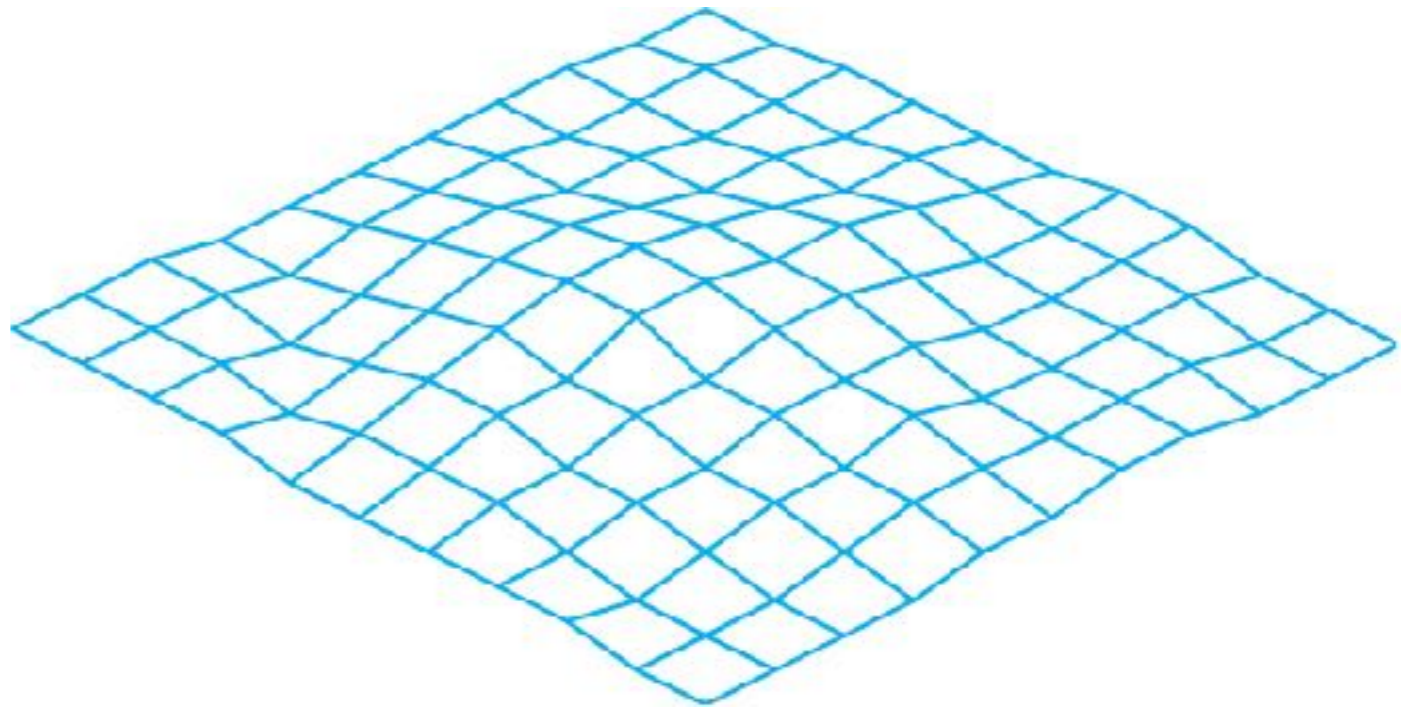


# Shading Polygonal Geometry

# Smooth surfaces are often approximated by polygons

Shading approaches:

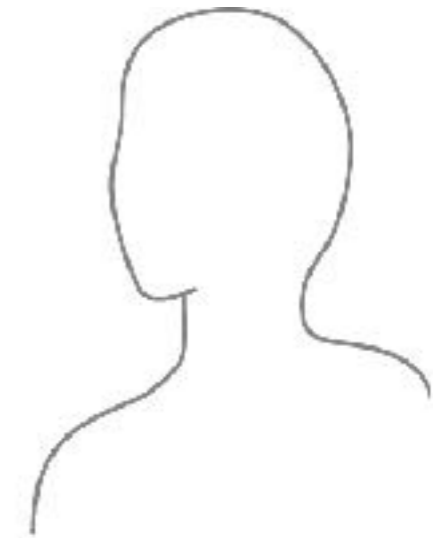
1. Flat
2. Smooth (Gouraud)
3. Phong





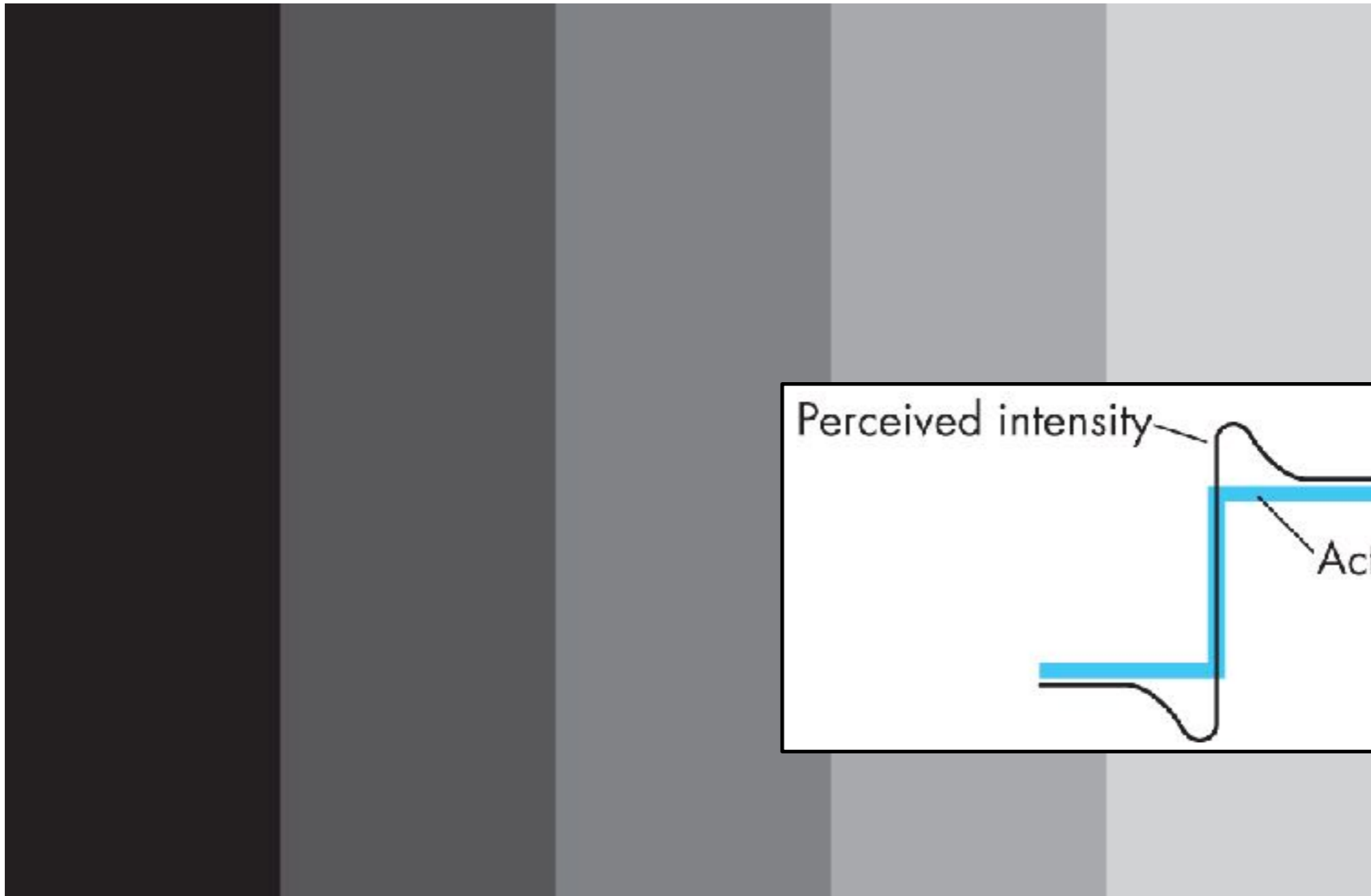
do the shading calculation once per **polygon**

# Flat Shading



valid for light at  $\infty$   
and viewer at  $\infty$   
and faceted surfaces

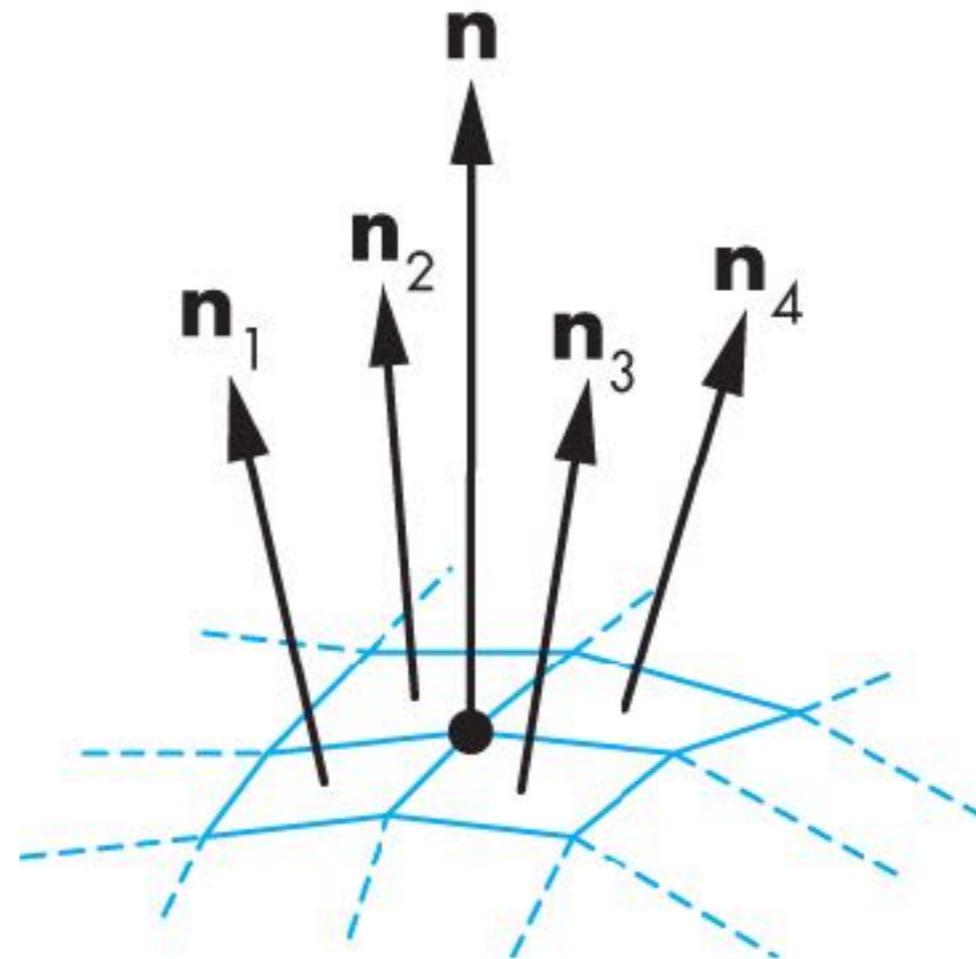
# Mach Band Effect





# Smooth Shading

$$\mathbf{n} = \frac{\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4}{\|\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4\|}$$

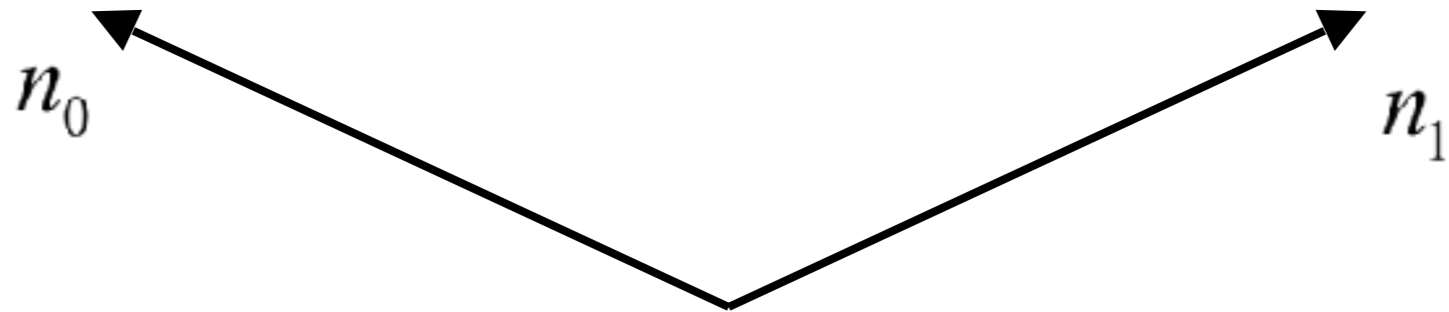


do the shading calculation once per **vertex**

# Interpolating Normals

---

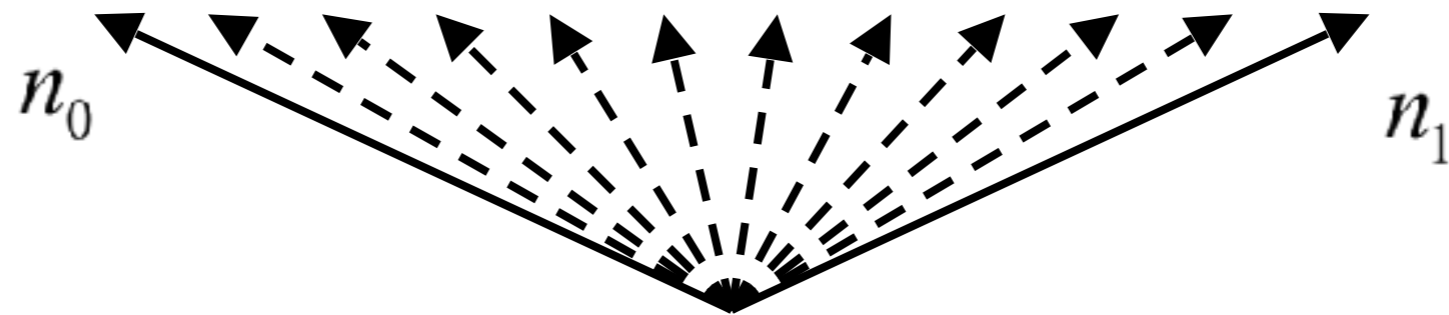
- Must renormalize



# Interpolating Normals

---

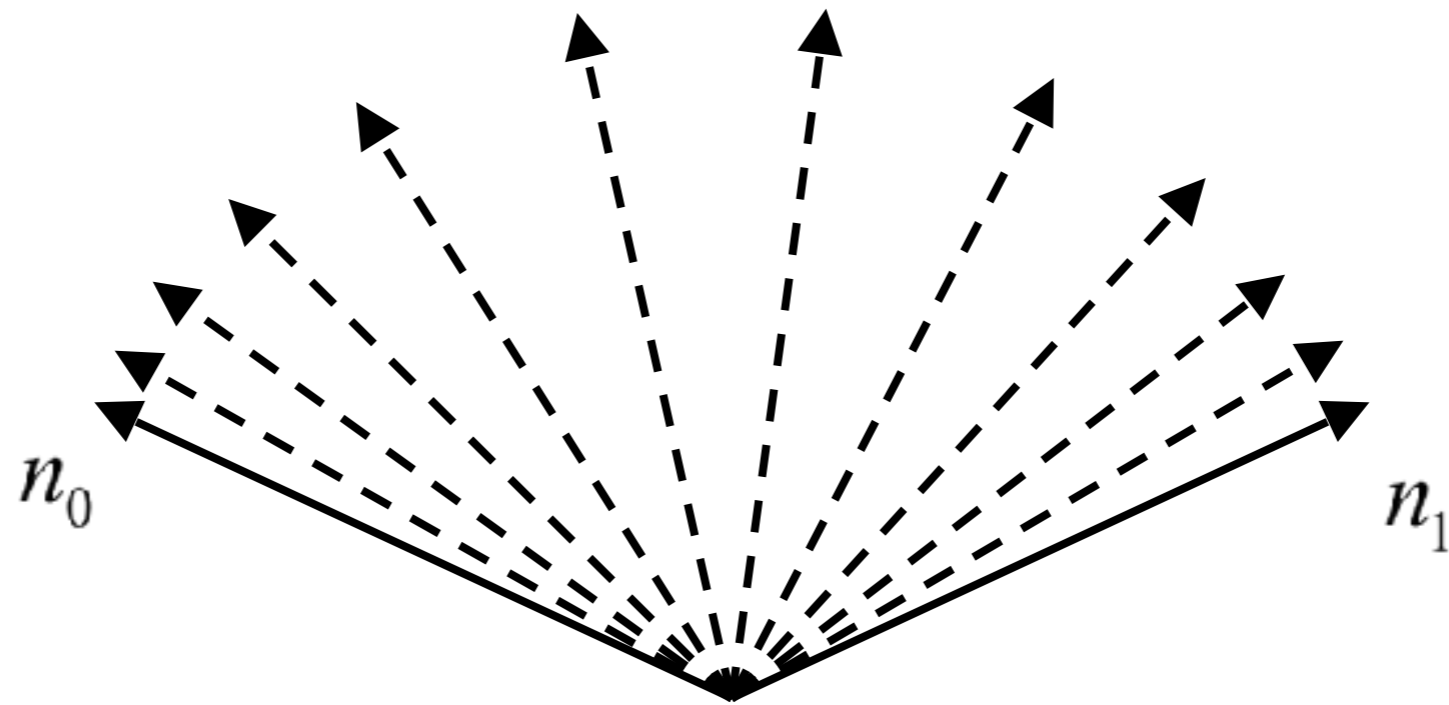
- Must renormalize



# Interpolating Normals

---

- Must renormalize

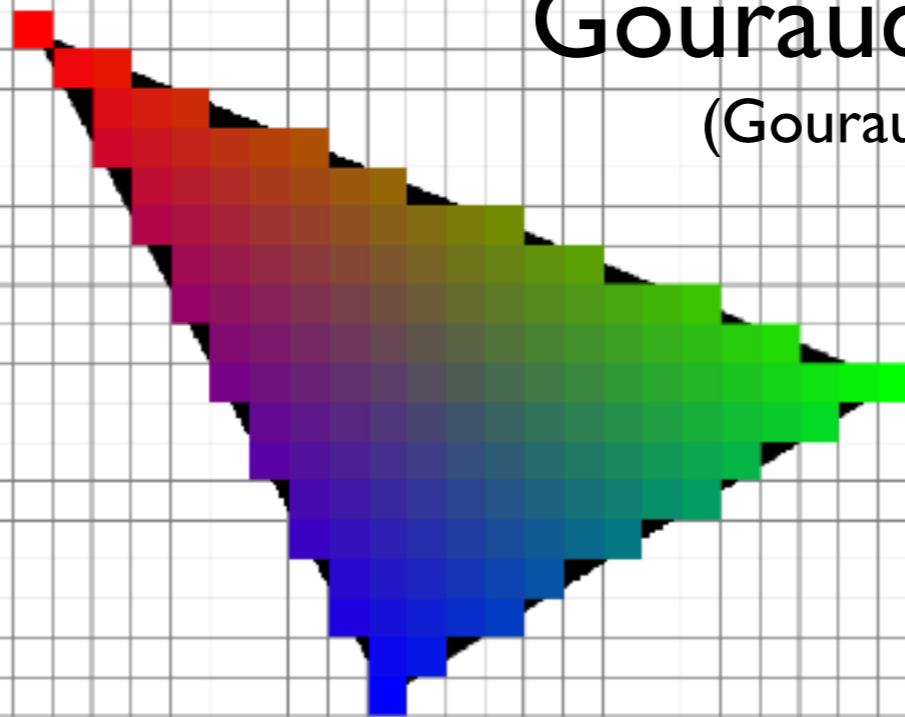




# We can interpolate attributes using barycentric coordinates

$$\mathbf{c} = \alpha \mathbf{c}_0 + \beta \mathbf{c}_1 + \gamma \mathbf{c}_2$$

**Gouraud shading**  
(Gouraud, 1971)

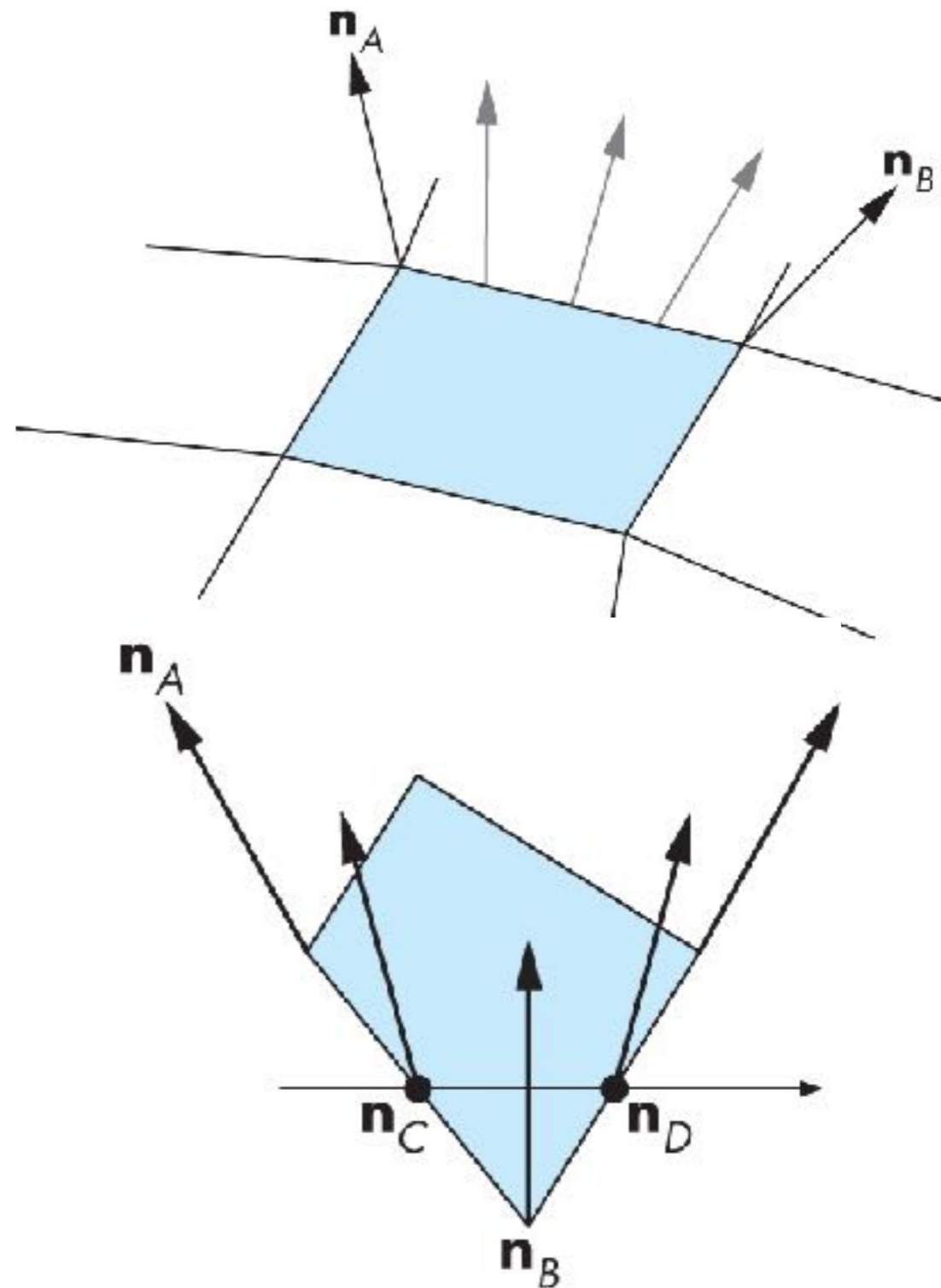


<http://jtibble.dyndns.org/graphics/eecs487/eecs487.html>



do the shading calculation once per **fragment**

# Phong Shading

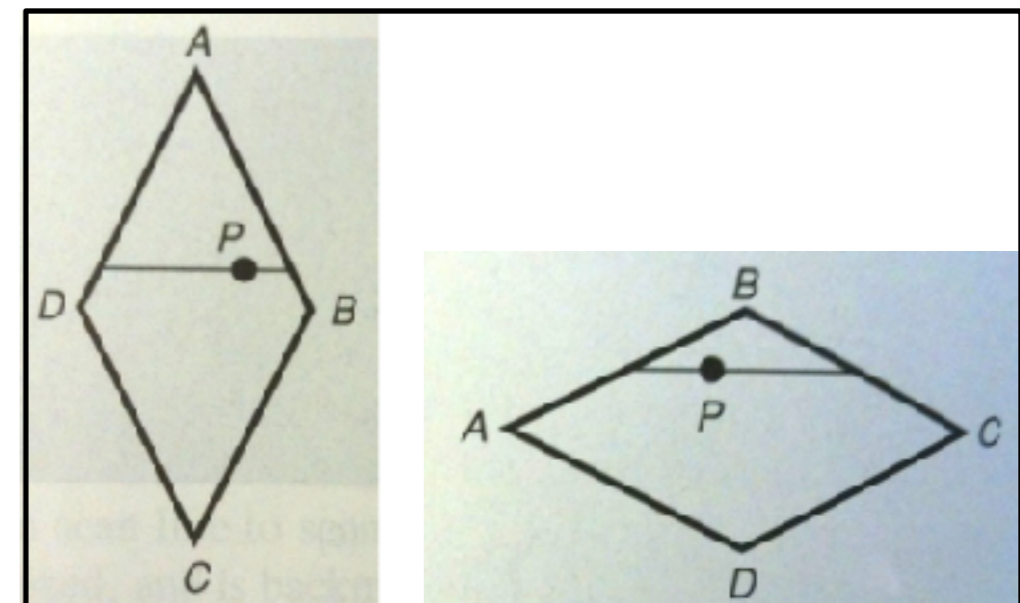
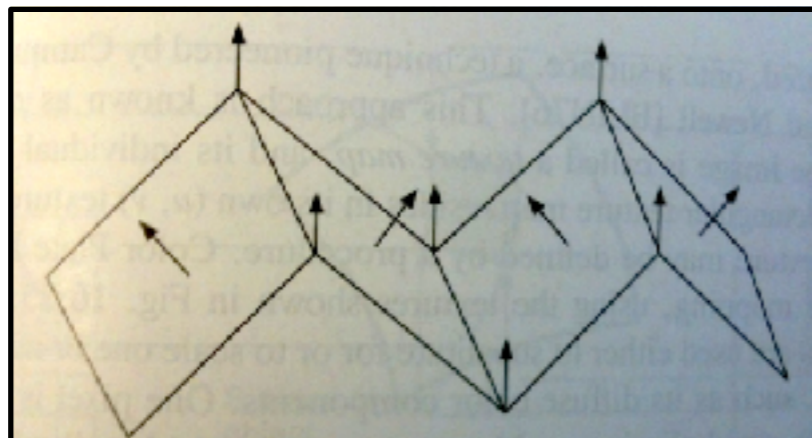
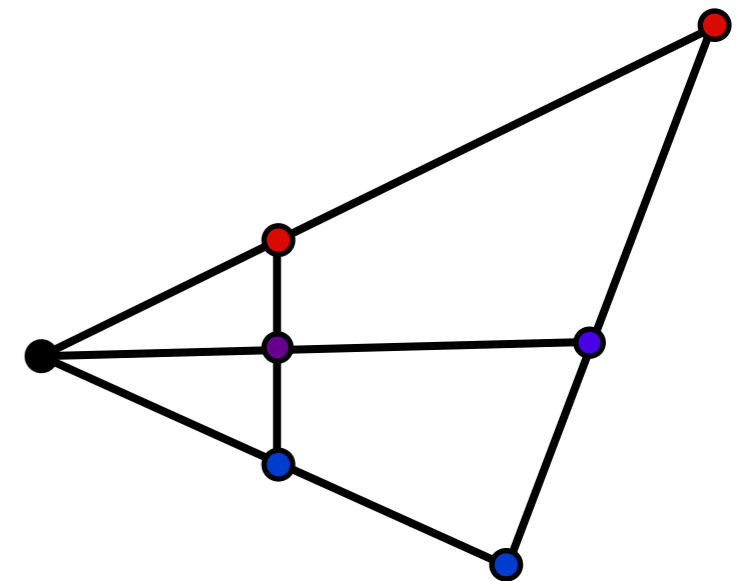


# Comparison



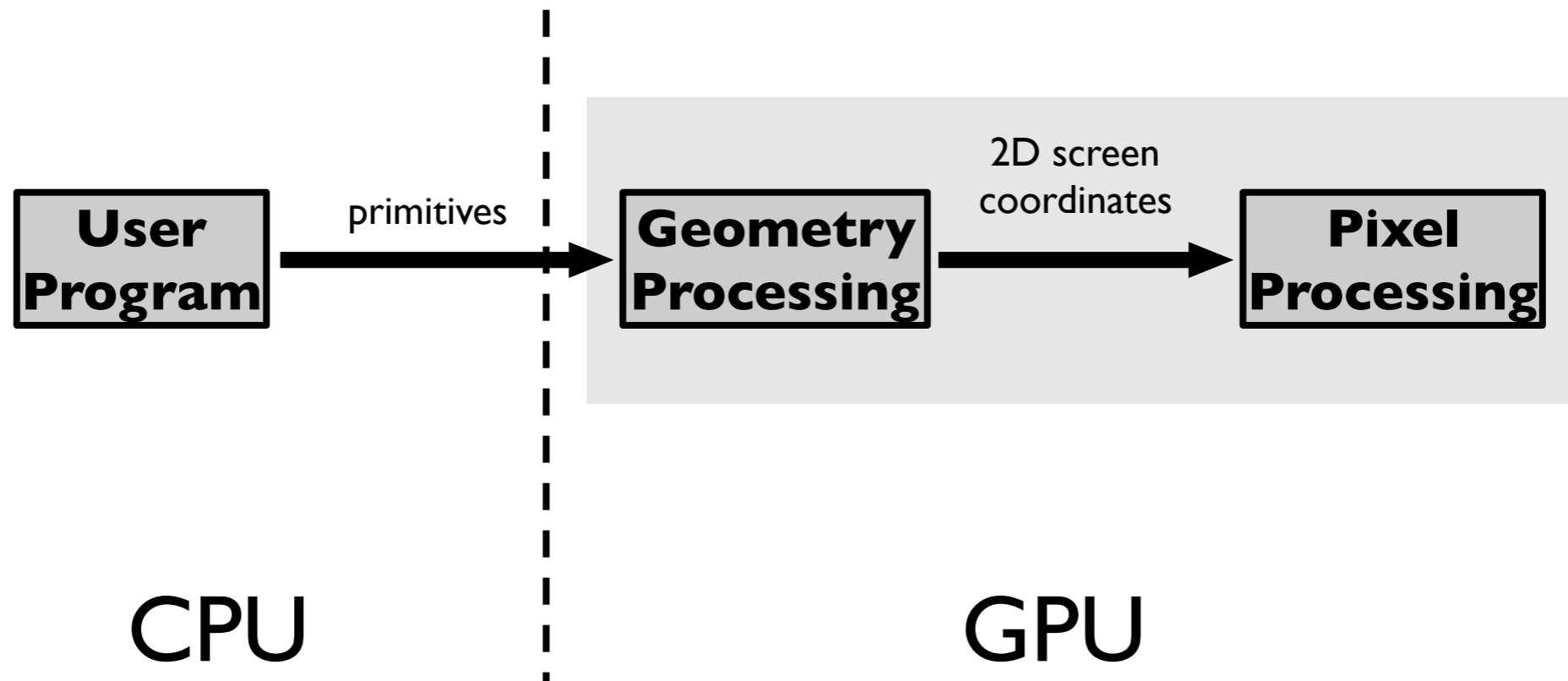
# Problems with Interpolated Shading

- Polygonal silhouette
- Perspective distortion
- Orientation dependence
- Unrepresentative surface normals



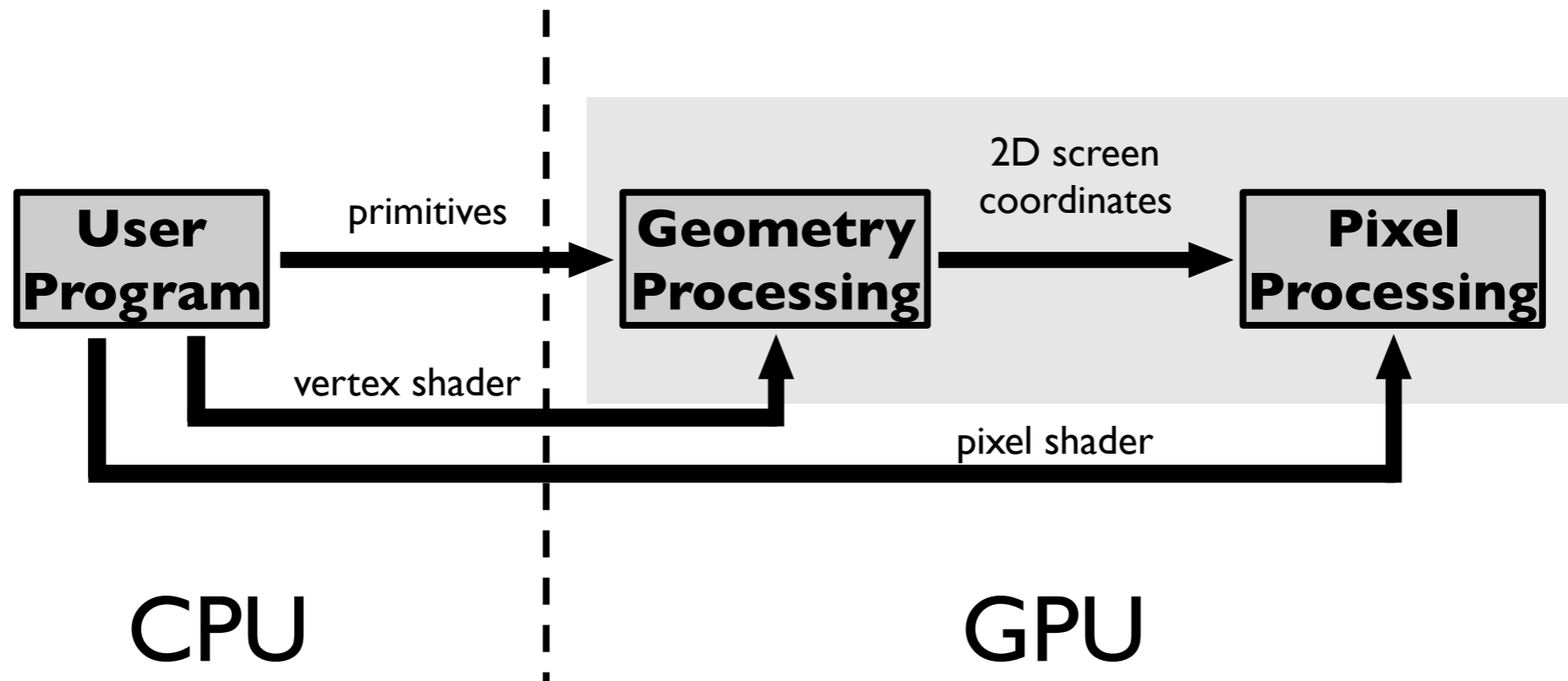
# Programmable Shading

# Fixed-Function Pipeline



Control pipeline through GL state variables

# Programmable Pipeline



Supply shader programs to be executed on GPU  
as part of pipeline

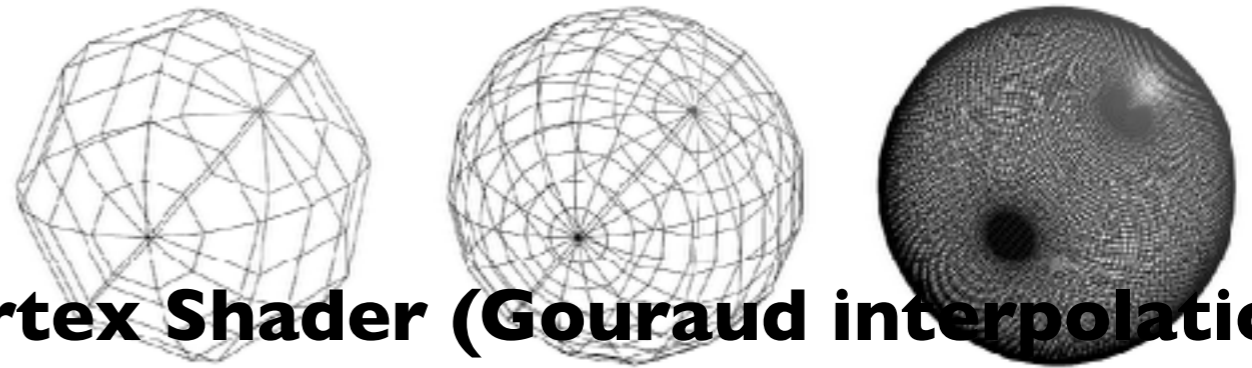
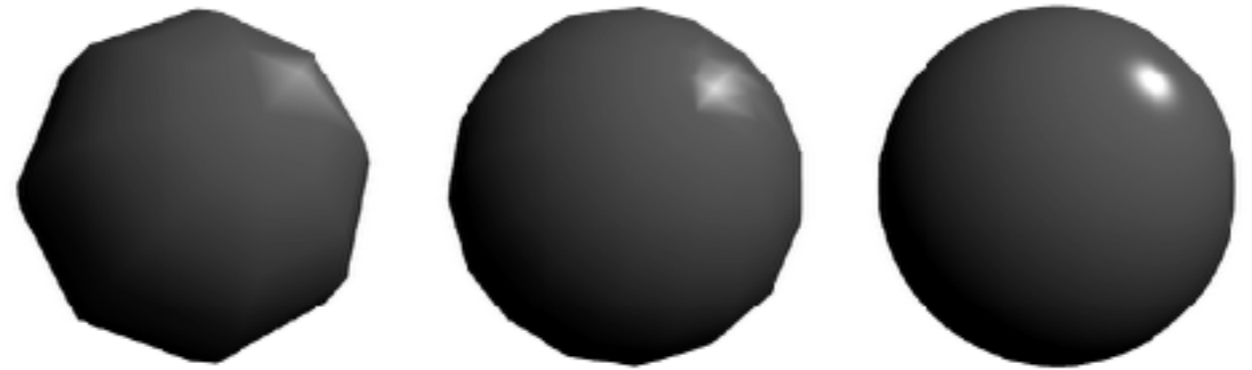
# Phong reflectance in vertex and pixel shaders using GLSL

```
void main(void)
{
    vec4 v = gl_modelView_Matrix * gl_Vertex;
    vec3 n = normalize(gl_NormalMatrix * gl_Normal);
    vec3 l = normalize(gl_lightSource[0].position - v);
    vec3 h = normalize(l - normalize(v));

    float p = 16;
    vec4 cr = gl_FrontMaterial.diffuse;
    vec4 cl = fl_LightSource[0].diffuse;
    vec4 ca = vec4(0.2, 0.2, 0.2, 1.0);

    vec4 color;
    if (dot(h,n) > 0)
        color = cr * (ca + cl * max(0,dot(n,l)))
            + cl * pow(dot(h,n), p);
    else
        color = cr * (ca + cl * max(0,dot(n,l)));

    gl_FrontColor = color;
    gl_Position = ftransform();
}
```



**Vertex Shader (Gouraud interpolation)**

```
varying vec4 v;
varying vec3 n;

void main(void)
{
    vec3 l = normalize(gl_lightSource[0].position - v);
    vec3 h = normalize(l - normalize(v));

    float p = 16;
    vec4 cr = gl_FrontMaterial.diffuse;
    vec4 cl = fl_LightSource[0].diffuse;
    vec4 ca = vec4(0.2, 0.2, 0.2, 1.0);

    vec4 color;
    if (dot(h,n) > 0)
        color = cr * (ca + cl * max(0,dot(n,l)))
            + cl * pow(dot(h,n), p);
    else
        color = cr * (ca + cl * max(0,dot(n,l)));

    gl_FragColor = color;
}
```



**Pixel Shader (Phong interpolation)**

[Shirley and Marschner]





*Call of Juarez DX10 Benchmark,ATI*



*Rusty car shader, NVIDIA*

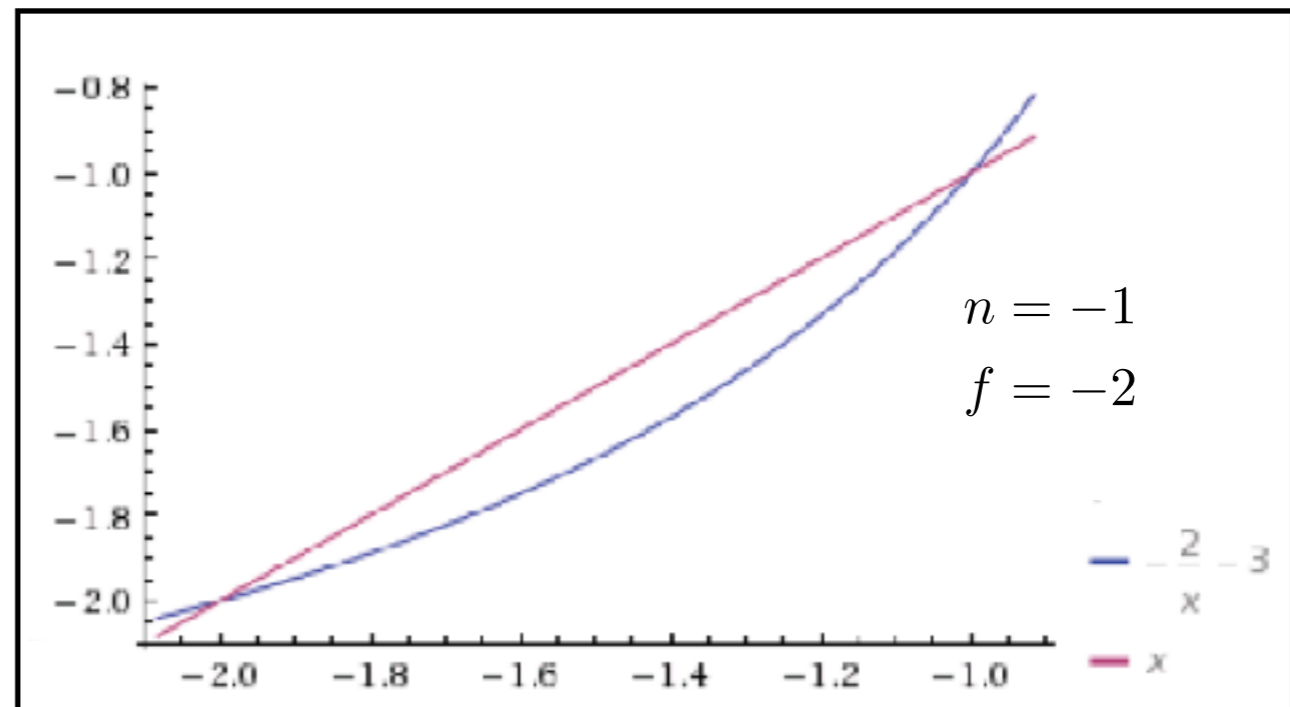
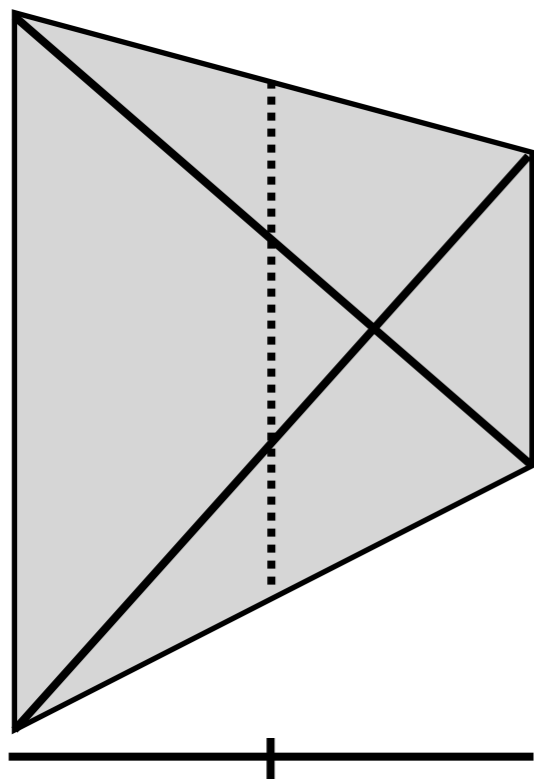


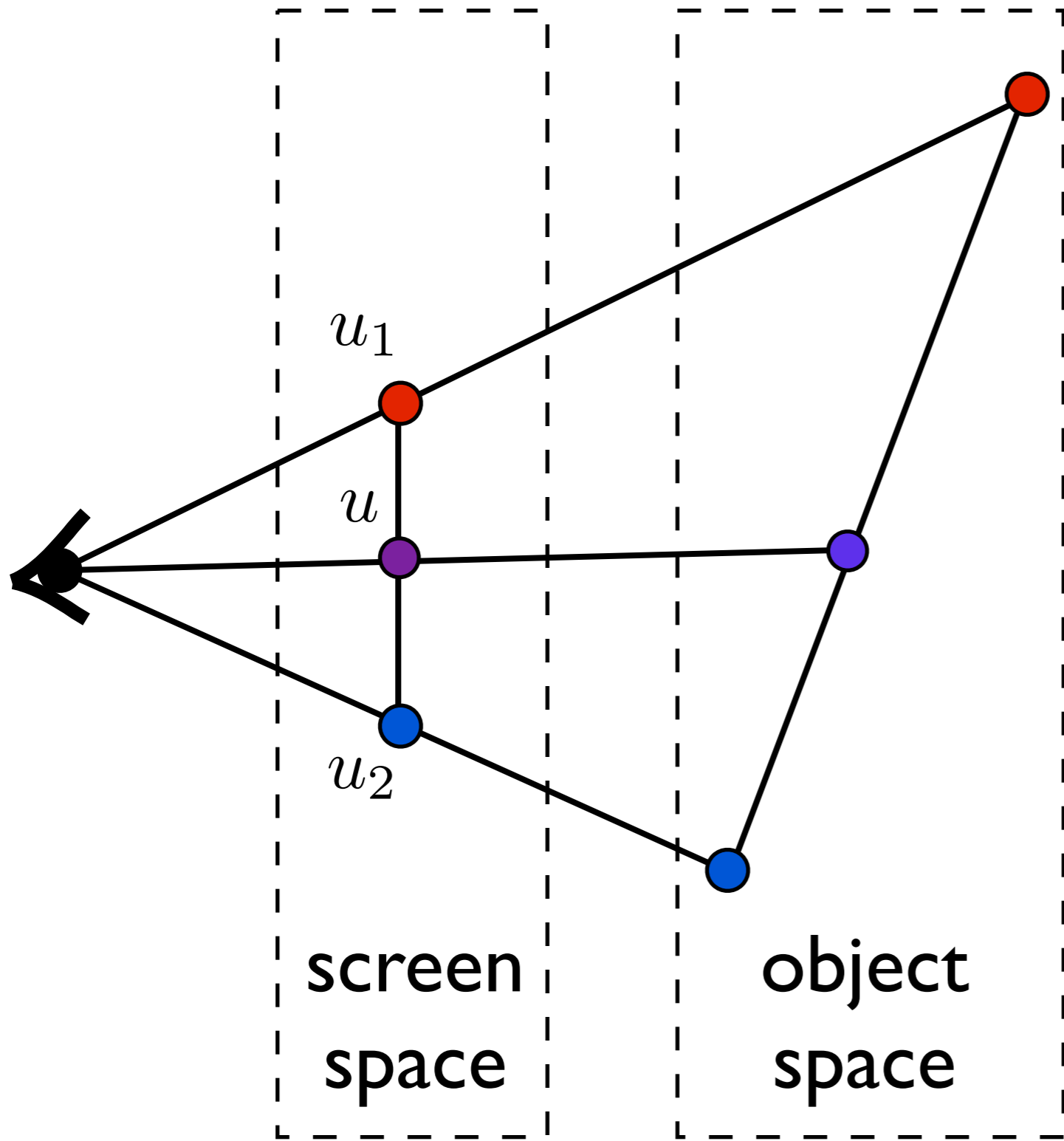
*Dawn, NVIDIA*

Perspective correct  
interpolation

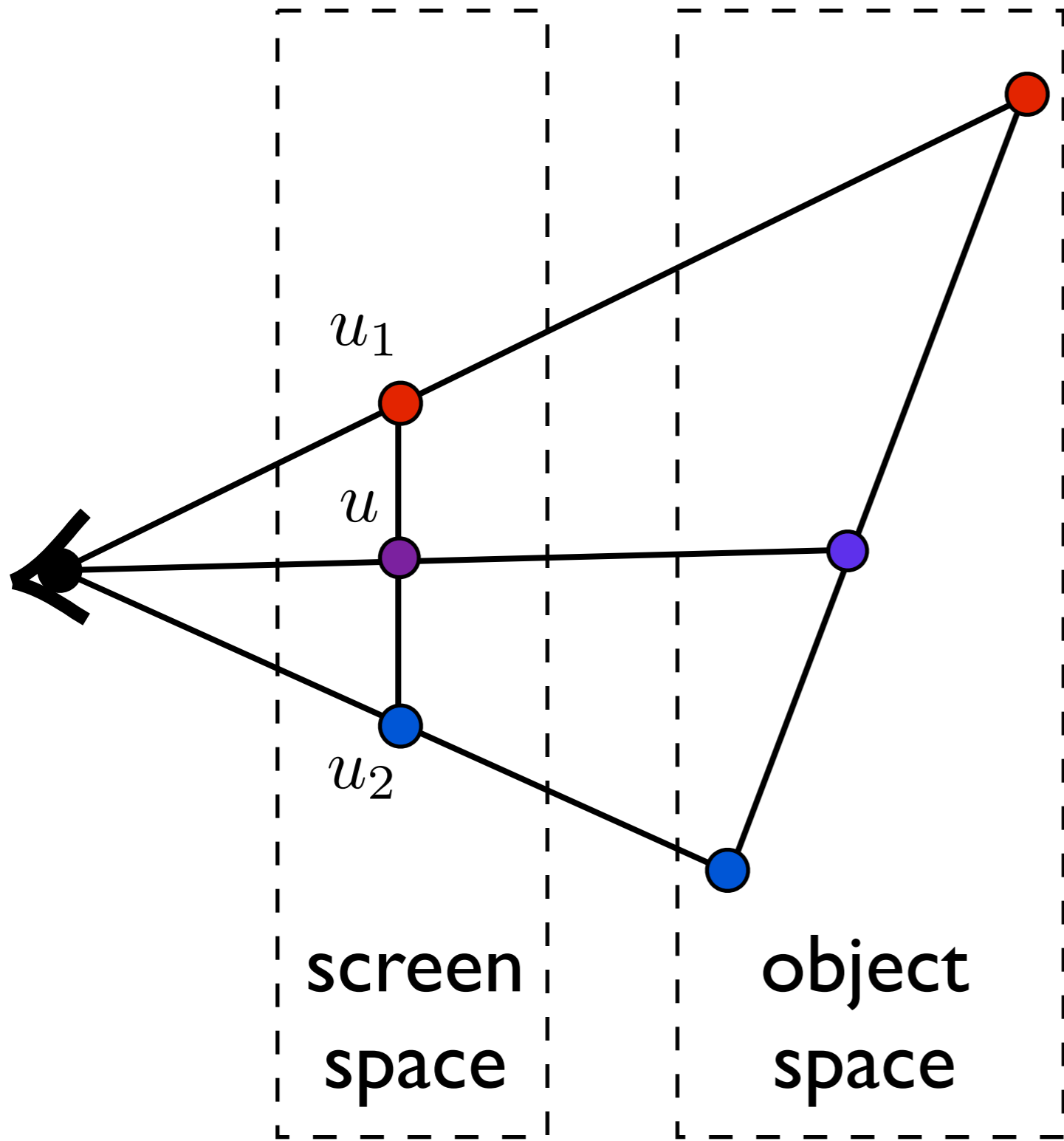
# Perspective correct interpolation

- In minigl pipeline, we find barycentric coordinates in 2D screen space
- but not the correct object space barycentric coords
- these coordinates are okay for z-buffer test

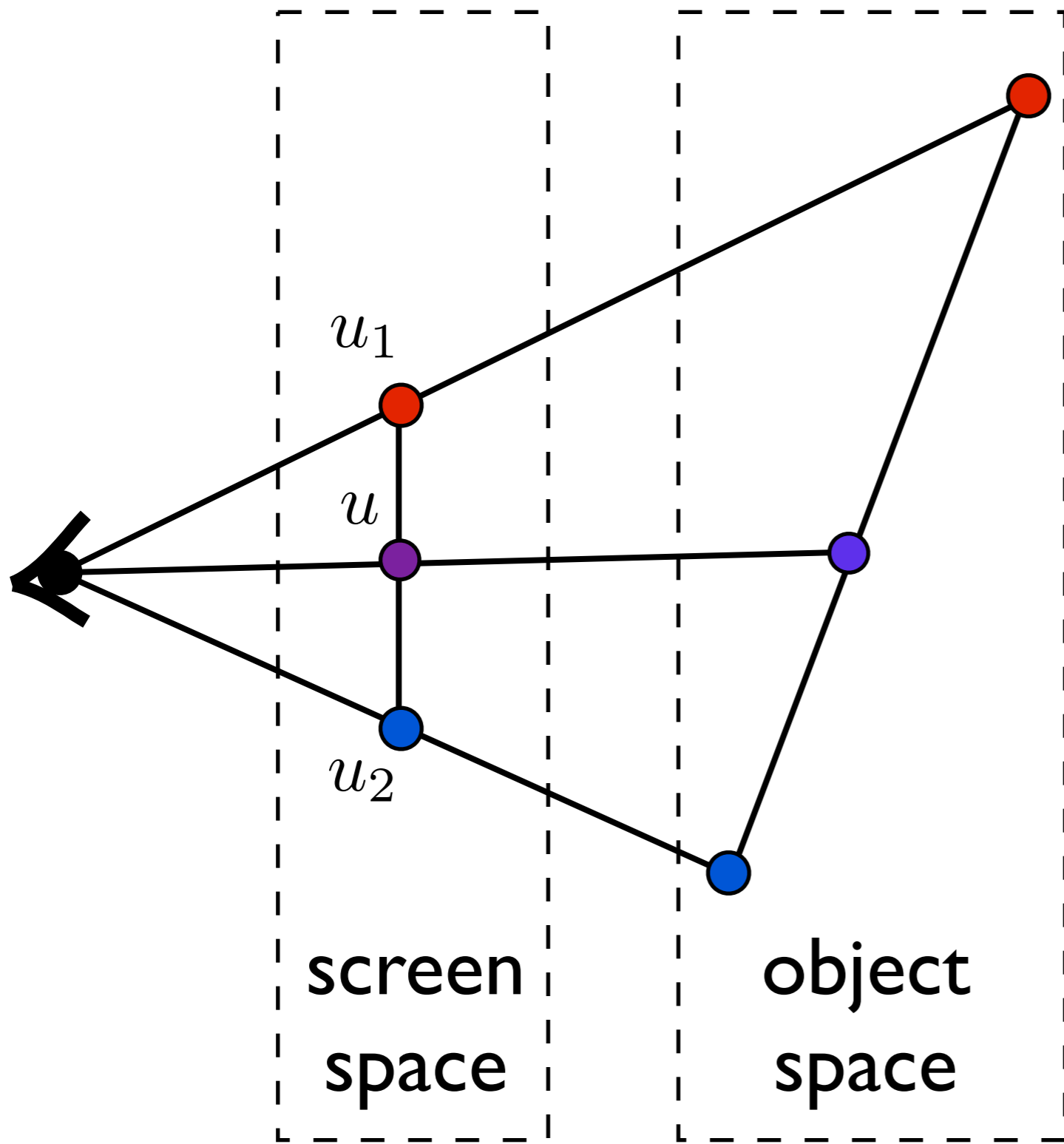




$$u = \frac{1}{2}u_1 + \frac{1}{2}u_2$$

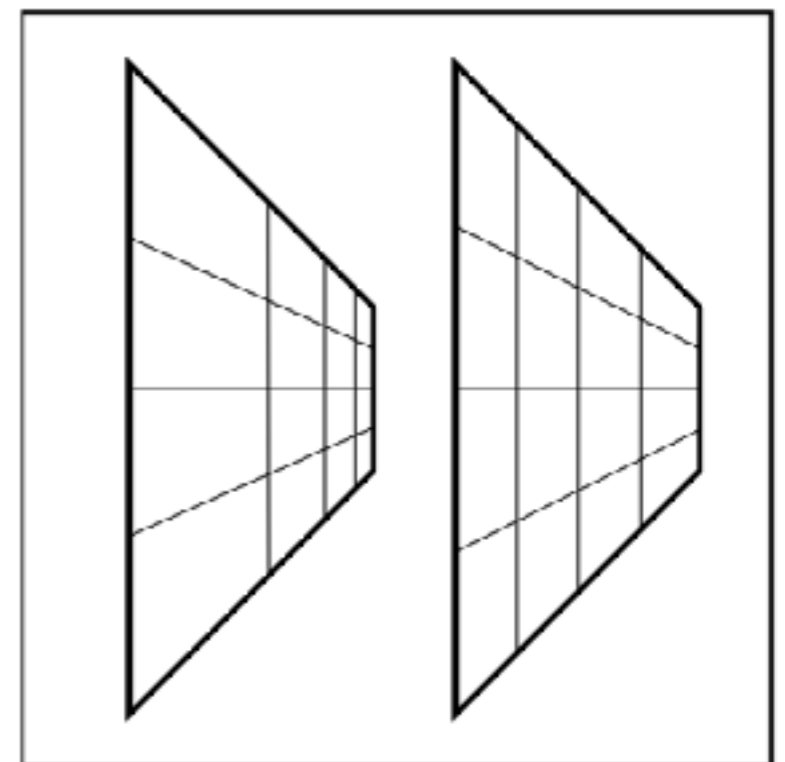


~~$$u = \frac{1}{2}u_1 + \frac{1}{2}u_2$$~~



Interpolation with screen space weights is incorrect

~~$$u = \frac{1}{2}u_1 + \frac{1}{2}u_2$$~~

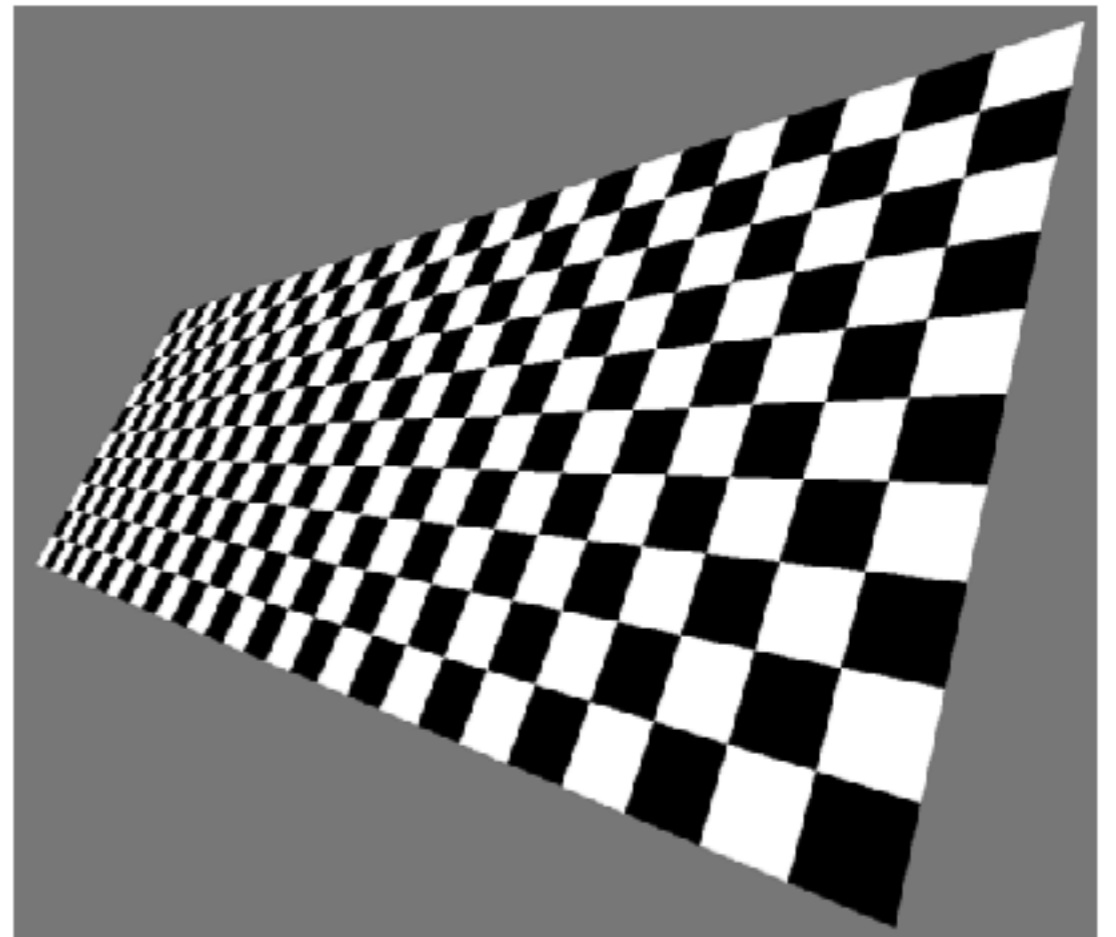
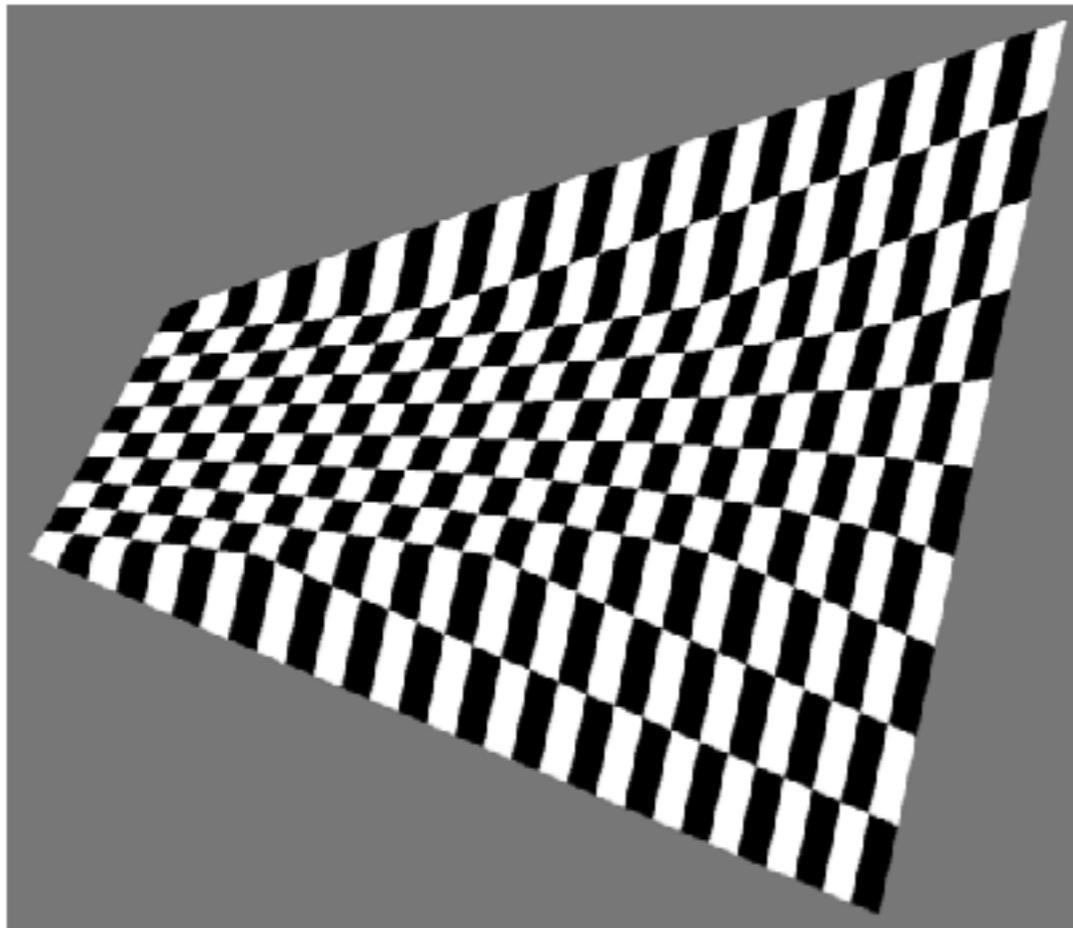


correct

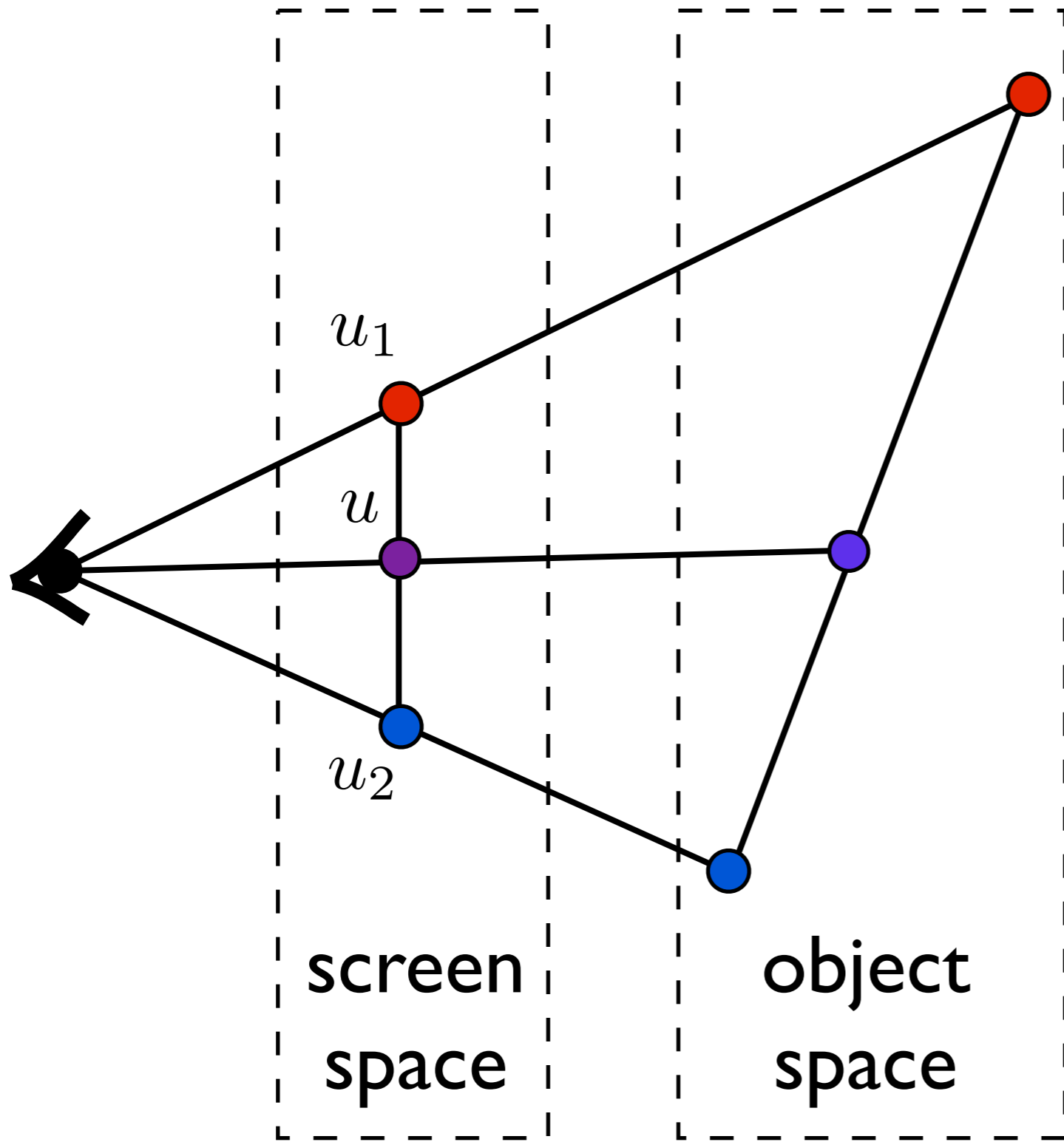
distorted

# Perspective correct interpolation

Using screen space weights looks wrong for textures



[Heckbert and Morton, 1990]

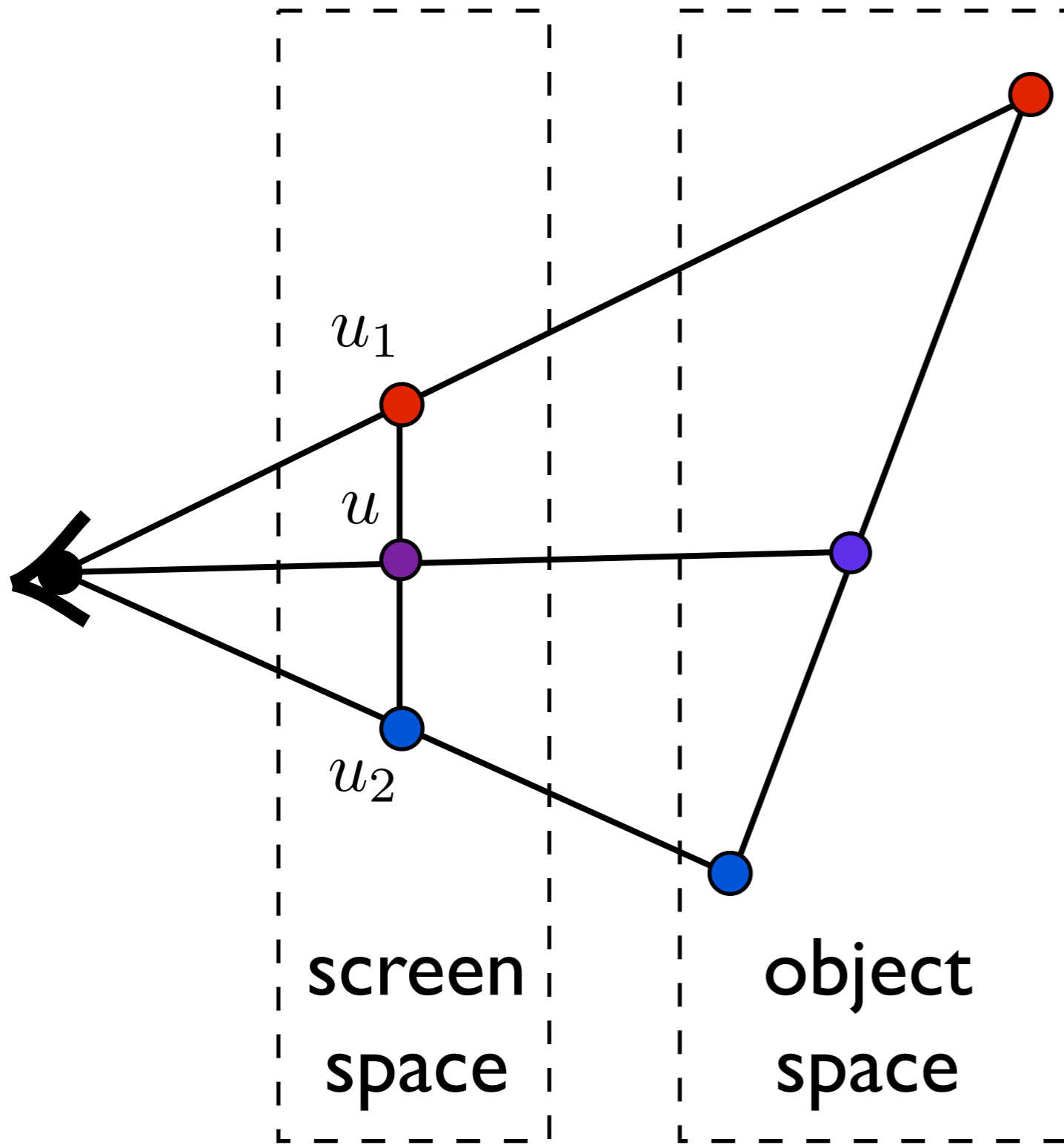


~~$$u = \frac{1}{2}u_1 + \frac{1}{2}u_2$$~~

Do we need to transform back to object space?

$$\mathbf{v}_{sc} = M_{vp}M_{pers}M_{cam}\mathbf{v}$$





~~$$u = \frac{1}{2}u_1 + \frac{1}{2}u_2$$~~

Do we need to transform back to object space?

**NO!**

<whiteboard>