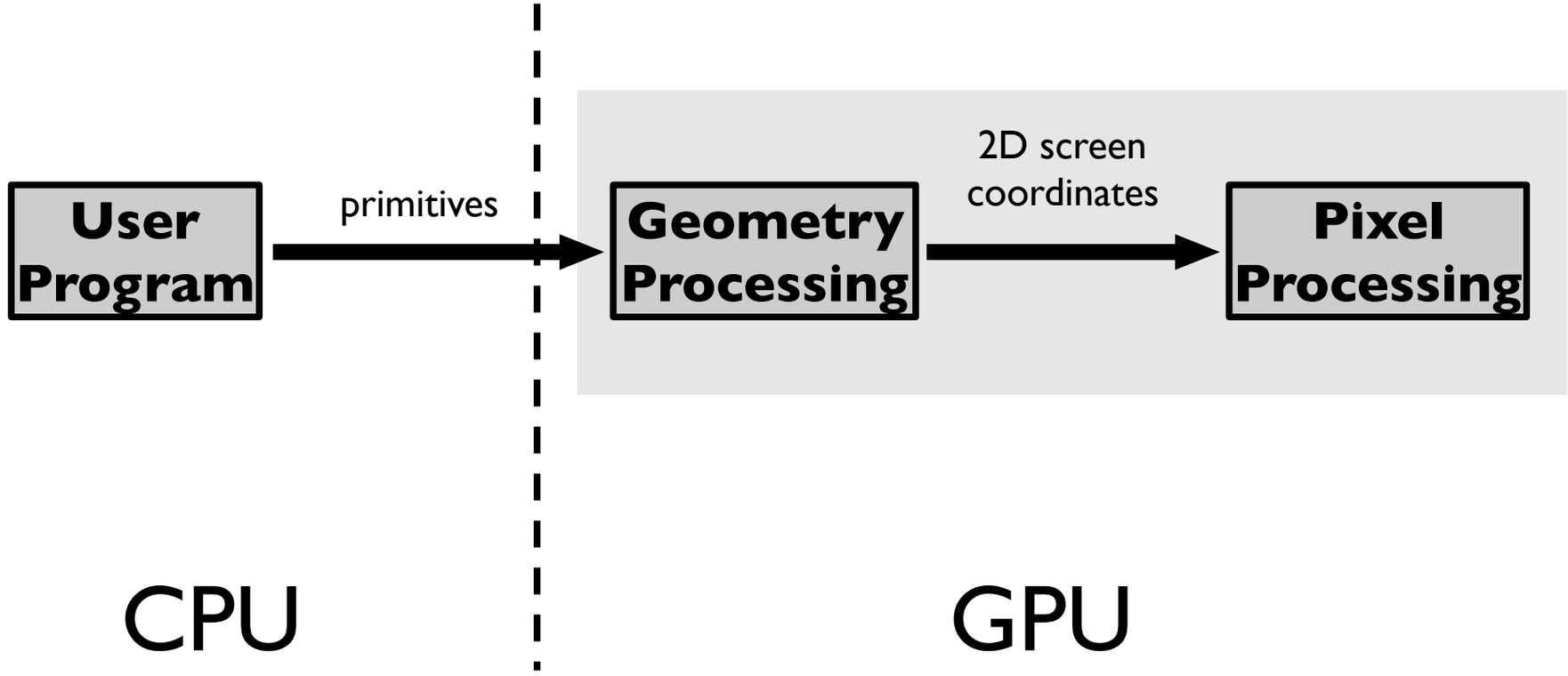




[Foley, van Dam, Feiner, Hughes]

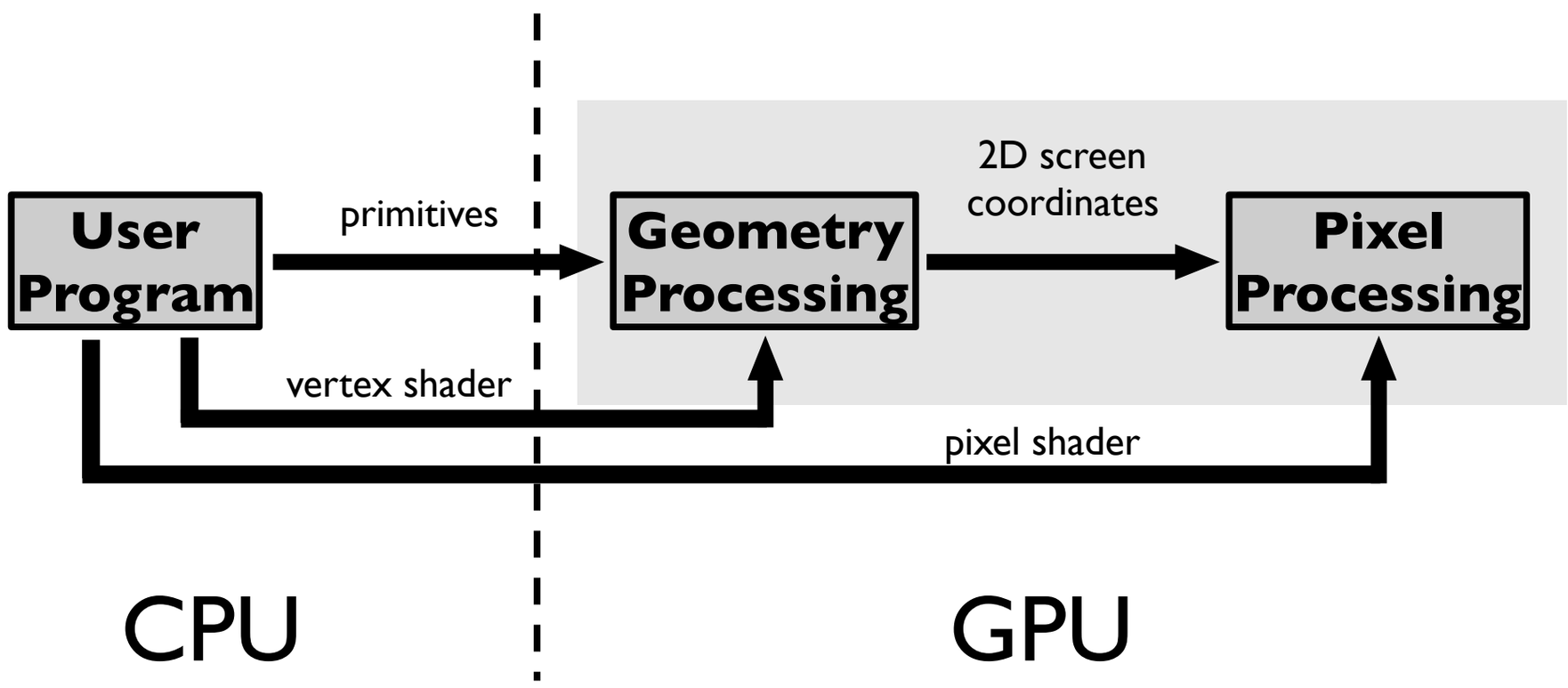
Programmable Shading

Fixed-Function Pipeline



Control pipeline through GL state variables

Programmable Pipeline



Supply shader programs to be executed on GPU as part of pipeline

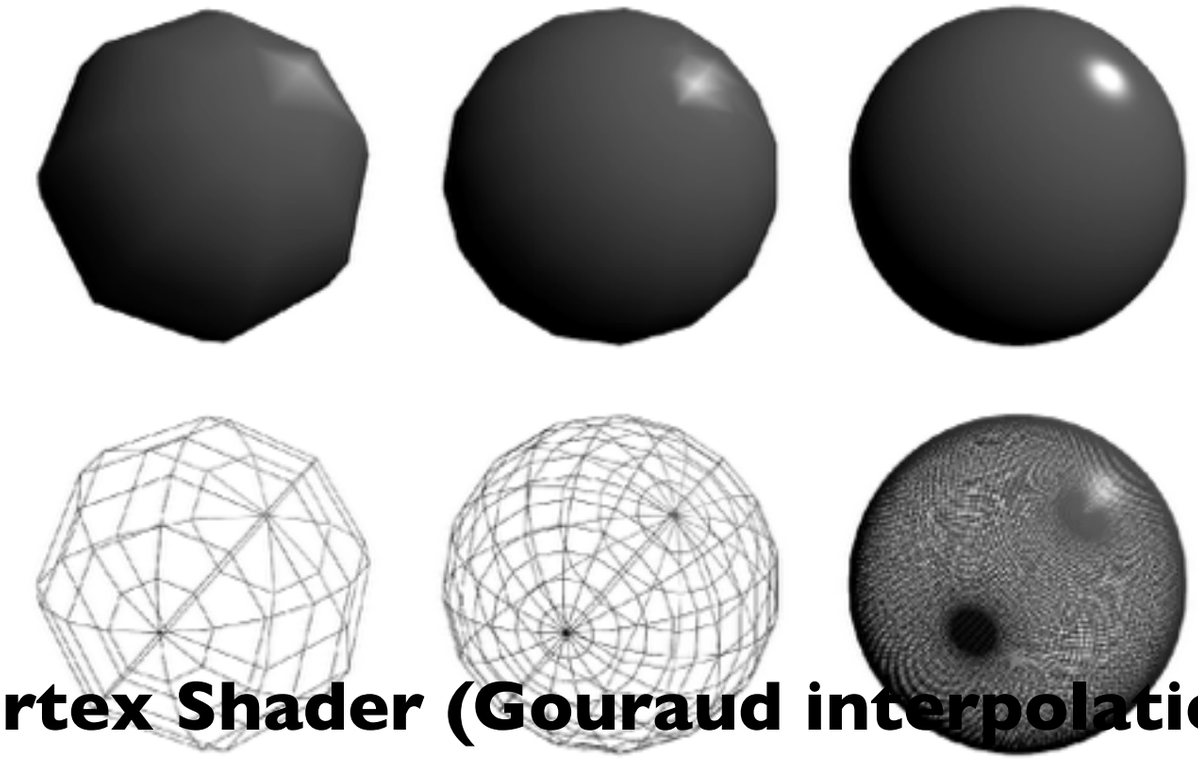
Phong reflectance in vertex and pixel shaders using GLSL

```
void main(void)
{
    vec4 v = gl_modelView_Matrix * gl_Vertex;
    vec3 n = normalize(gl_NormalMatrix * gl_Normal);
    vec3 l = normalize(gl_lightSource[0].position - v);
    vec3 h = normalize(l - normalize(v));

    float p = 16;
    vec4 cr = gl_FrontMaterial.diffuse;
    vec4 cl = fl_LightSource[0].diffuse;
    vec4 ca - vec4(0.2, 0.2, 0.2, 1.0);

    vec4 color;
    if (dot(h,n) > 0)
        color = cr * (ca + cl * max(0,dot(,n,l)))
            + cl* pow(dot(h,n), p);
    else
        color = cr * (ca + cl * max(0,dot(,n,l)));

    gl_FrontColor = color;
    gl_Position = ftransform();
}
```



Vertex Shader (Gouraud interpolation)

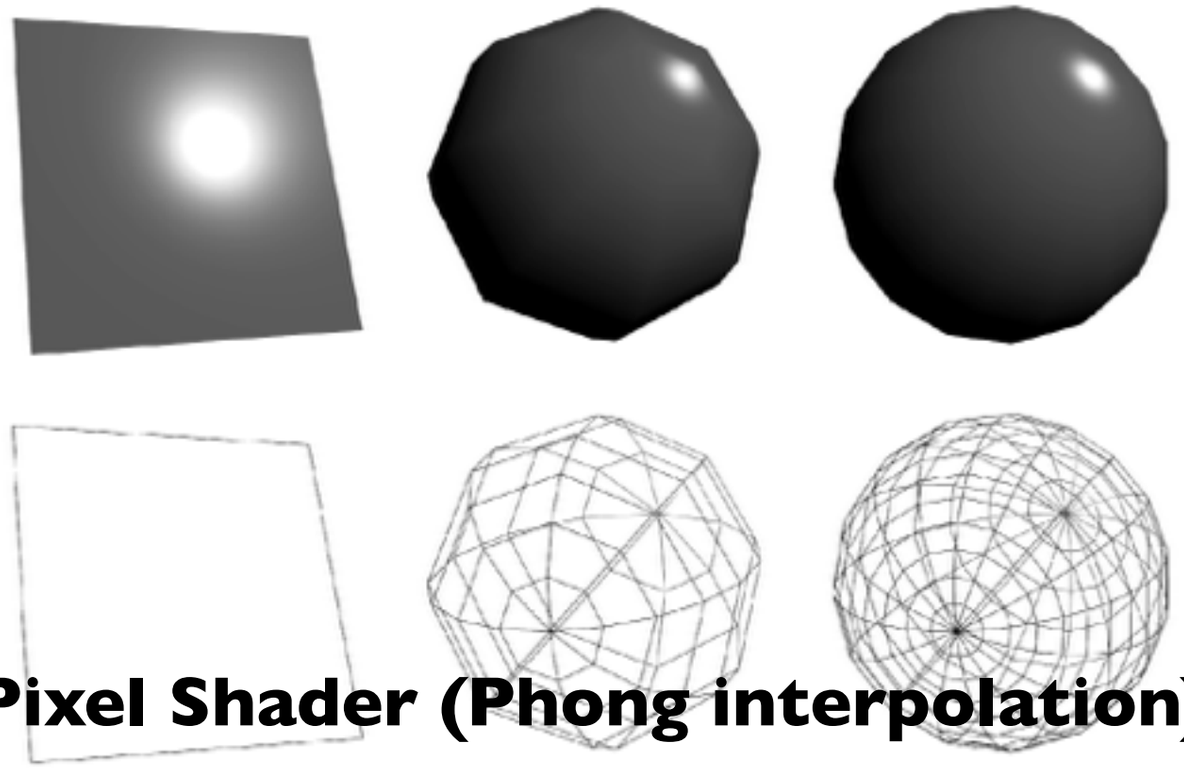
```
varying vec4 v;
varying vec3 n;

void main(void)
{
    vec3 l = normalize(gl_lightSource[0].position - v);
    vec3 h = normalize(l - normalize(v));

    float p = 16;
    vec4 cr = gl_FrontMaterial.diffuse;
    vec4 cl = fl_LightSource[0].diffuse;
    vec4 ca - vec4(0.2, 0.2, 0.2, 1.0);

    vec4 color;
    if (dot(h,n) > 0)
        color = cr * (ca + cl * max(0,dot(,n,l)))
            + cl* pow(dot(h,n), p);
    else
        color = cr * (ca + cl * max(0,dot(,n,l)));

    gl_FragColor = color;
}
```

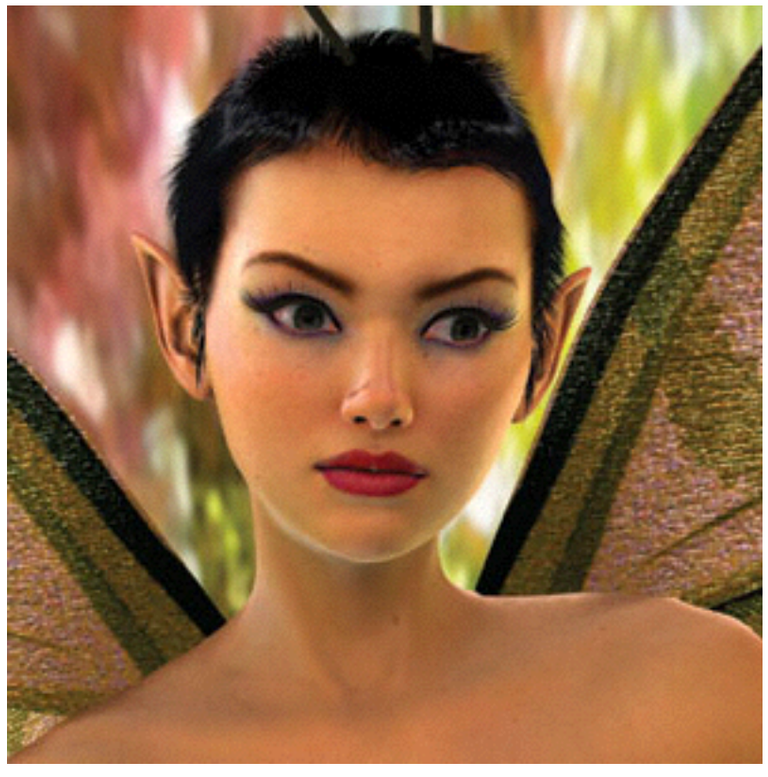


Pixel Shader (Phong interpolation)

[Shirley and Marschner]

Rusty car shader, NVIDIA

Call of Juarez DX10 Benchmark, ATI



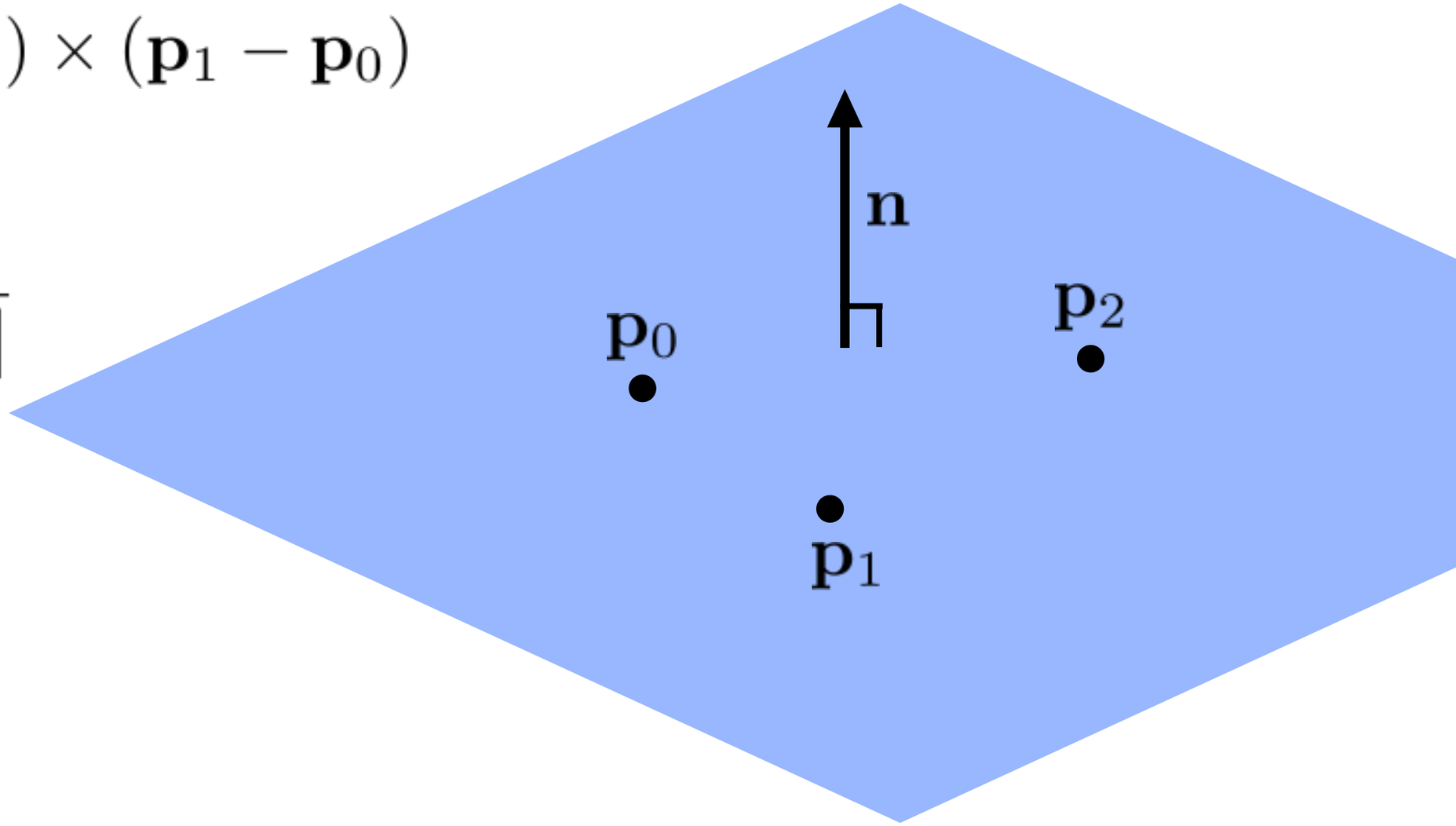
Dawn, NVIDIA

Computing Normal Vectors

Plane Normals

$$\mathbf{v} = (\mathbf{p}_2 - \mathbf{p}_0) \times (\mathbf{p}_1 - \mathbf{p}_0)$$

$$\mathbf{n} = \frac{\mathbf{v}}{||\mathbf{v}||}$$



Implicit function normals

$$f(\mathbf{p}) = 0$$

$$\nabla f(\mathbf{p})$$

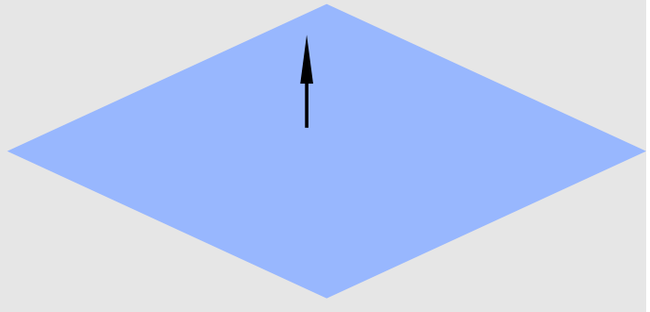
$$\nabla f = \begin{pmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \\ \frac{\partial f}{\partial z} \end{pmatrix}$$

sphere

$$\mathbf{p} \cdot \mathbf{p} - r^2 = 0$$

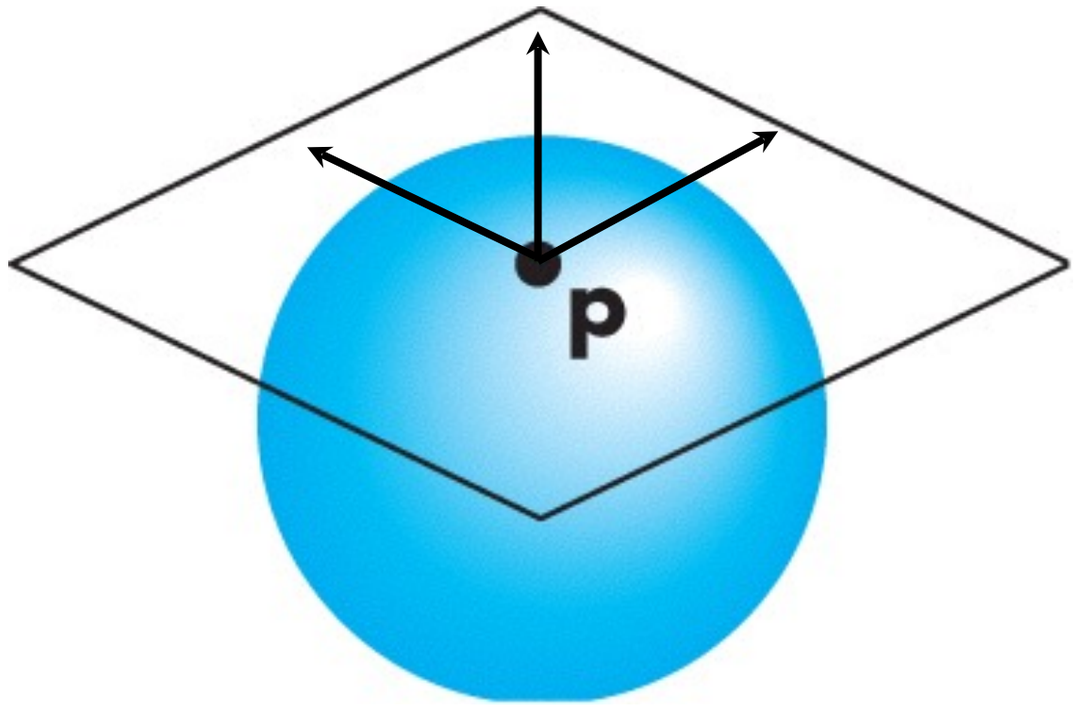
plane

$$\mathbf{n} \cdot (\mathbf{p} - \mathbf{p}_0) = 0$$



Parametric form

$$\mathbf{p}(u,v) = \begin{pmatrix} x(u,v) \\ y(u,v) \\ z(u,v) \end{pmatrix}$$



tangent vectors $\dfrac{\partial \mathbf{p}}{\partial u} \qquad \dfrac{\partial \mathbf{p}}{\partial v}$

normal $$\frac{\frac{\partial \mathbf{p}}{\partial u} \times \frac{\partial \mathbf{p}}{\partial v}}{||\frac{\partial \mathbf{p}}{\partial u} \times \frac{\partial \mathbf{p}}{\partial v}||}$$