The general algorithm for ray tracing is as follows:
for each pixel (i,j):
Compute the 'world position' of the pixel
Create a ray from the camera position to the world position of the pixel Cast the ray and evaluate the color of the pixel:

Find the closest object that intersects with the ray.
Get the pixel color by using Shader_Surface function of a shader.
If there are no objects, use background_shader
else, use the intersected object material_shader

Please find the appropriate files in the skeleton code and fill the blanks below.

1. World_Position function in Camera class, returns the world position of a given pixel (ivec2 pixel_index).
a. World_Position function is implemented in camera.cpp starting from line \# $\qquad$ .
2. Cell_Center function in Camera class, returns the screen position of a given pixel, ivec2 pixel_index.
a. Cell_Center function is implemented in camera.h starting from line \#
$\qquad$ .
3. Locate where the loop that iterates through all pixels are located.
a. The loop is located in $\qquad$ function in render_world.cpp
4. Cast_Ray function in render_world.cpp returns the color of the pixel using the shader of the closest object it intersects with. Find the function in render_world.cpp and fill below.
a. Cast_Ray function is implemented in render_world.cpp starting from line \# $\qquad$ -
b. Cast_Ray function is called in $\qquad$ function in render_world.cpp.
5. Closest Intersection function will be used in Cast Ray function to find the closest object that intersects with the ray and (if any) provide it's intersection information in a object of type Hit.
a. Closest_Intersection function is implemented in render_world.cpp starting from line \# $\qquad$ .
b. The output object hit should store the following information:
$\qquad$ -
c. Any intersection with distance <= small_t should be $\qquad$ .
6. Intersection function is a function of the Object class (object.h) which is a base class for scene objects such as plane and sphere. This function is overloaded by these classes and should return true if the object intersects with the ray and return an hit object the closest intersection.
7. Vectors. Given that $u$ and v are vec3 objects storing 3D vectors, fill the missing cells in the table below with code or it's explanation.

| Code | Description |
| :---: | :---: |
| $\begin{aligned} & \mathrm{u}[0]=5 \\ & \mathrm{v}[2]=6 \end{aligned}$ | Sets $u_{x}, \mathrm{x}$ component of u , to 5 <br> Sets $v_{z}, \mathrm{z}$ component of v , to 6 |
| vec3 $\mathrm{m}=\mathrm{u}+\mathrm{v}$ |  |
| vec3 $\mathrm{p}=\mathrm{u}[0] * v$ |  |
| double $k=\operatorname{dot}(\mathrm{u}, \mathrm{v})$ |  |
|  | Create a vec3 c that stores the cross product of $u$ and $v$ |
|  | returns magnitude (length) of $u$ |
| u.normalized() | returns u/\|u| <br> (the unit vector in u's direction) |
|  | Create a vec3 k, such that $k=\frac{(u \cdot v) u}{\|u\|^{2}}$ |
| cout << u << endl; | prints vector u (values separated with commas) |

## GETTING STARTED WITH THE RAY TRACER PROJECT

Compile: scons
Run test N (00-29): ./ray_tracer -i ./tests/N.txt
Compare test $N$ (00-29): ./ray_tracer -i ./tests/N.txt -s ./tests/N.png
Run grading script: ./grading-script.py .

Functions to implement for this lab:
$\square$ camera.cpp: World_Position
$\square$ render_world.cpp: Render_Pixel (only ray construction)
$\square$ render_world.cpp: Closest_Intersection
$\square$ render_world.cpp: Cast_Ray
$\square$ sphere.cpp: Intersection: returns intersection of ray and the sphere.
$\square$ plane.cpp: Intersection: returns intersection of ray and the plane.

## Important Classes:

```
render_world.h/cpp:
class Render_World: //Stores the rendering parameters such as
    std::vector<Object*> objects //list of objects in the scene
    std::vector<Light*> lights; //list of lights in the scene
    Camera camera; //the camera object (see below)
```


## camera.h/cpp:

```
class Camera: // Stores the camera parameters, such as the camera position
```

                        // screen horizontal and vertical vectors etc.
    object.h:
class Hit: // Stores the ray object intersection data such as the distance
// from the endpoint to the intersection point with the object.
ray.h:
class Ray // stores ray parameters: end_point, direction
vec3 Point(double t); // returns the point on the ray at distance t, // i.e. (end_point + direction * t)
sphere.h/cpp:
class Sphere // Stores sphere parameters (center, radius)
plane.h/cpp:
class Plane // Stores plane parameters (x0, normal)

## World position of a pixel (camera.cpp):

The world position of a pixel can be calculated by the following formula:

$$
F_{p}+u C_{x}+v C_{y}
$$

$u$ : horizontal_vector, $v:$ vertical_vector,
and $F_{p}$ : film_position (bottom left corner of the screen)
$C:$ of type vec2 can be obtained by Cell_Center(pixel_index) //see camera.h

Constructing the ray (Render_Pixel function):
end_point: camera position (from camera class)
direction: a unit vector from the camera position to the world position of the pixel.
vec3 class has normalized() function that returns the normalized vector;
e.g. (v1-v2).normalized()

## Closest_Intersection:

The pseudo code is:

```
Set min_t to a large value (google std numeric_limits)
For each object* in objects:
        use object-> Intersect to get the hit with the object
        If hit is the closest so far and larger than small_t
        (i.e. with smallest t, that is larger than small_t)
            then store the hit as the closest hit
return closest hit
```


## Cast_Ray:

Get the closest hit with an object using Closest_Intersection If there is an intersection:

Set color using the object Shade_Surface function which calculates and returns the color of the ray/object intersection point.
Shade_Surface receives as parameters: ray, intersection point, normal at the intersection point and recursion_depth. You can get the intersection point using the ray object and the normal using the object pointer inside the hit object.
Else (if there is no intersection)
Use background_shader of the render_world class. The background shader is a flat_shader so you can use any $3 d$ vector as parameters.

Credits: Muzaffer Akbay (Winter/17), Revision: Cassio (Fall/18)

