CS 130 Final

Winter 2018

Name	
Student ID	
Signature	

You may not ask any questions during the test. If you believe that there is something wrong with a question, write down what you think the question is trying to ask and answer that.

Question	Points	Score
True/False		
1	1	
2	1	
3	1	
4	1	
5	1	
6	1	
7	1	
8	1	
9	1	
10	1	
11	1	
12	1	
13	1	
14	1	
15	1	
16	1	
17	1	
18	1	
19	1	
20	1	
Multiple Choice		
21	2	
22	2	
23	2	
24	2	
25	2	
26	2	
27	2	
28	2	
29	2	
30	2	
Written Response		
31	4	
32	8	
33	8	
34	4	
35	8	
36	8	
Total	80	

1 True/False

For each question, indicate whether the statement is true or false by circling T or F, respectively. You get -0.25 points for answering the question incorrectly and 0.5 points for leaving it blank. (It is statistically to your advantage to answer only if you are at least 60% confident that your answer is correct).

- 1. (T/F) OpenGL is a platform independent software interface to graphics hardware.
- 2. (T/F) $f(\mathbf{p}) = \mathbf{N} \cdot (\mathbf{p} \mathbf{q}) = 0$, where **N** is a normal vector, and **q** a point, is an implicit line equation in 2D or implicit plane equation in 3D.
- 3. (T/F) The Phong reflectance model can be used both within the OpenGL graphics pipeline approach to rendering and within a ray tracing framework.
- 4. (T/F) Matrix multiplication is commutative.
- 5. (T/F) Let T be a translation matrix, R be a rotation matrix, and **p** be a point. Then the product $TR\mathbf{p}$ first rotates the point and then translate it.
- 6. (T/F) Scaling and rotating are both examples of linear transformations.
- 7. (T/F) The camera transformation in the graphics pipeline is an example of a rigid transformation.
- 8. (T/F) This matrix is a rigid body transformation

$$\begin{pmatrix} \cos\theta & -\sin\theta & 0 & 0\\ \sin\theta & \cos\theta & 0 & 1\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{pmatrix}$$

9. (T/F) This matrix reflects about the yz-plane

$$\left(\begin{array}{rrrrr} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array}\right)$$

- 10. (T/F) The z-buffer stores the depth of each pixel in order to resolve fragment visibility issues.
- 11. (T/F) The order of operations in the graphics pipeline is as follows: modelview transformation, projection transformation, divide by w, viewport transform.
- 12. (T/F) Sets of parallel lines remain parallel under orthographic projection in the OpenGL graphics pipeline.
- 13. (T/F) When rasterizing a triangle under a perspective projection, linear interpolation with screen-space barycentric weights can be used to determine fragment depth values.
- 14. (T/F) In keyframe character animation, interpolation between keyframe character poses is used to produce the illusion of continuous motion.
- 15. (T/F) When doing physical simulation, use of a smaller time step for the numerical time integration has the advantage of speeding up the overall computation and improving accuracy.
- 16. (T/F) A Bezier curve of degree n + 1 has n distinct control points.
- 17. (T/F) If all control points of a Bezier curve lie on a line, then the Bezier curve lies on that line.
- 18. (T/F) Newton's second law states that the mass times acceleration of a particle is equal to the net force on the particle.

2 Multiple Choice

For each question, circle exactly one of (a)-(e), unless otherwise stated.

- 21. Which statement about transformations in the OpenGL pipeline is true?
 - (a) Changing the order of applied transformation matrices would not affect the final position of a point.
 - (b) Vertex positions and normal vectors are both translated the same way when multiplied by a transformation matrix representing a translation.
 - (c) The 4-vector (x, y, z, 0) represents the three-dimensional point located at (x, y, z).
 - (d) The 4-vectors (1, 2, 3, 4) and (2, 4, 6, 8) represent the same physical point.
 - (e) None of the above.
- 22. Match the type of transformation in the left column with the example transformation matrix in the right by drawing lines between the matching boxes.



23. OpenGL perspective projection

- (a) preserves parallel lines.
- (b) preserves the z ordering between the near and far planes, but not necessarily everywhere else.
- (c) preserves the z ordering everywhere.
- (d) is a linear transformations in z.
- (e) is an affine transformations.

- 24. Perspective correct interpolation
 - (a) is needed for implementing the z-buffer in the graphics pipeline.
 - (b) is rarely needed.
 - (c) requires completely reversing all the geometric transformations in the graphics pipeline.
 - (d) is important when using texture maps in the graphics pipeline.
 - (e) none of the above.
- 25. Which statement about curves is true?
 - (a) OpenGL has built-in functions for drawing Bezier curves.
 - (b) Bezier curves go through all of their control points.
 - (c) High order polynomials are often used to interpolate large collections of points representing an object surface.
 - (d) Spline curves do not have good smoothness properties.
 - (e) Bezier curves are contained in the convex hull of their control points.

- 26. Which statement about curves is <u>false</u>?
 - (a) The cubic Bezier curve approximating 4 data points is the unique cubic that interpolates the 4 points.
 - (b) There is a unique n degree polynomial that interpolates n + 1 distinct data points.
 - (c) The monomial basis for curves up to degree 3 is the set $1, u, u^2, u^3$.
 - (d) The blending functions for a degree 3 Bezier curve are all of degree 3.
 - (e) When using piecewise polynomial curves to interpolate a set of data points, care must be taken at join points to ensure the desired level of continuity.
- 27. Which statement about physics-based simulation is true?
 - (a) The coefficient of restitution is applied to the tangential velocity of a particle to create an effect/illusion of friction.
 - (b) In particle simulations, applying the forward Euler method to update velocities and positions would naturally handle collisions.
 - (c) A large time step reduces the effects of errors due to numerical integration in time.
 - (d) Using a rigid body approximation can significantly reduce the number of degrees of freedom of a very stiff object.
 - (e) None of the above.
- 28. Which statement about OpenGL is <u>false</u>?
 - (a) In OpenGL, the ModelView matrix can represent rotation, scale, and translation of an object.
 - (b) A quadrilateral can be represented by two triangles in OpenGL.
 - (c) In an OpenGL program, the number of popMatrix operations can be higher or equal to the number of pushMatrix operations.
 - (d) Translating an object by (1,0,0) before rotating by 90 degrees is <u>not</u> the same as rotating the object by 90 degrees after translating by (1,0,0).
 - (e) The modern OpenGL graphics pipeline is a programmable pipeline.
- 29. Which of the following statements about animation is true?
 - (a) A triangle mesh consisting of masses and springs can be used to simulate falling cloth.
 - (b) Determining the joint angles on a skeleton arm so that its hand is in a desired end position is the problem of Forward Kinematics.
 - (c) Principles such as squash and stretch apply to hand-drawn animation, not computer-generated animation.
 - (d) In keyframe animation, a character's motion is determined by the shape of the interpolating curve but not by the particular time parameterization of the curve.
 - (e) None of the above.

3 Written Response

- 31. Write down the transformation matrices as stated in each part.
 - (a) Write down the 4×4 3D matrix to translate a point by (x, y, z).
 - (b) Write down the 4×4 3D matrix to rotate counter-clockwise by an angle θ about the z-axis.
 - (c) Write down the 4×4 3D matrix to scale an object by 50% in all directions.
 - (d) Write down the 2D rotation matrix that rotates by 90 degrees <u>clockwise</u>.

32. Find a sequence of transformation matrices that map the triangle ABC to the triangle A'B'C'. Sketch the triangle after each transformation. How are these transformation matrices combined into a single transformation matrix to map ABC to A'B'C'?



33. Find the inverse of the rigid body transformation

$$\begin{pmatrix} R & \mathbf{t} \\ 0 & 0 & 0 & 1 \end{pmatrix},$$

where R is a 3×3 rotation matrix and **t** is a 3-vector.

34. Consider the cubic Bezier curve $f(u) = a_0 + a_1u + a_2u^2 + a_3u^3$ with control points p_0, p_1, p_2, p_3 , which is given by the conditions

$$f(0) = p_0$$

$$f'(0) = 3(p_1 - p_0)$$

$$f'(1) = 3(p_3 - p_2)$$

$$f(1) = p_3$$

(a) Write down the 4×4 matrices C and P such that

$$C\begin{pmatrix}a_0\\a_1\\a_2\\a_3\end{pmatrix} = P\begin{pmatrix}p_0\\p_1\\p_2\\p_3\end{pmatrix}$$

(b) Given that $B = C^{-1}P$ is given by the following matrix

$$B = \begin{pmatrix} 1 & 0 & 0 & 0 \\ -3 & 3 & 0 & 0 \\ 3 & -6 & 3 & 0 \\ -1 & 3 & -3 & 1 \end{pmatrix},$$

what are the cubic Bezier blending functions $b_0(u), b_1(u), b_2(u), b_3(u)$?

35. Use the de Casteljau algorithm to evaluate the position of the cubic Bezier curve with its control points at (0,0), (0,1), (1,1), (1,0) for parameter values u = 0.5 and u = 0.75. Drawing a sketch will help you do this.