

# CS230 : Computer Graphics

Lecture 12: Introduction to Animation

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# Types of animation

- keyframing
- rotoscoping
- stop motion
- procedural
- simulation
- motion capture

# Performance capture



Lord of the Rings, 2001



Rise of the Planet of the Apes, 2011



Avatar, 2009

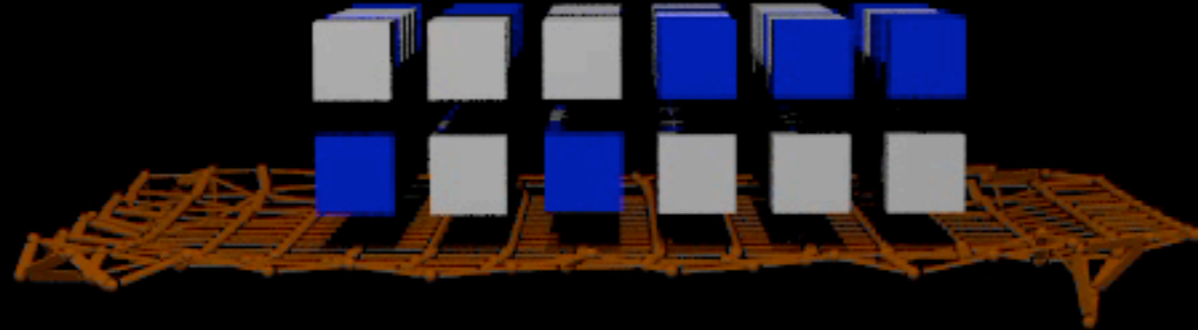
Andy Serkis – Gollum, Lord of the Rings  
challenges – resolution, occlusion,

# Rigid body simulation

Rachel Weinstein, Joey Teran and Ron Fedkiw



# Rigid body simulation



Rachel Weinstein, Joey Teran and Ron Fedkiw

# Deformable object simulation

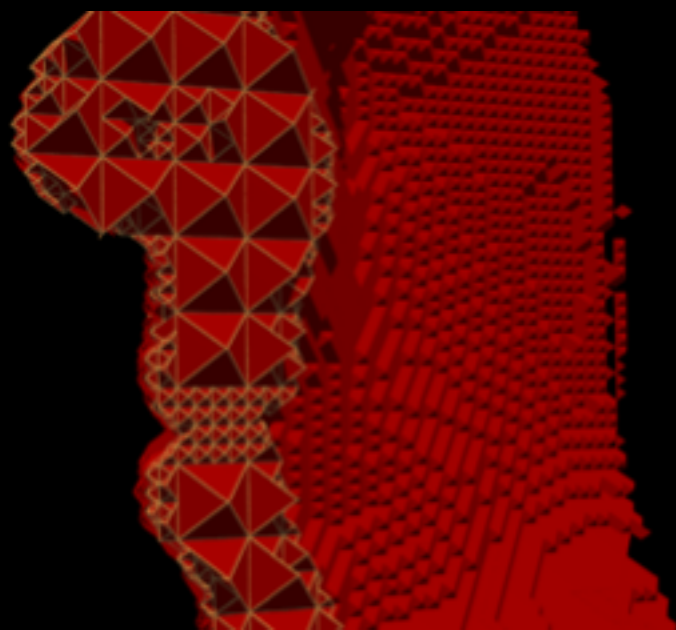


N. Molino, Z. Bao, R. Fedkiw



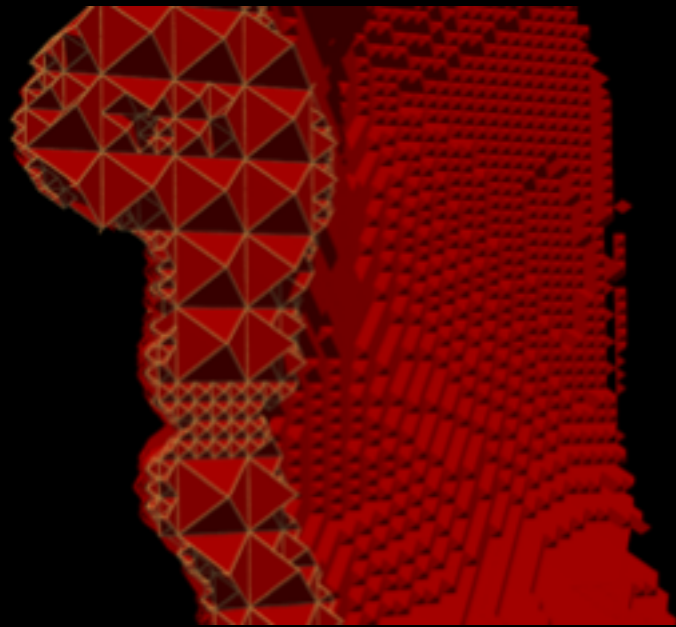
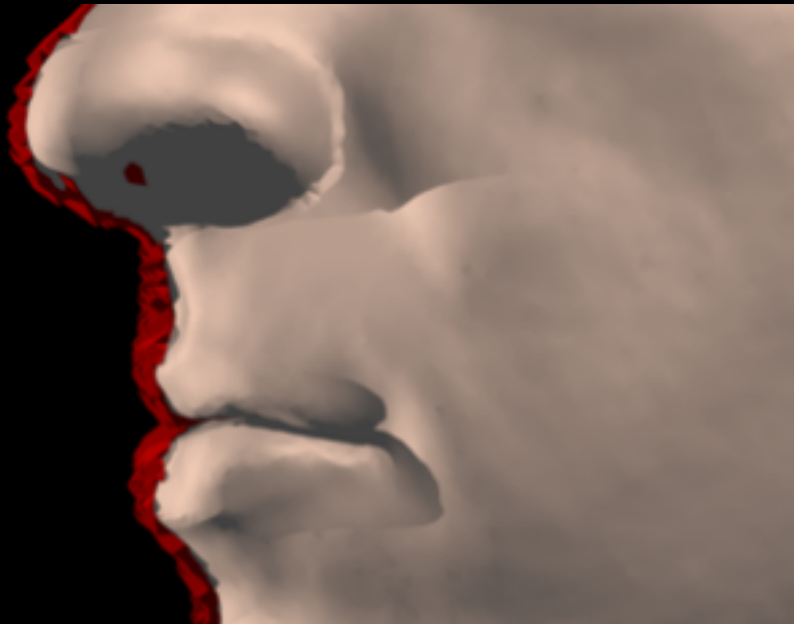
Selle et al., 2008

# Facial animation



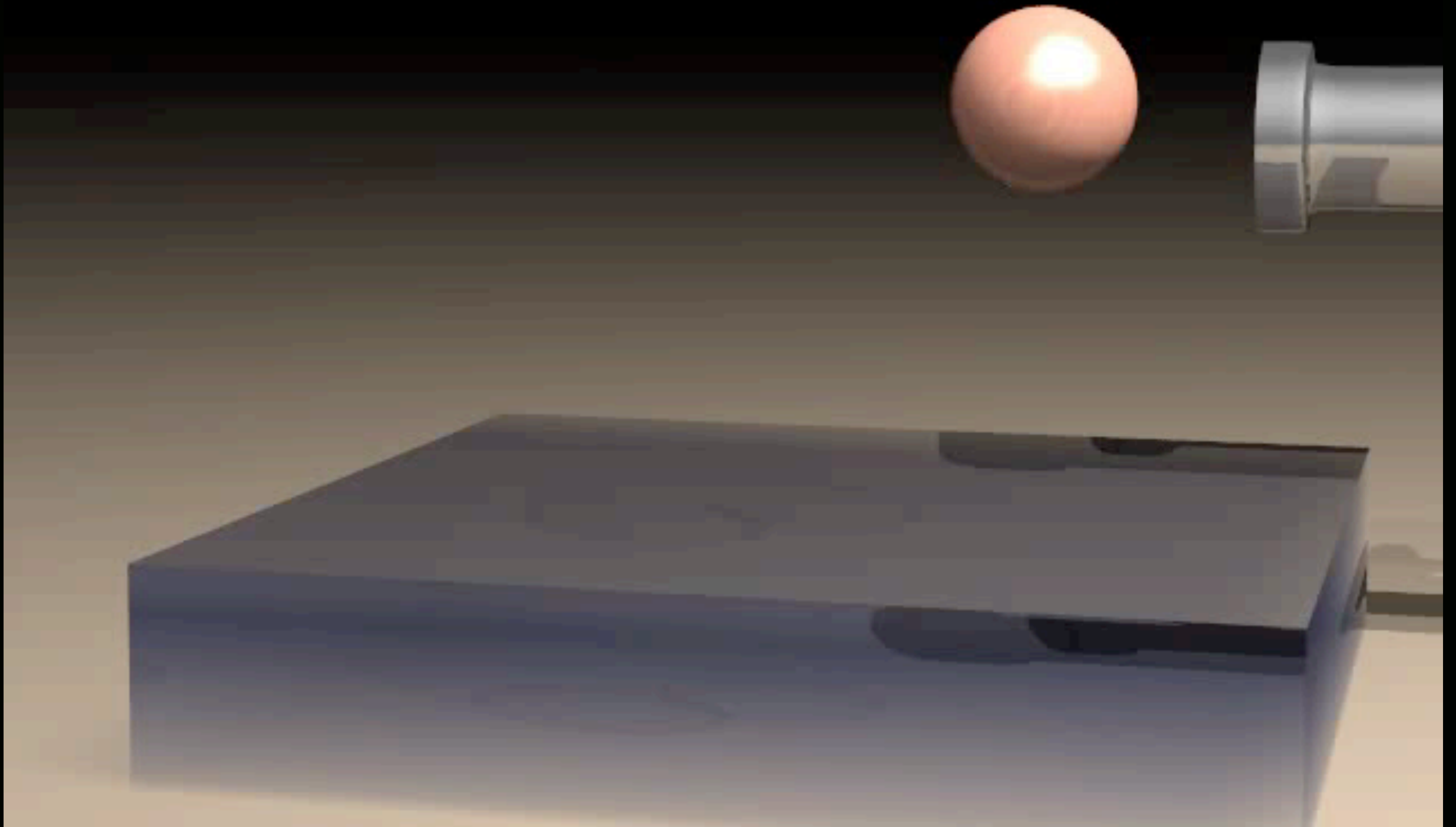


# Facial animation



# Fluid simulation

# Fluid simulation



# Control of virtual character

issues: control algorithms, interaction with environment



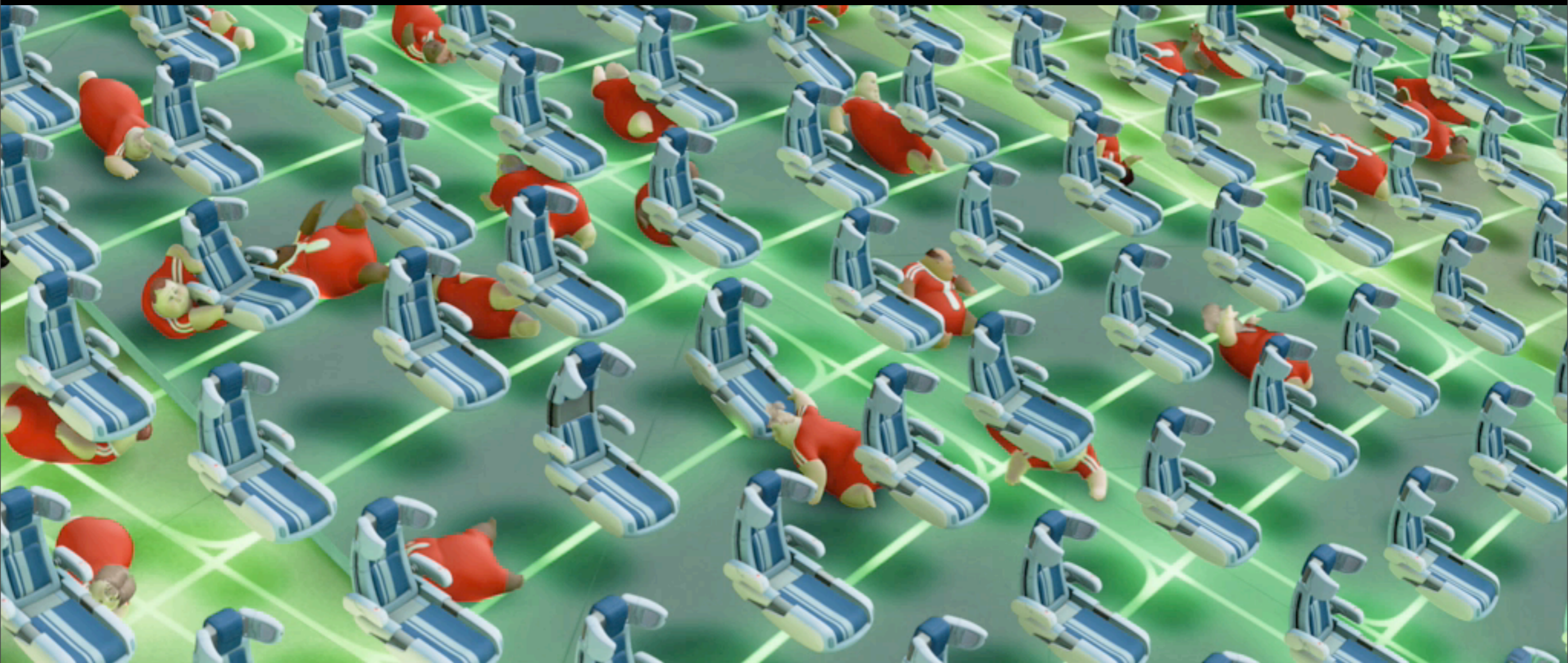
# Control of virtual character



issues: control algorithms, interaction with environment

rigid/deformable simulator in Pixar's *WALL-E*





rigid/deformable simulator in Pixar's *WALL-E*



# Crowd simulation



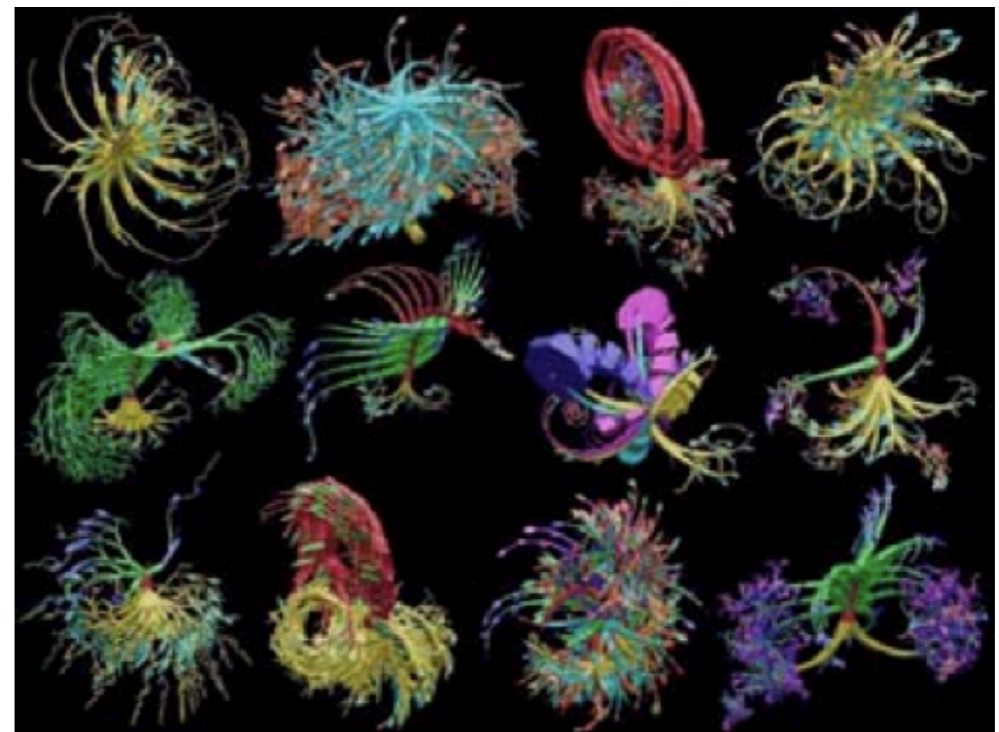
Treuille et al., 2006

- agent-based, model behavior
- also, “global effects” – e.g., incompressibility
- emergent phenomena



# Artificial life

- plants - movement and growth
- evolving artificial life



**history**

# Gertie the Dinosaur

1914

12 minutes

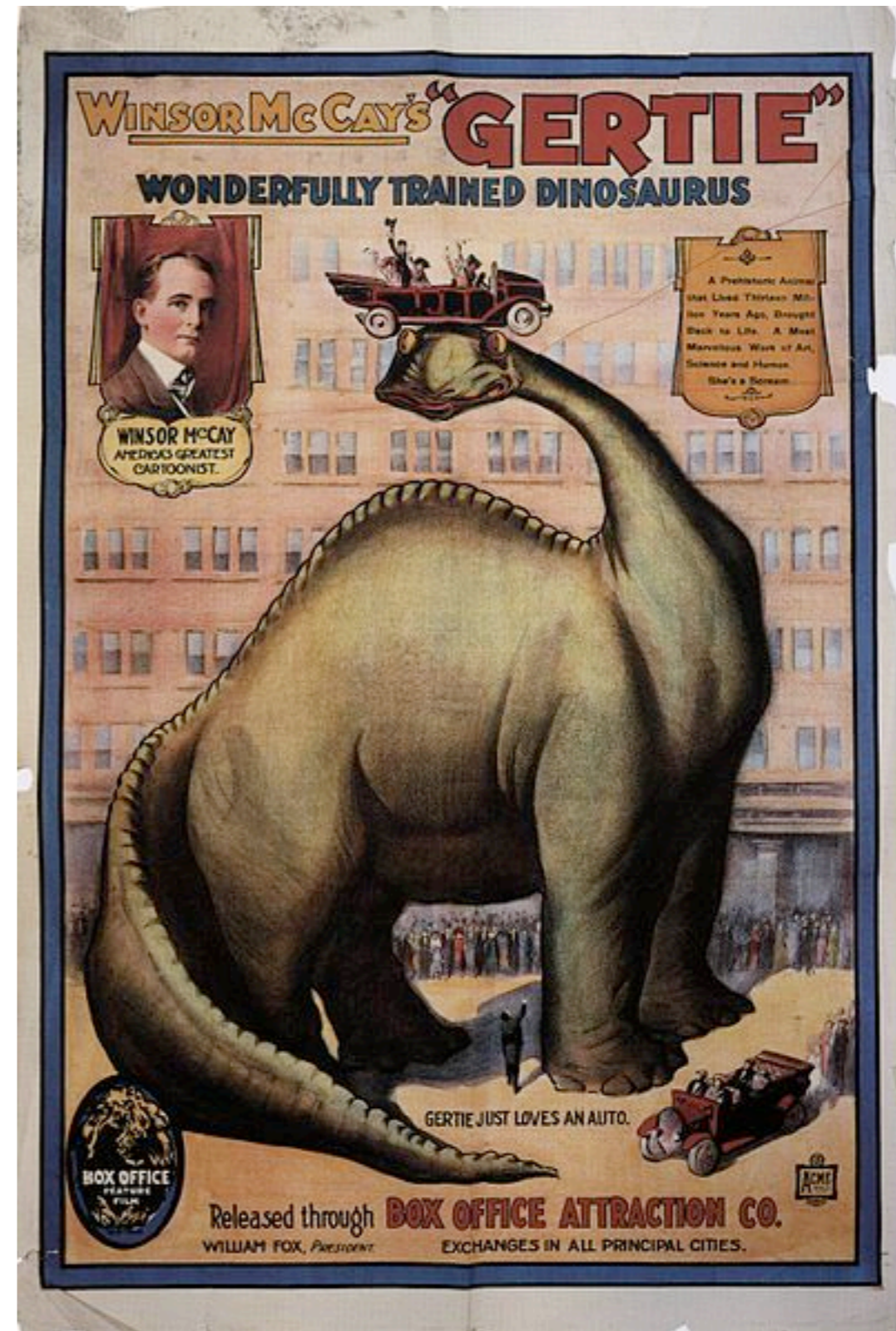
hand drawn

keyframe animation

registration

cycling

link



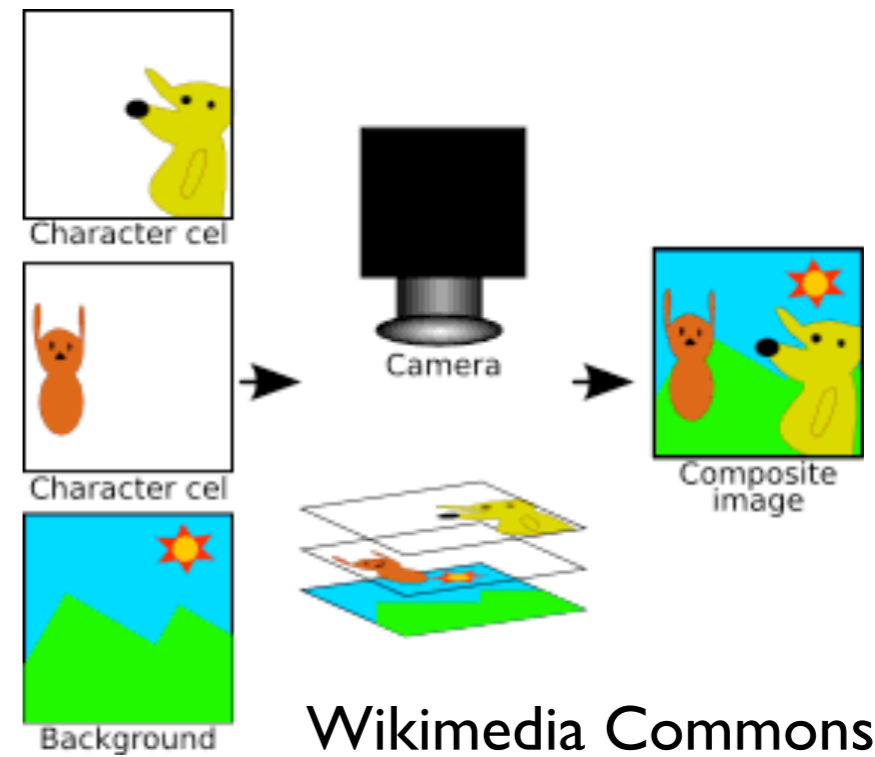


# Traditional animation

- Cels
- Multipane camera

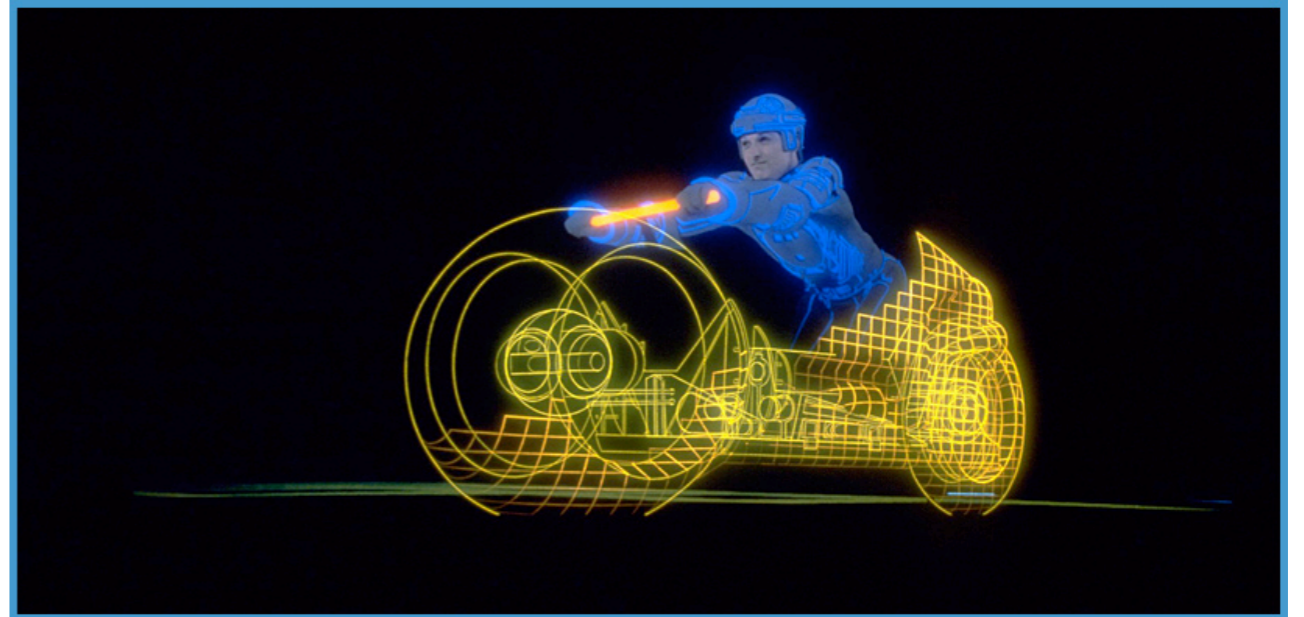


Sleeping Beauty, Disney, 1959

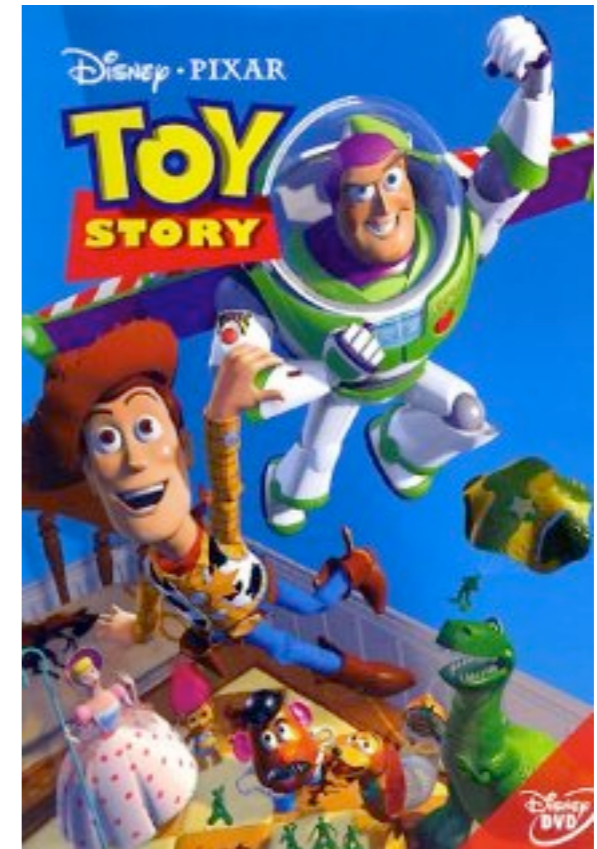




# Realistic 3D animation



- Disney's Tron, 1981
- Pixar's Toy Story, 1995, first 3D feature



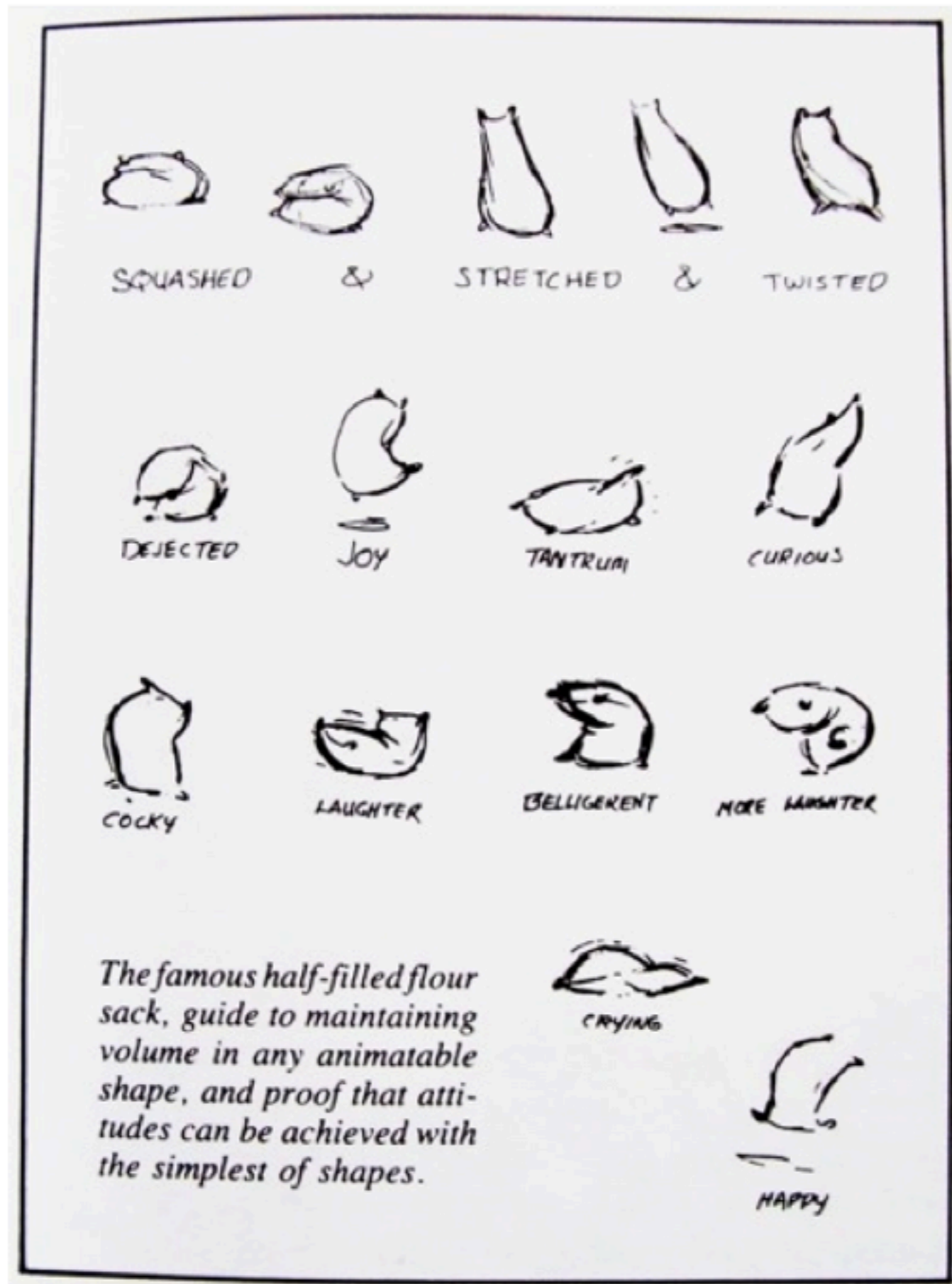
# Performance Capture

- Final Fantasy 2001
- Lord of the Rings 2001
- Beowulf 2007
- Avatar, 2009
- Adventures of Tintin, 2011



Lord of the Rings, 2001

# animation principles

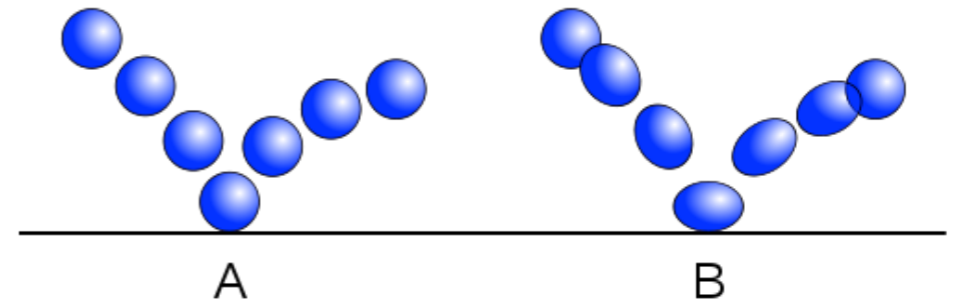


- animation can bring even a flour sack to life
- animations principles common to any type of animation



# 12 principles of animation

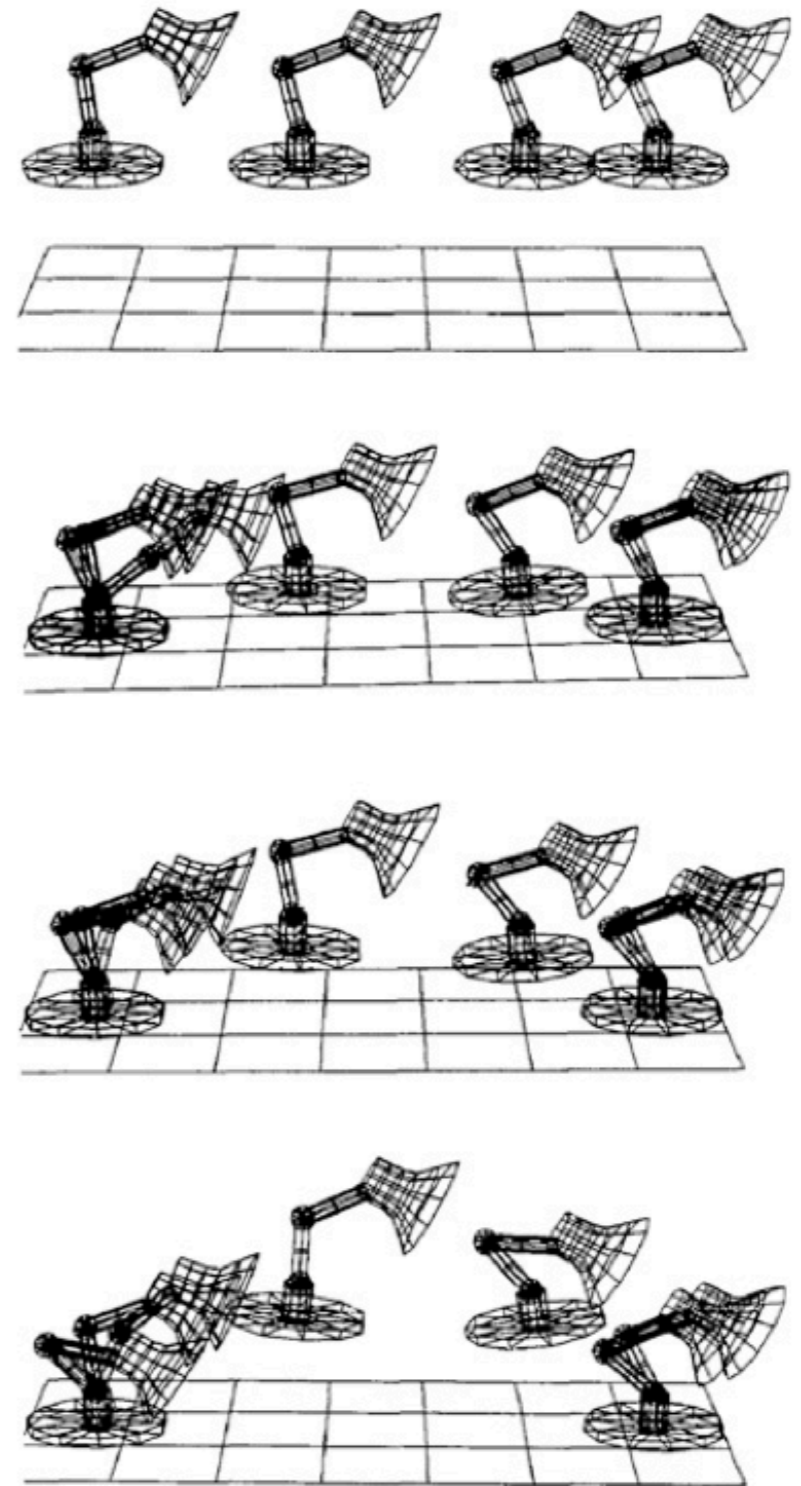
1. Squash and stretch
2. Anticipation
3. Staging
4. Straight ahead action and pose to pose
5. Follow through and overlapping action
6. Slow in and slow out
7. Arcs
8. Secondary action
9. Timing
10. Exaggeration
11. Solid drawing
12. Appeal



principles are related to the underlying physics of motion  
timing: important information. ease in/ease out

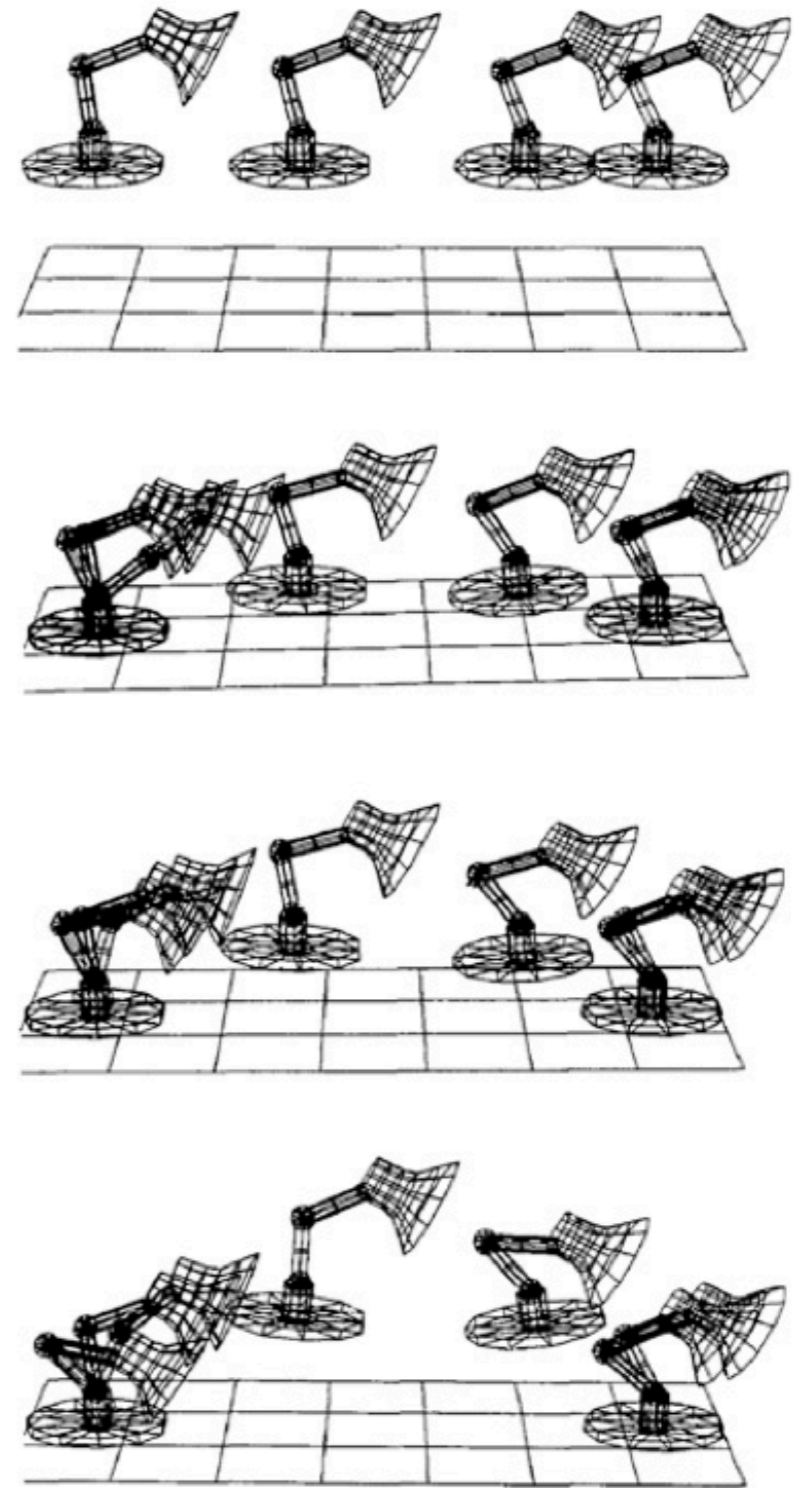
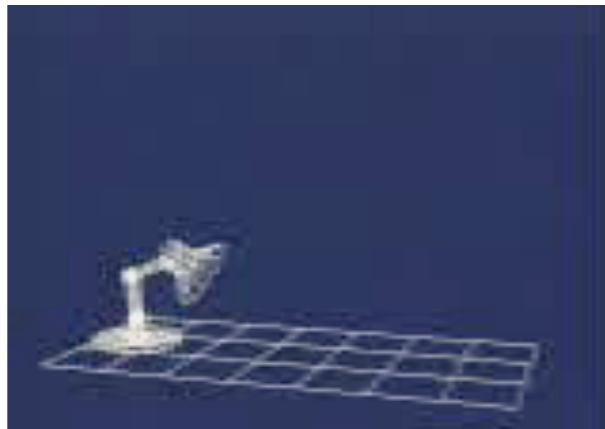
# Physics-based animation

- Many animation principles follow from underlying physics
- anticipation, follow through, secondary action, squash and stretch, ...
- *Spacetime Constraints*, Witkin and Kass 1988



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- Many animation principles follow from underlying physics
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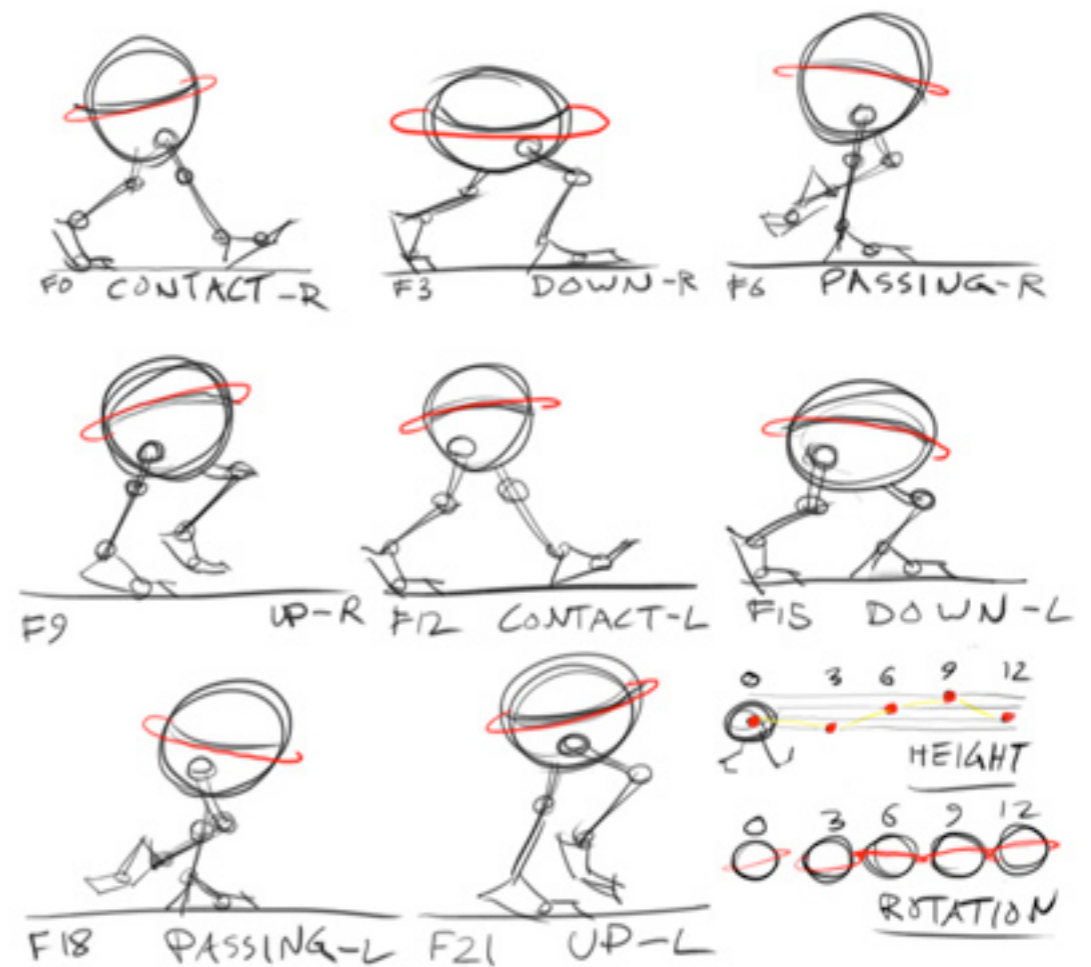


**keyframe animation**



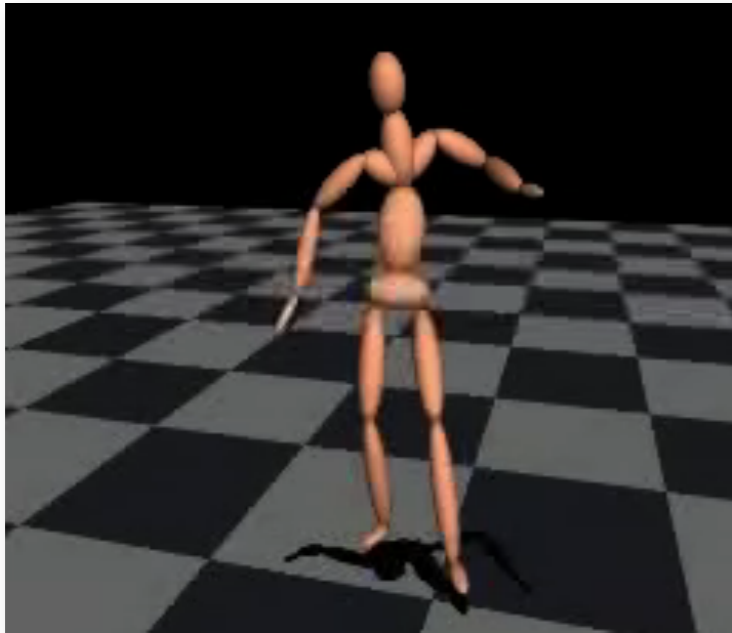
# Keyframe animation

- draw a series of poses
- fill in the frames in between (“inbetweening”)
- computer animation uses interpolation



<http://anim.tmog.net>

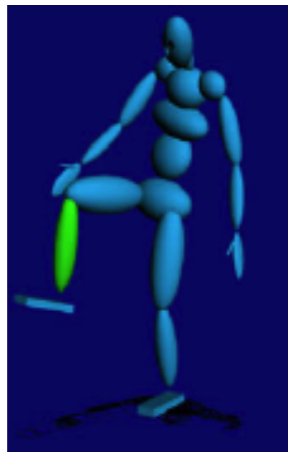
# Keyframe character DOFs



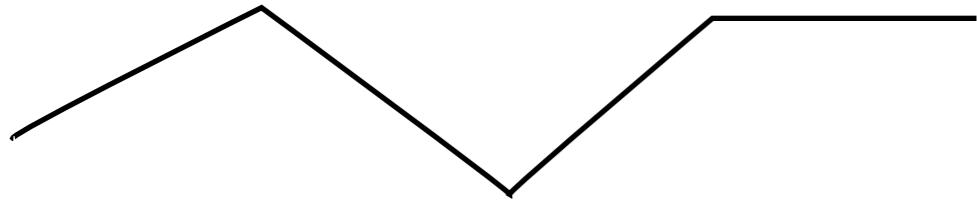
3 translational DOFs

48 rotational DOFs

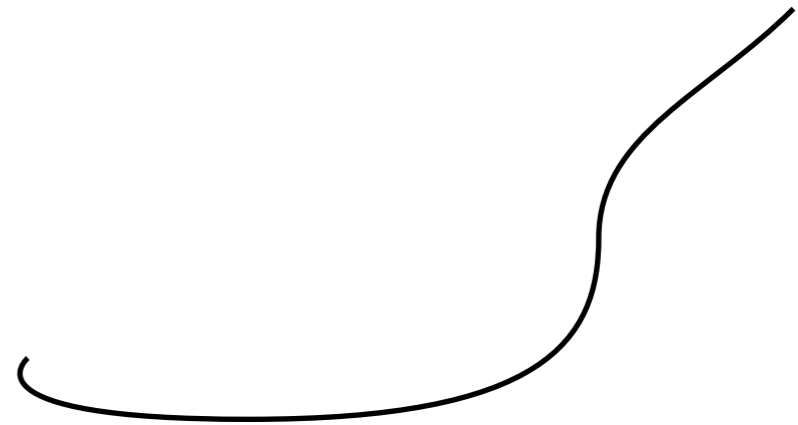
Each joint can have up to 3 DOFs



# Interpolation of keyframes



linear interpolation



spline interpolation

Straightforward to interpolate position but what about orientation?

**general rotations**



# Rotation

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$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \quad \text{X axis}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \quad \text{Y axis}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \quad \text{Z axis}$$

# Rotation about an arbitrary axis

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## Rotating about an axis by theta degrees

- Rotate about x to bring axis to xz plane
- Rotate about y to align axis with z -axis
- Rotate theta degrees about z
- Unrotate about y, unrotate about x

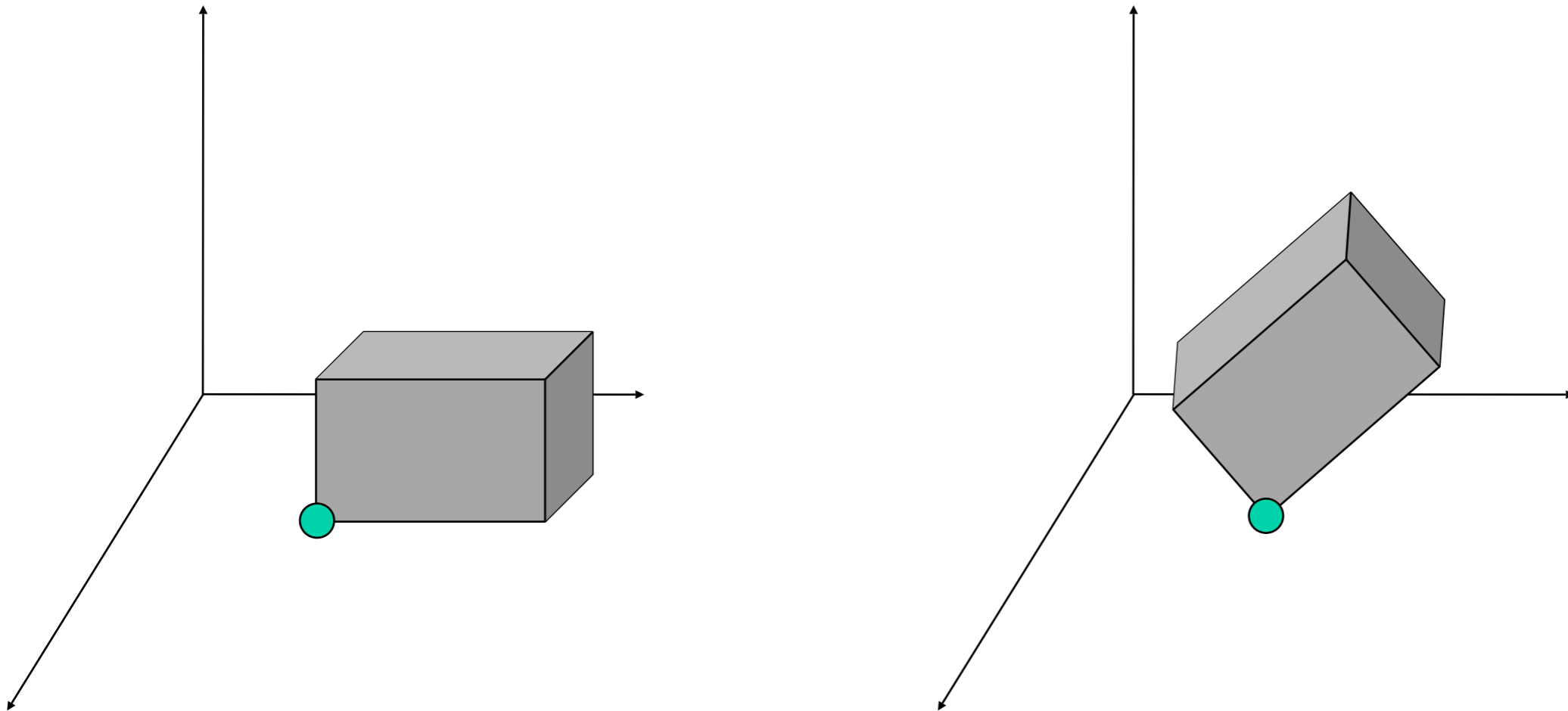
$$\mathbf{M} = \mathbf{R}_x^{-1} \mathbf{R}_y^{-1} \mathbf{R}_z(\theta) \mathbf{R}_y \mathbf{R}_x$$

- Can you determine the values of  $\mathbf{R}_x$  and  $\mathbf{R}_y$ ?

# Composite Transformations

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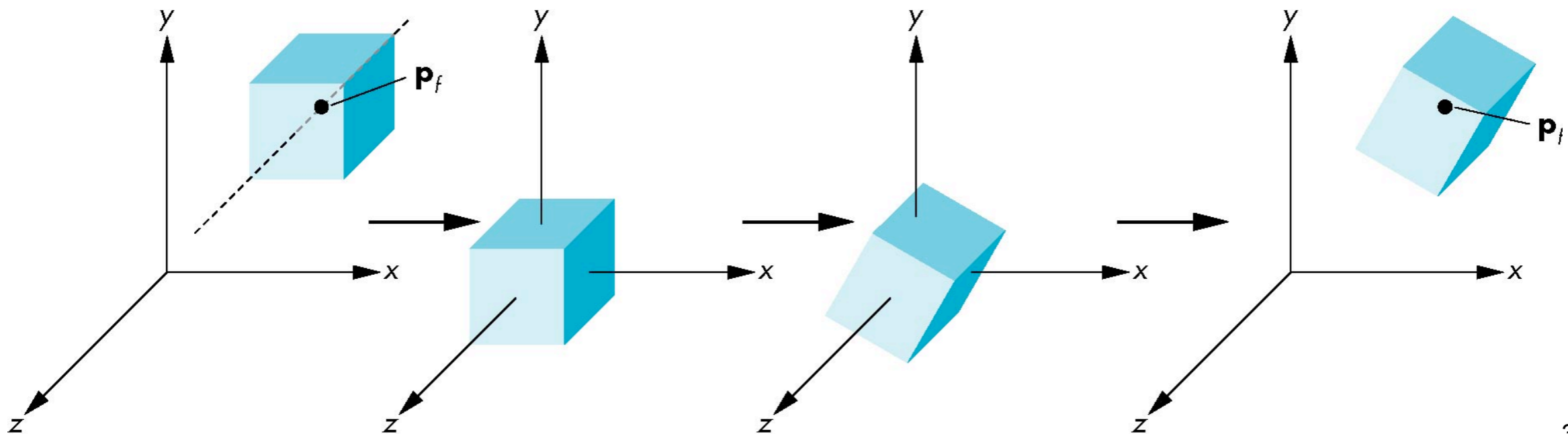
- Rotating about a fixed point
  - **basic** rotation alone will rotate about origin but we want:



# Composite Transformations

- Rotating about a fixed point
  - Move fixed point  $(p_x, p_y, p_z)$  to origin
  - Rotate by desired amount
  - Move fixed point back to original position

$$\mathbf{M} = \mathbf{T}(p_x, p_y, p_z) \mathbf{R}_z(\theta) \mathbf{T}(-p_x, -p_y, -p_z)$$





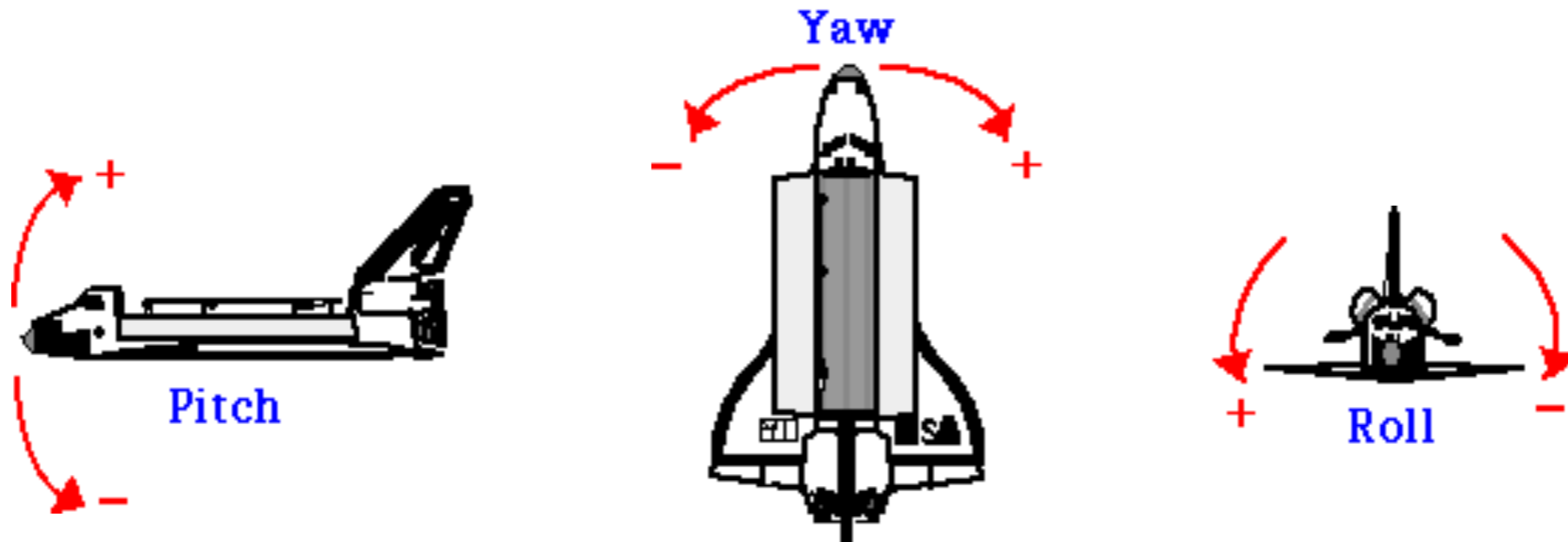
# Euler's Rotation Theorem

*Any displacement of a rigid body such that a point on the rigid body remains fixed, can be described as a rotation by some angle about some axis*

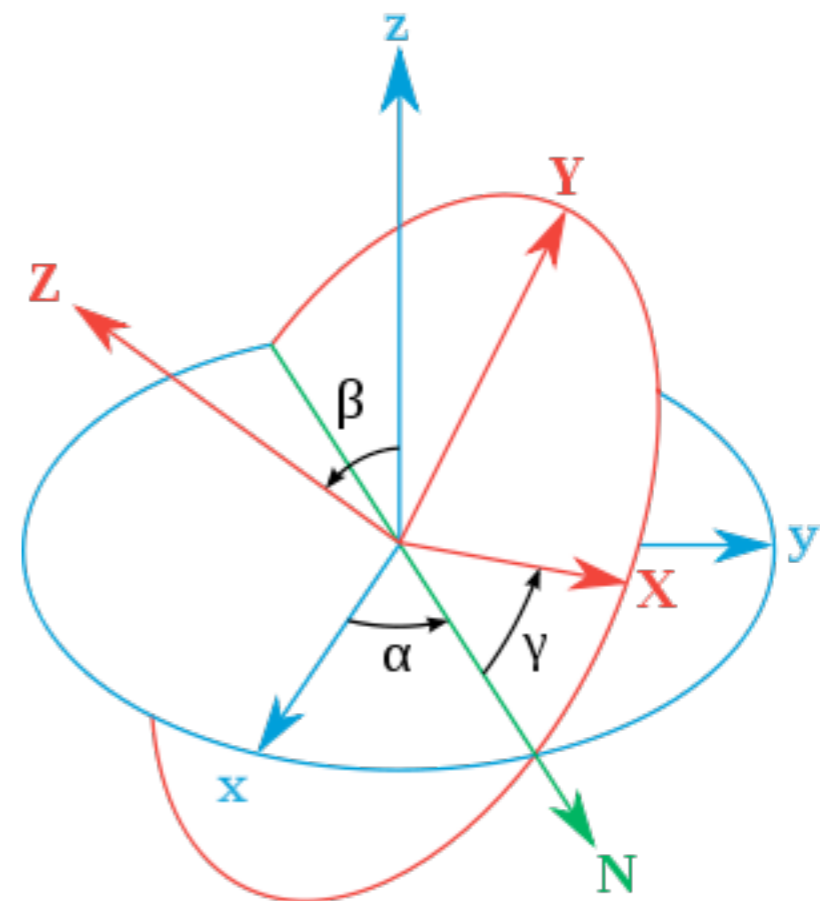
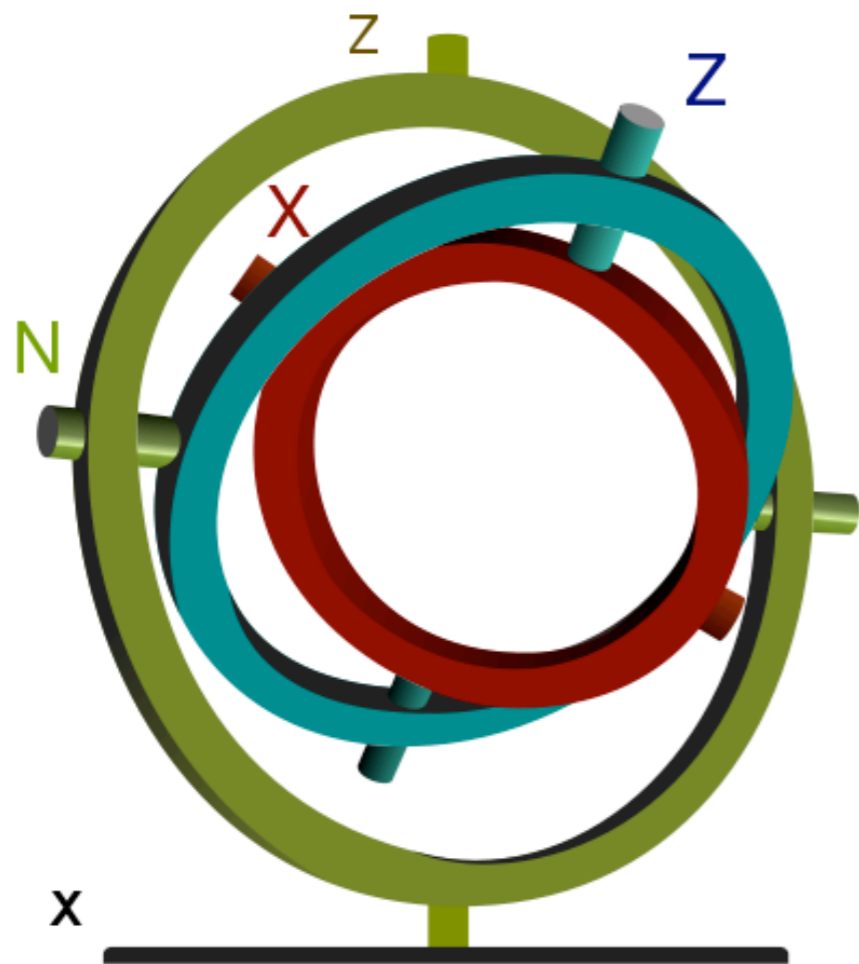
euler angles

# Euler Angles

- A general rotation is a combination of three elementary rotations: around the x-axis (x-roll) , around the y-axis (y-pitch) and around the z-axis (z-yaw).

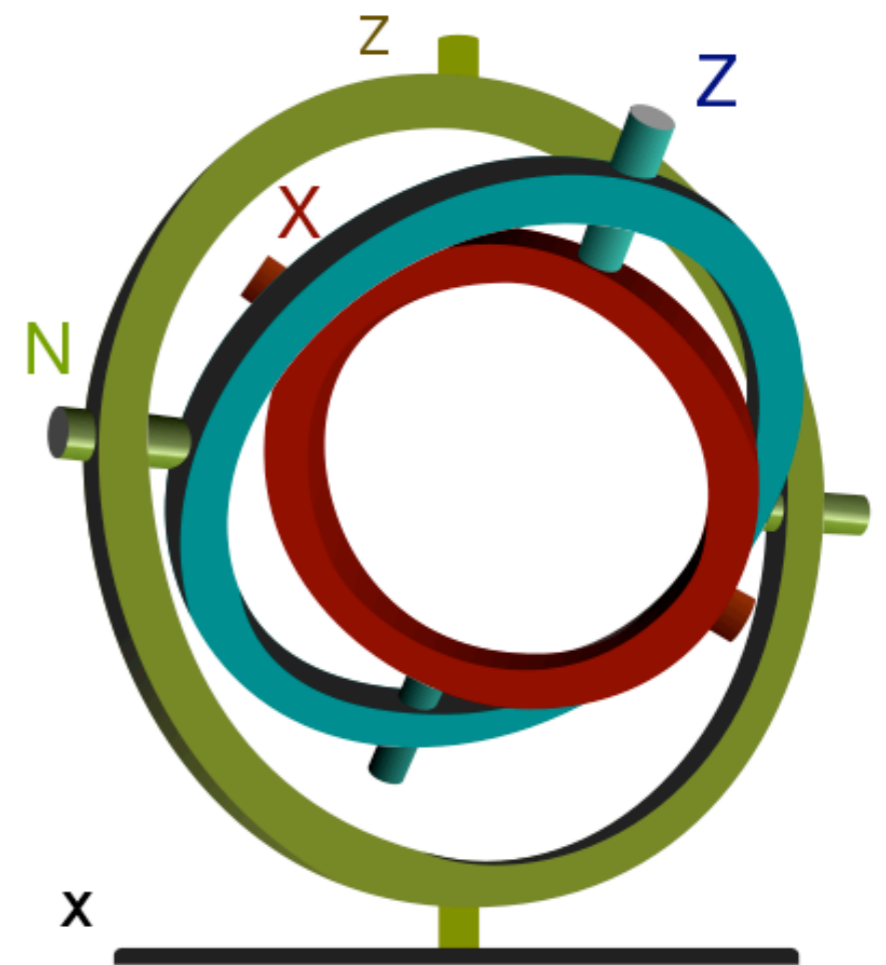
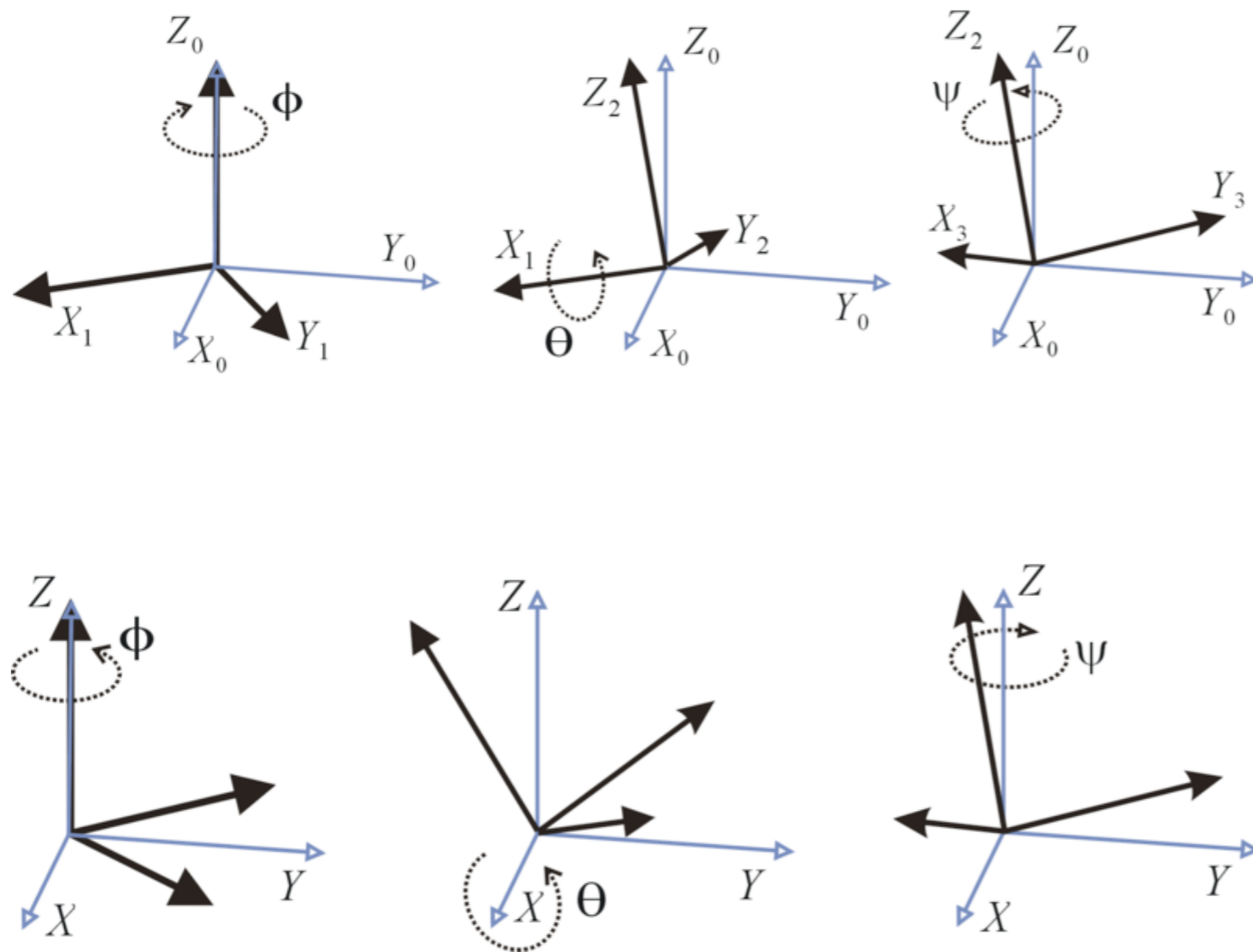


# Gimbal and Euler Angles



**Z-X'-Z''**

# Extrinsic vs. Intrinsic rotations



Wikimedia Commons



# Euler Angles and Rotation Matrices

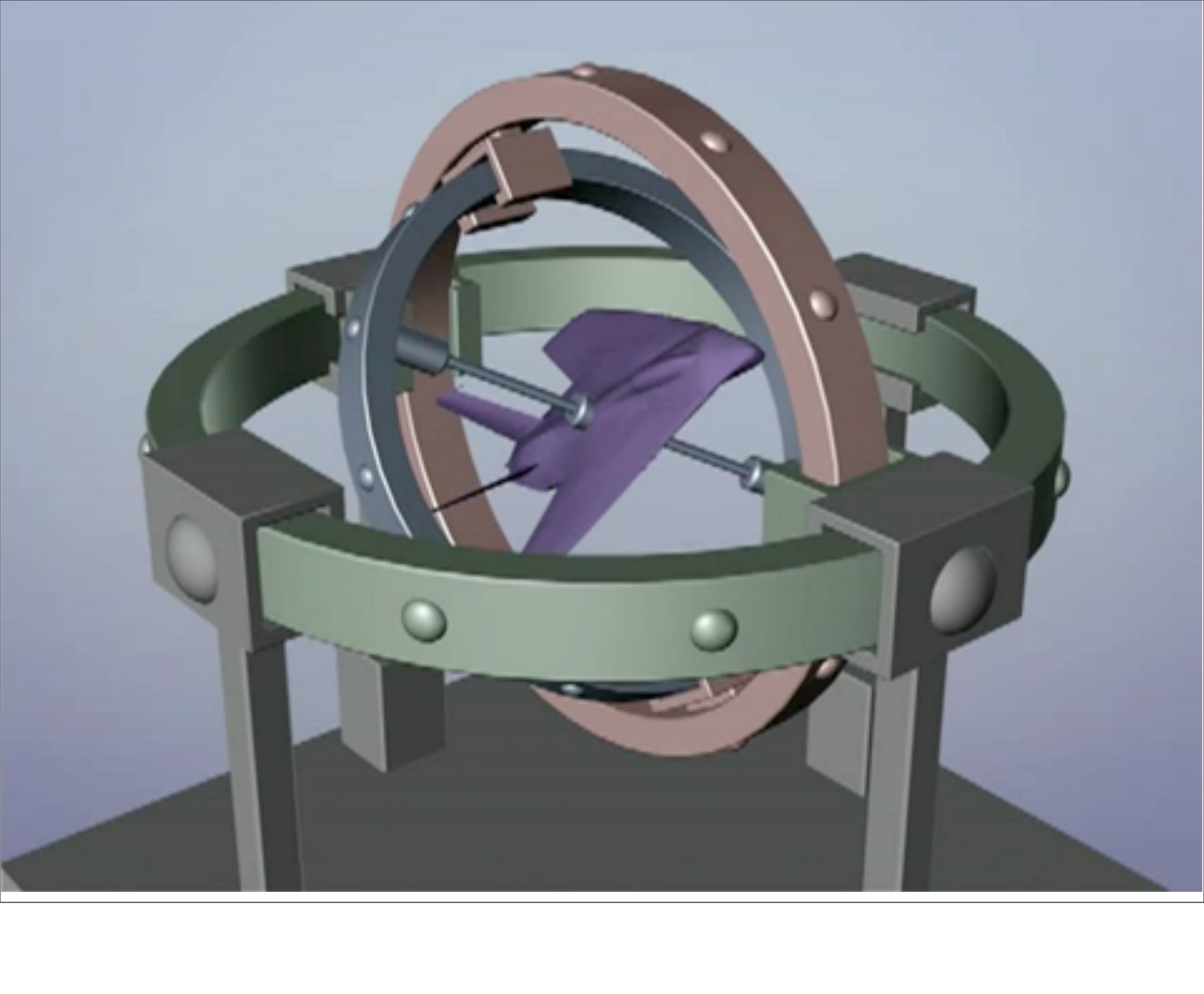
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$$x - \text{roll}(\theta_1) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta_1 & \sin\theta_1 & 0 \\ 0 & -\sin\theta_1 & \cos\theta_1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$y - \text{pitch}(\theta_2) = \begin{pmatrix} \cos\theta_2 & 0 & -\sin\theta_2 & 0 \\ 0 & 1 & 0 & 0 \\ \sin\theta_2 & 0 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$z - \text{yaw}(\theta_3) = \begin{pmatrix} \cos\theta_3 & \sin\theta_3 & 0 & 0 \\ -\sin\theta_3 & \cos\theta_3 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$R(\theta_1, \theta_2, \theta_3) = \begin{pmatrix} c_2 c_3 & c_2 s_3 & -s_2 & 0 \\ s_1 s_2 c_3 - c_1 s_3 & s_1 s_2 s_3 + c_1 c_3 & s_1 c_2 & 0 \\ c_1 s_2 c_3 + s_1 s_3 & c_1 s_2 s_3 - s_1 c_3 & c_1 c_2 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$



**quaternions**

Here as he walked by  
on the 16th of October 1843  
Sir William Rowan Hamilton  
in a flash of genius discovered  
the fundamental formula for  
quaternion multiplication

$$i^2 = j^2 = k^2 = ijk = -1$$

Engraved on a stone of the bridge

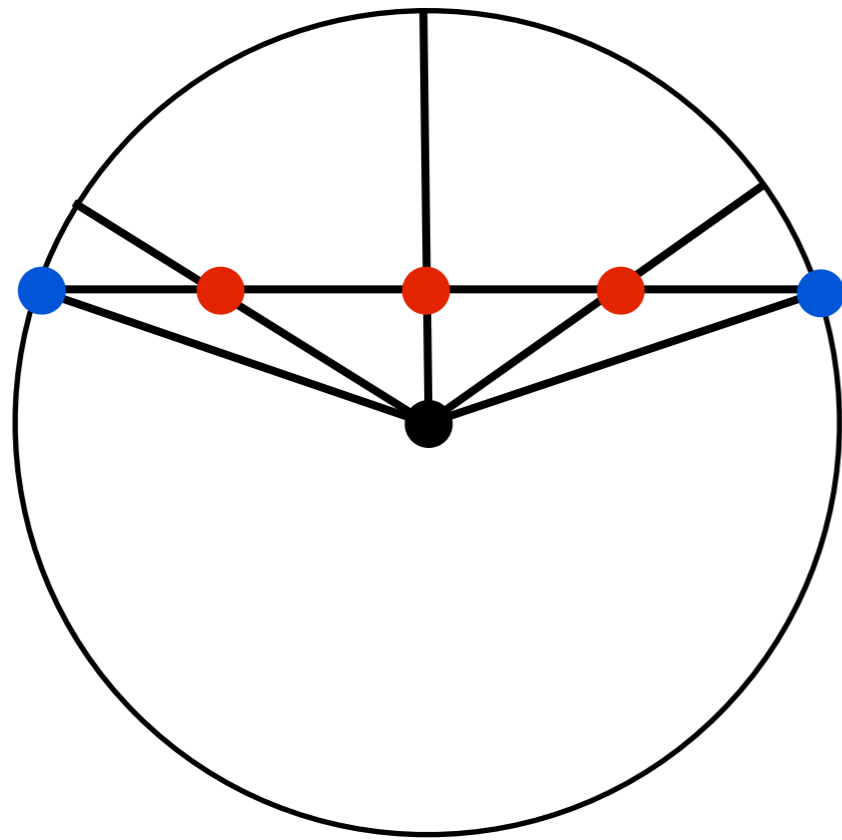
# Quaternions

- axis/angle representation
- interpolates smoothly
- easy to compose

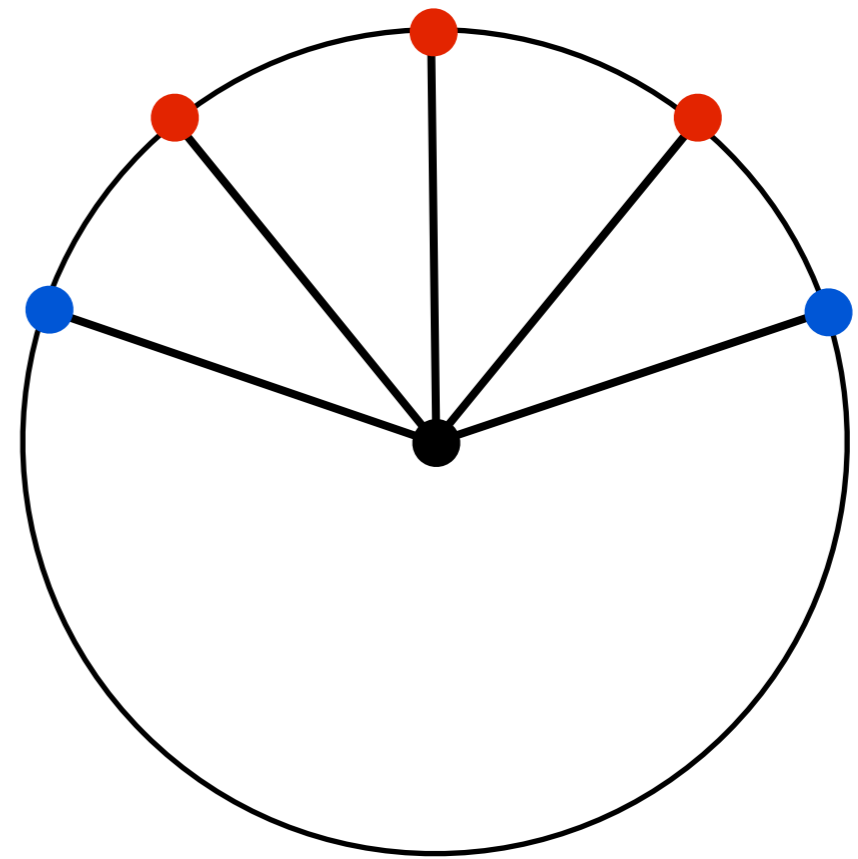
<whiteboard>



# Quaternion Interpolation



linear

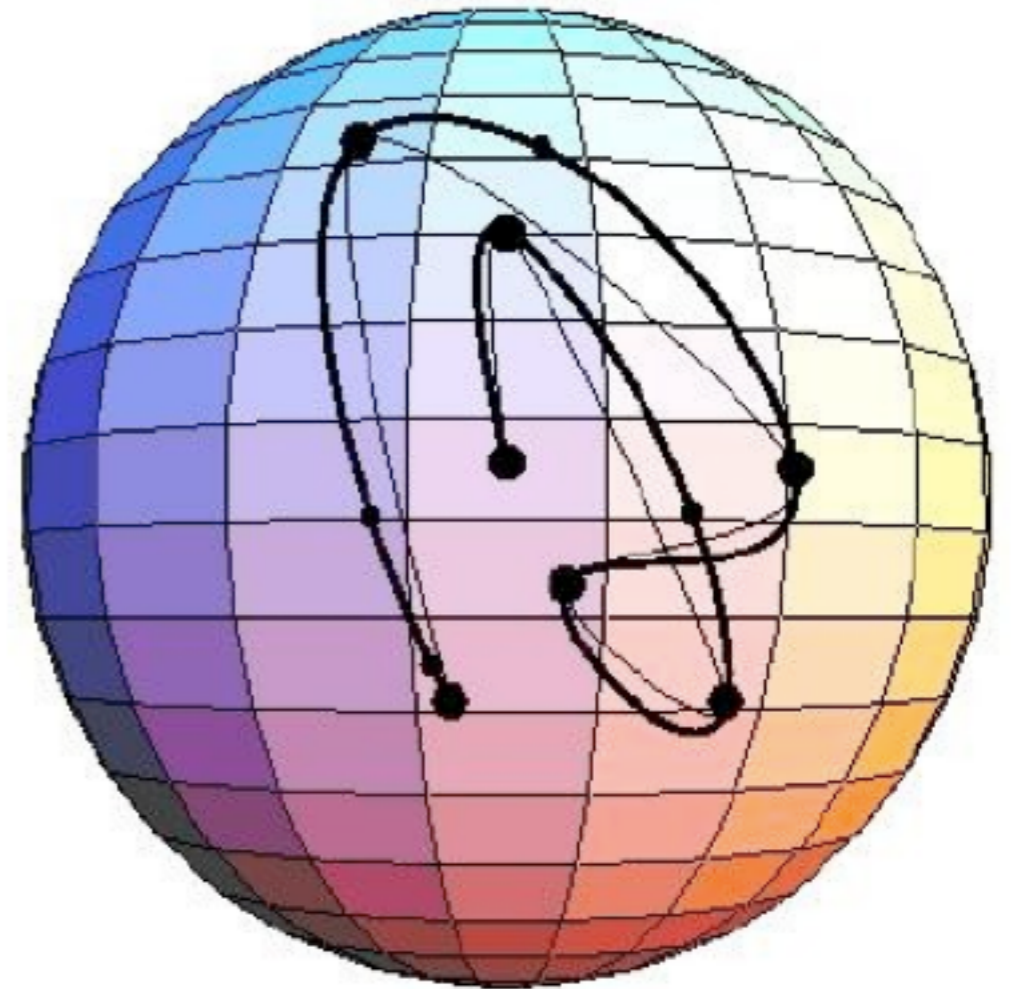


spherical linear  
“slerp”

linear: treat quaternions as 4-vectors, note non-uniform speed  
spherical linear: constant speed

# Higher order interpolation

- Bezier curve
- Shoemake, *Animating rotation with quaternion curves*, 1985



# Matrix form

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$$\mathbf{q} = \begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix}$$

$$\mathbf{R}(\mathbf{q}) = \begin{bmatrix} 1 - 2y^2 - 2z^2 & 2xy + 2wz & 2xz - 2wy & 0 \\ 2xy - 2wz & 1 - 2x^2 - 2z^2 & 2yz + 2wx & 0 \\ 2xz + 2wy & 2yz - 2wx & 1 - 2x^2 - 2y^2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Rotations in Reality

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- It's easiest to express rotations in Euler angles or Axis/angle
- We can convert to/from any of these representations
- Choose the best representation for the task
  - input: Euler angles
  - interpolation: quaternions
  - composing rotations: quaternions, orientation matrix