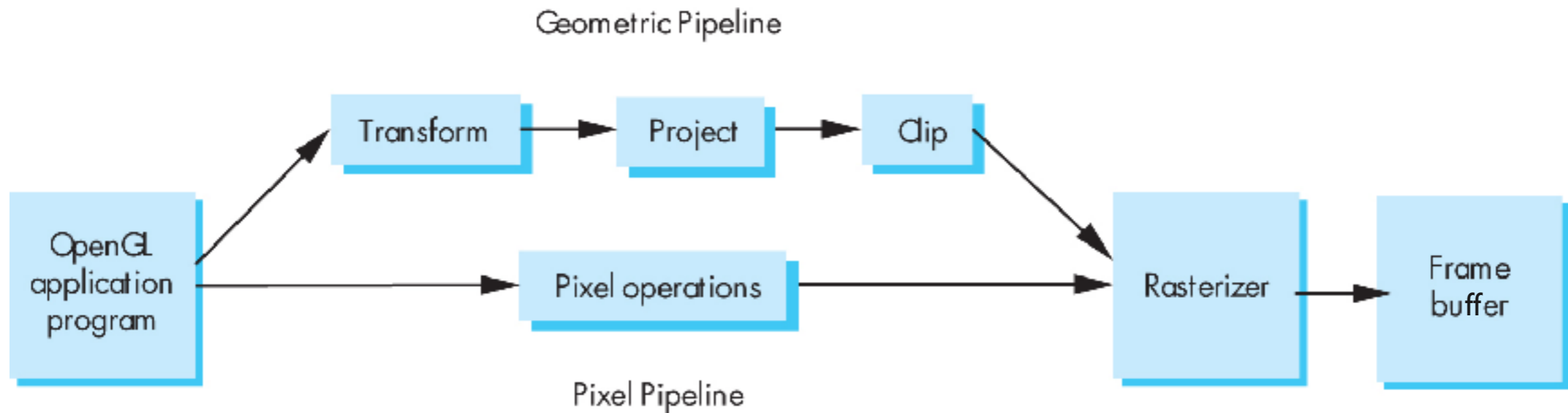
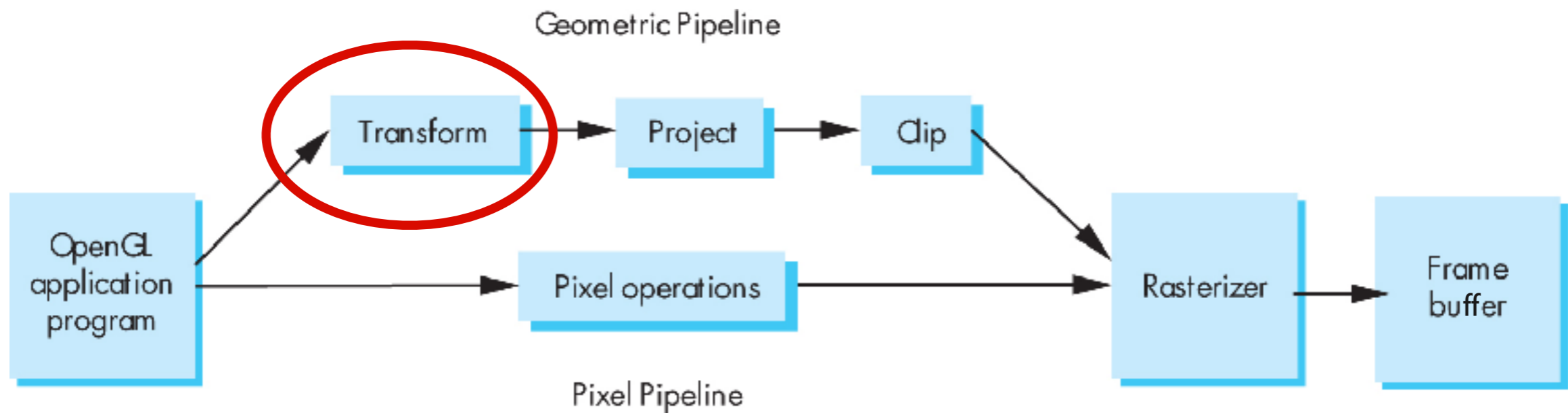


# Graphics Pipeline (cont.)

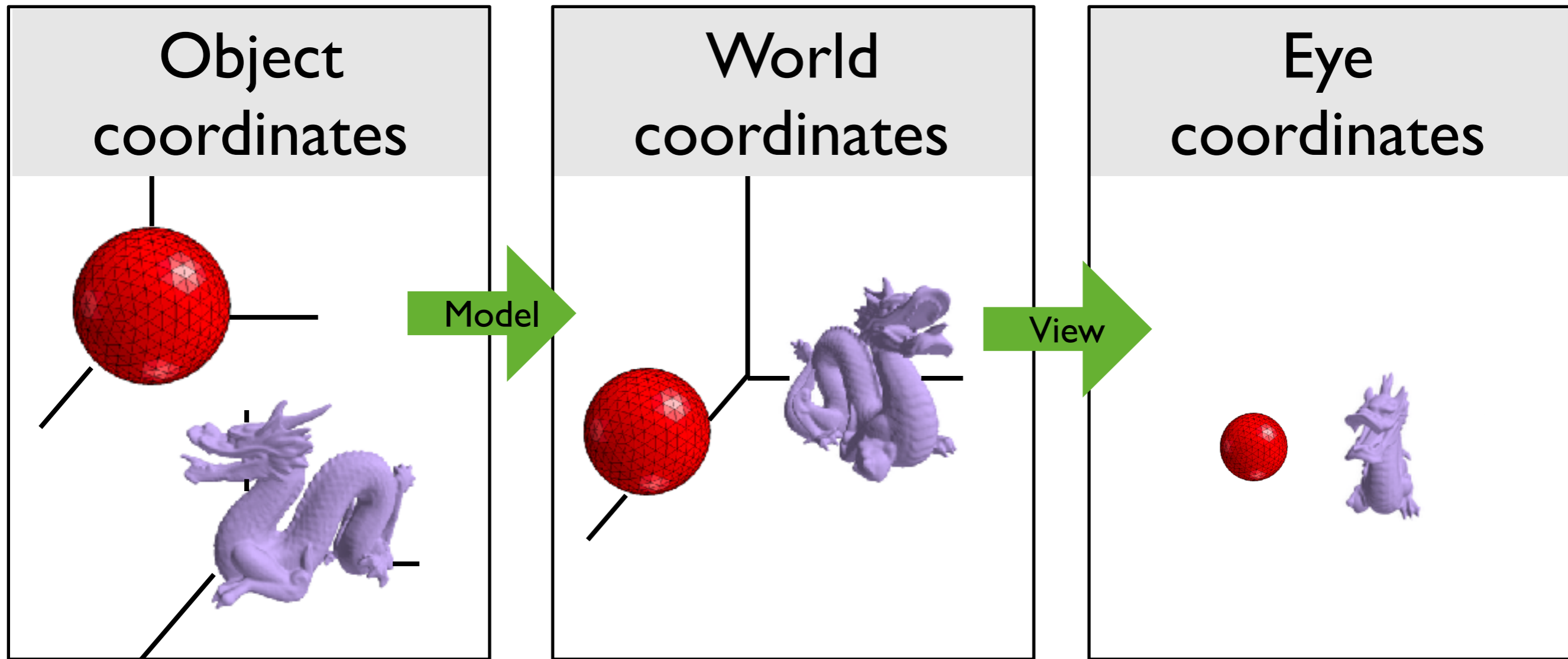
# Graphics Pipeline



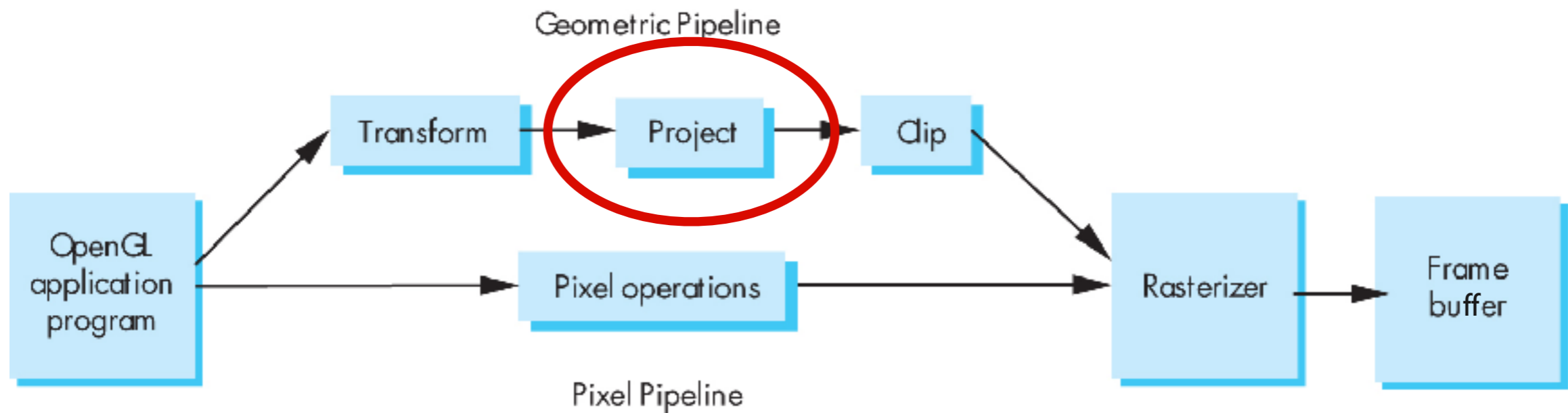
# Transform



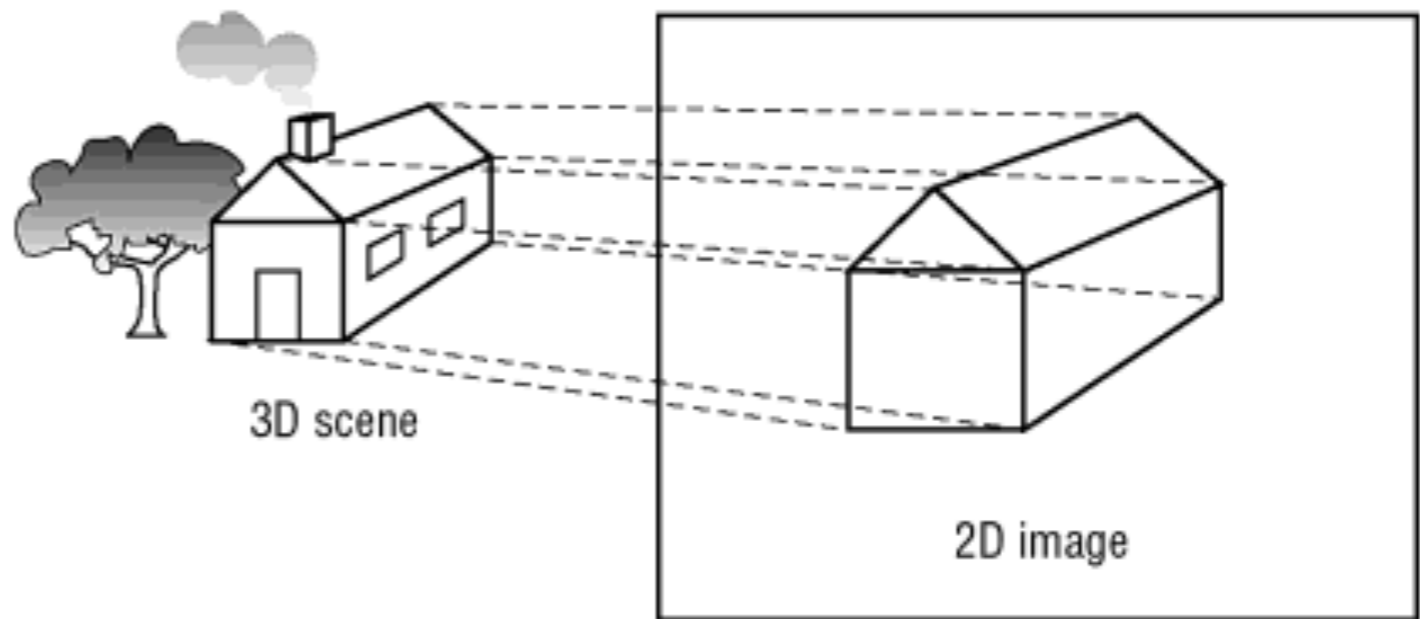
# “Modelview” Transformation



# Project

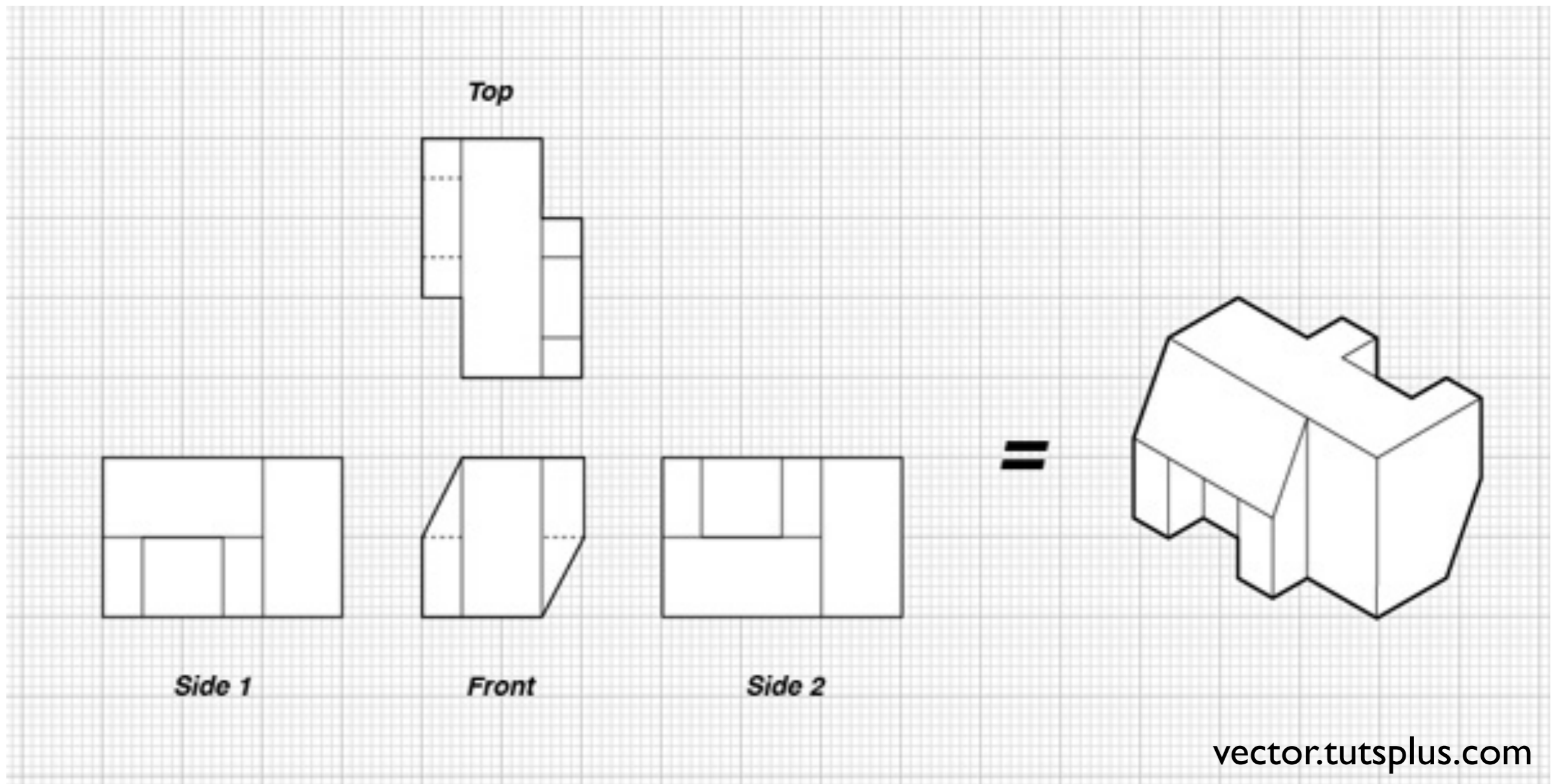


Projection: map  
3D scene to  
2D image



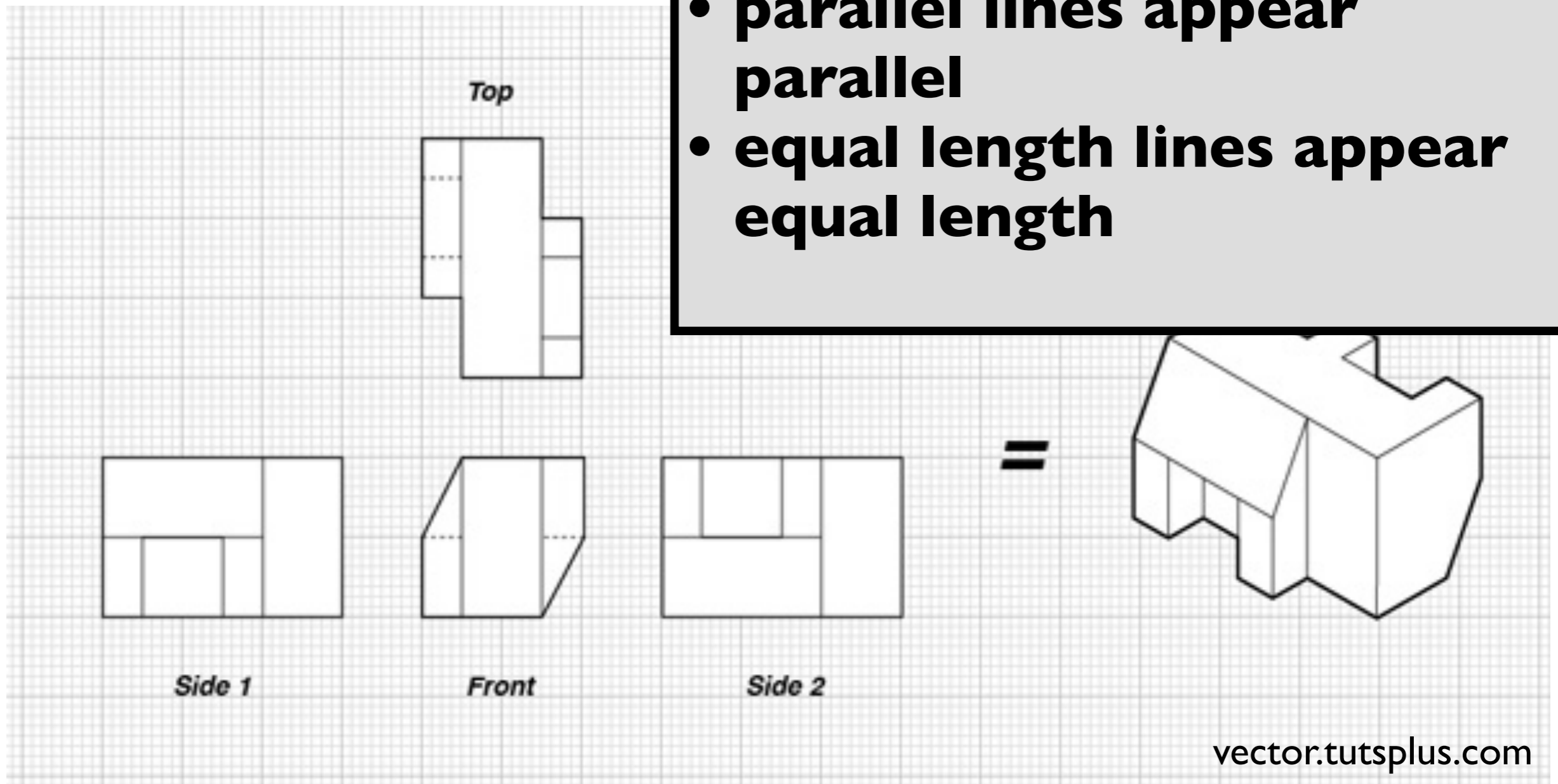
OpenGL Super Bible, 5th Ed.

# Orthographic projection



# Orthographic projection

- **parallel lines appear parallel**
- **equal length lines appear equal length**

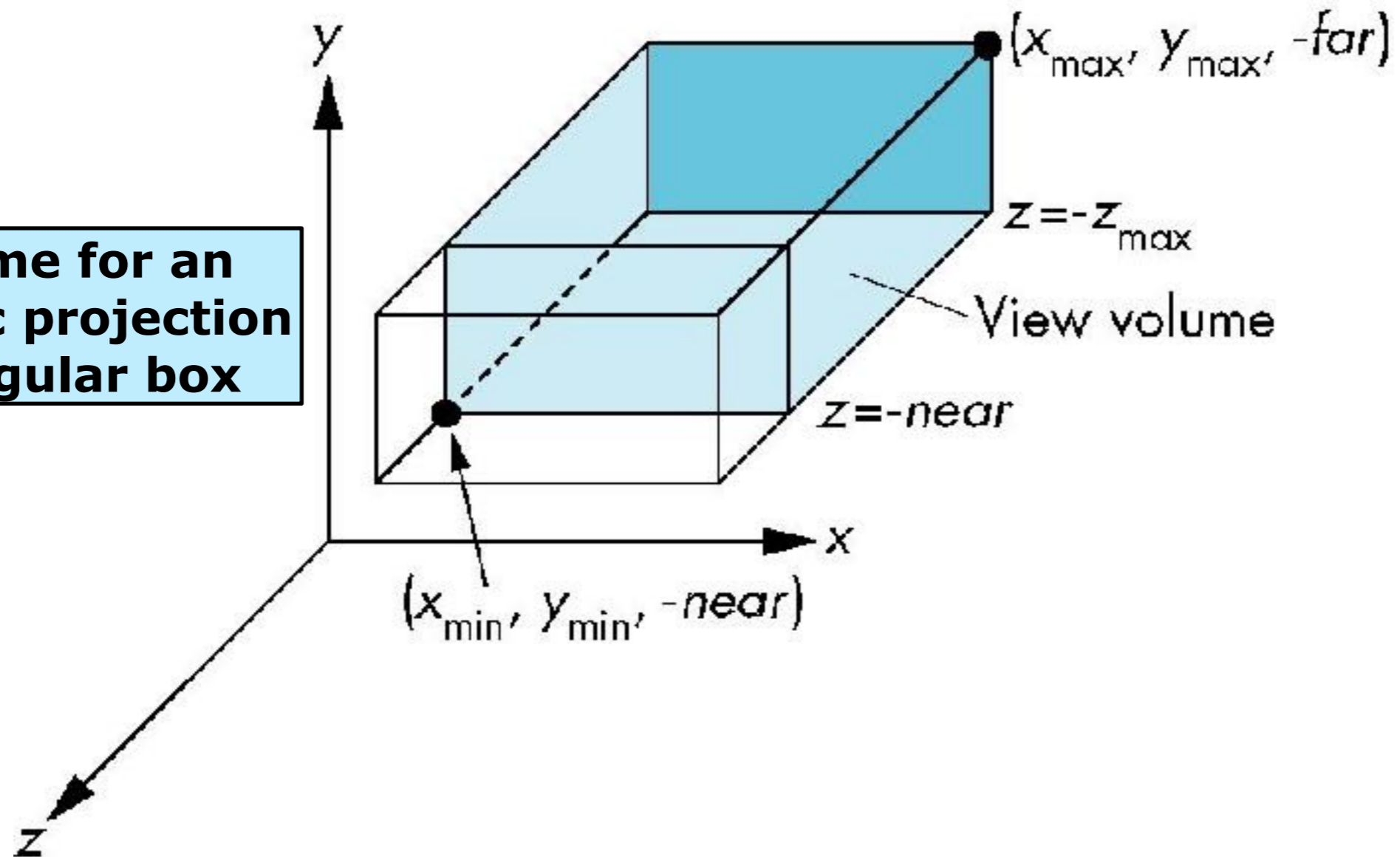




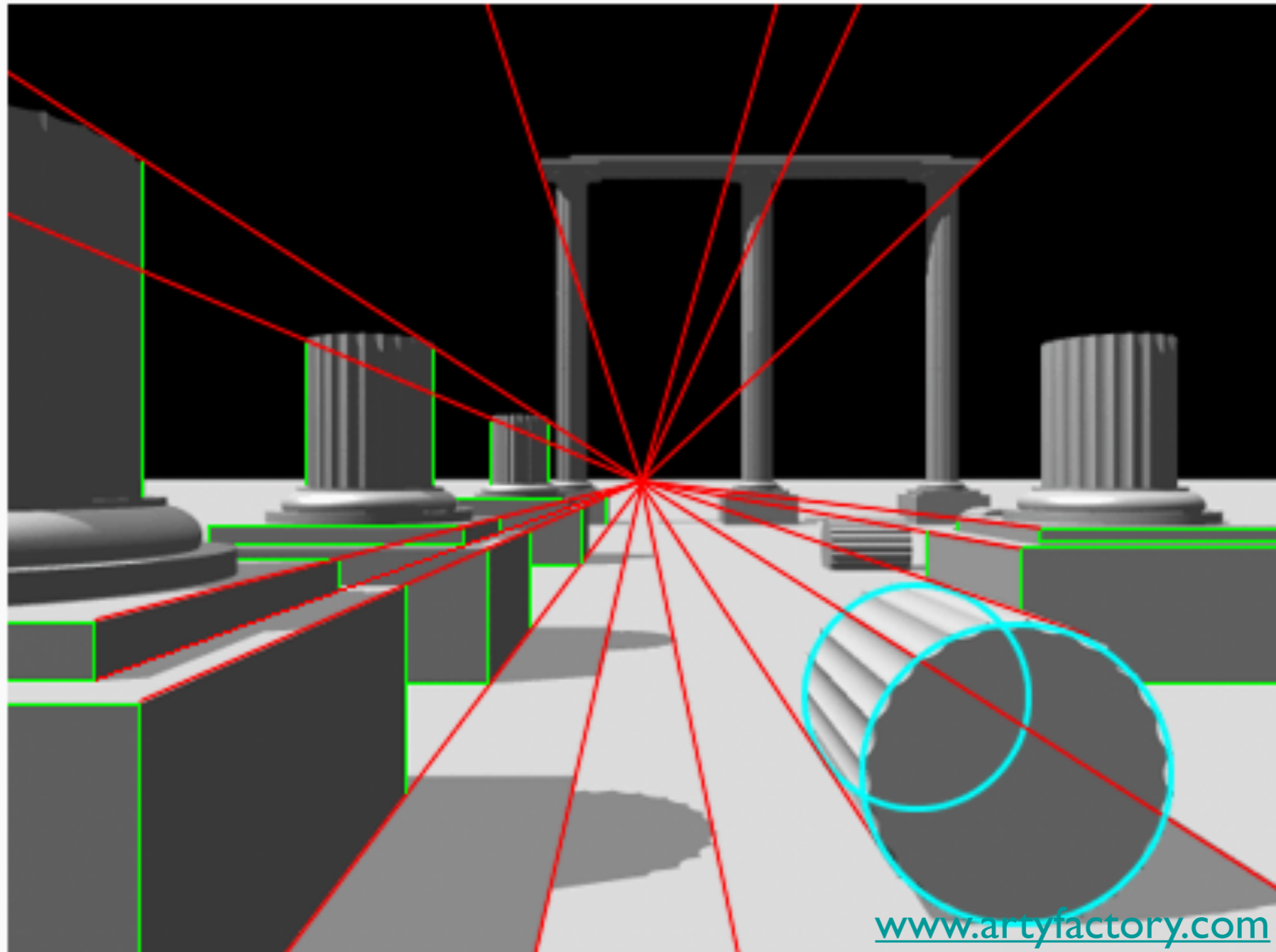
# OpenGL Orthogonal Viewing

`glOrtho(left, right, bottom, top, near, far)`

View volume for an orthographic projection is a rectangular box



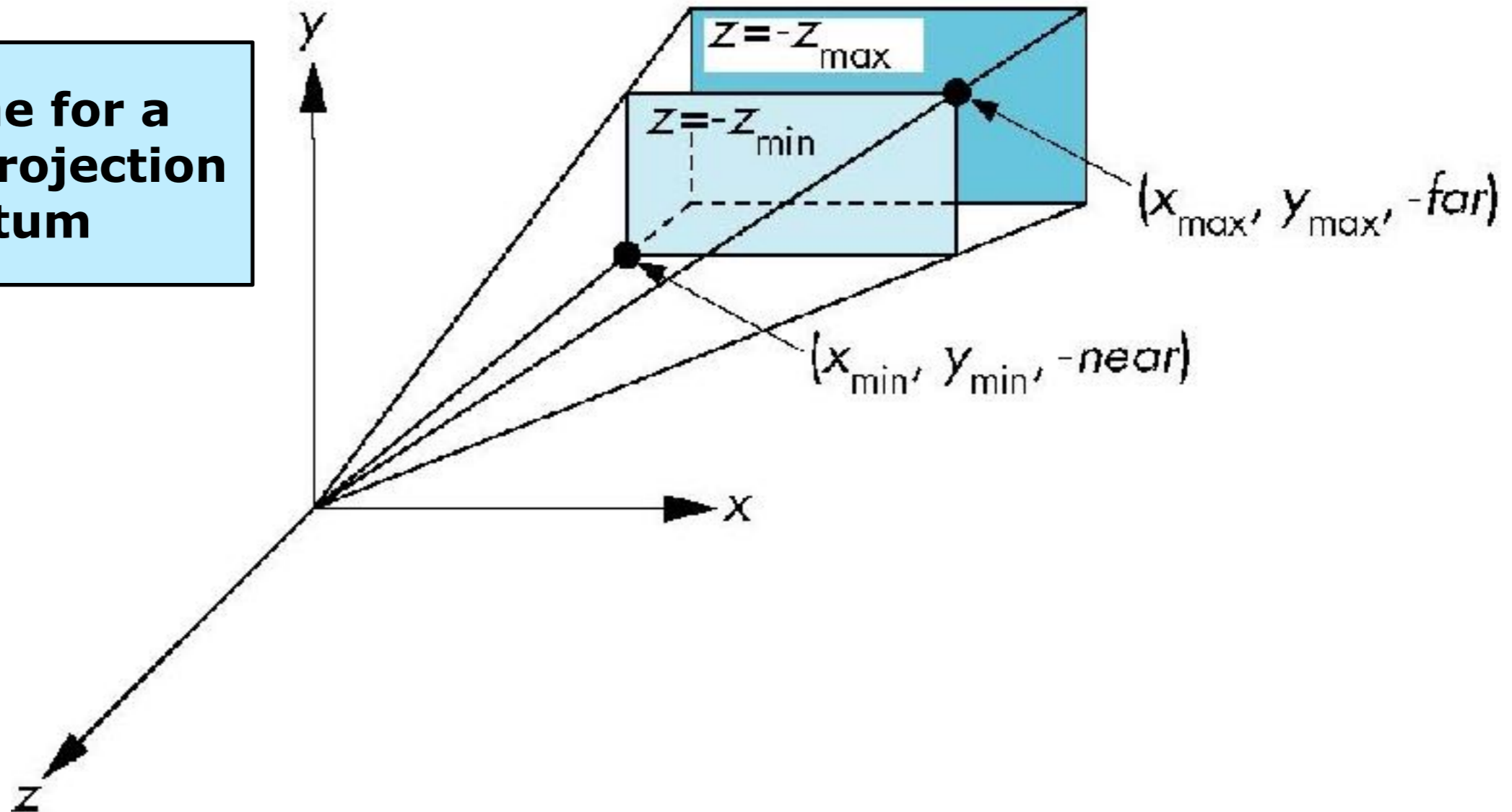
# Perspective projection



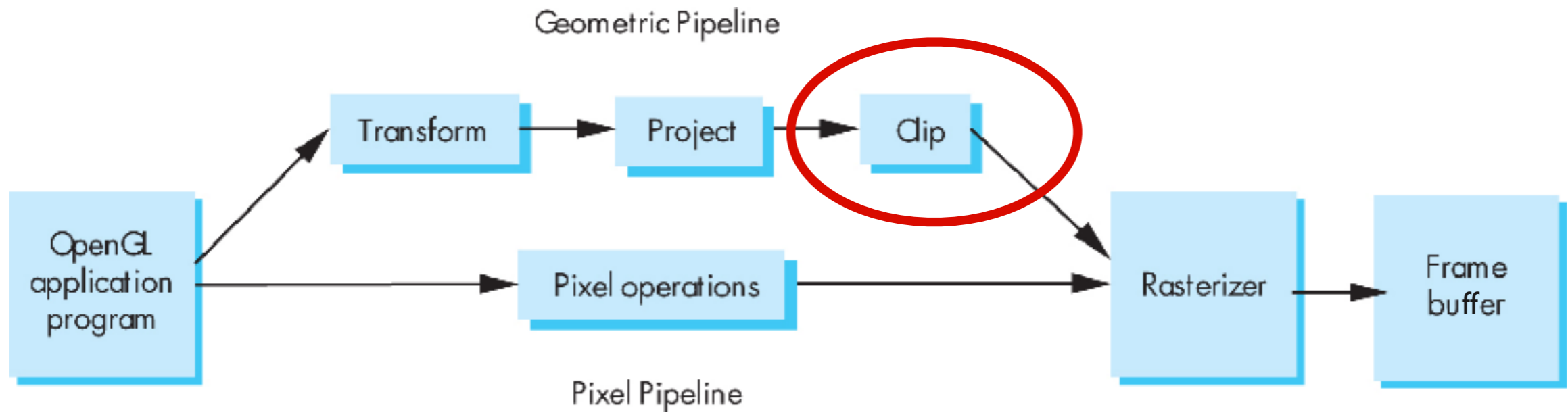
# OpenGL Perspective Viewing

`glFrustum(xmin, xmax, ymin, ymax, near, far)`

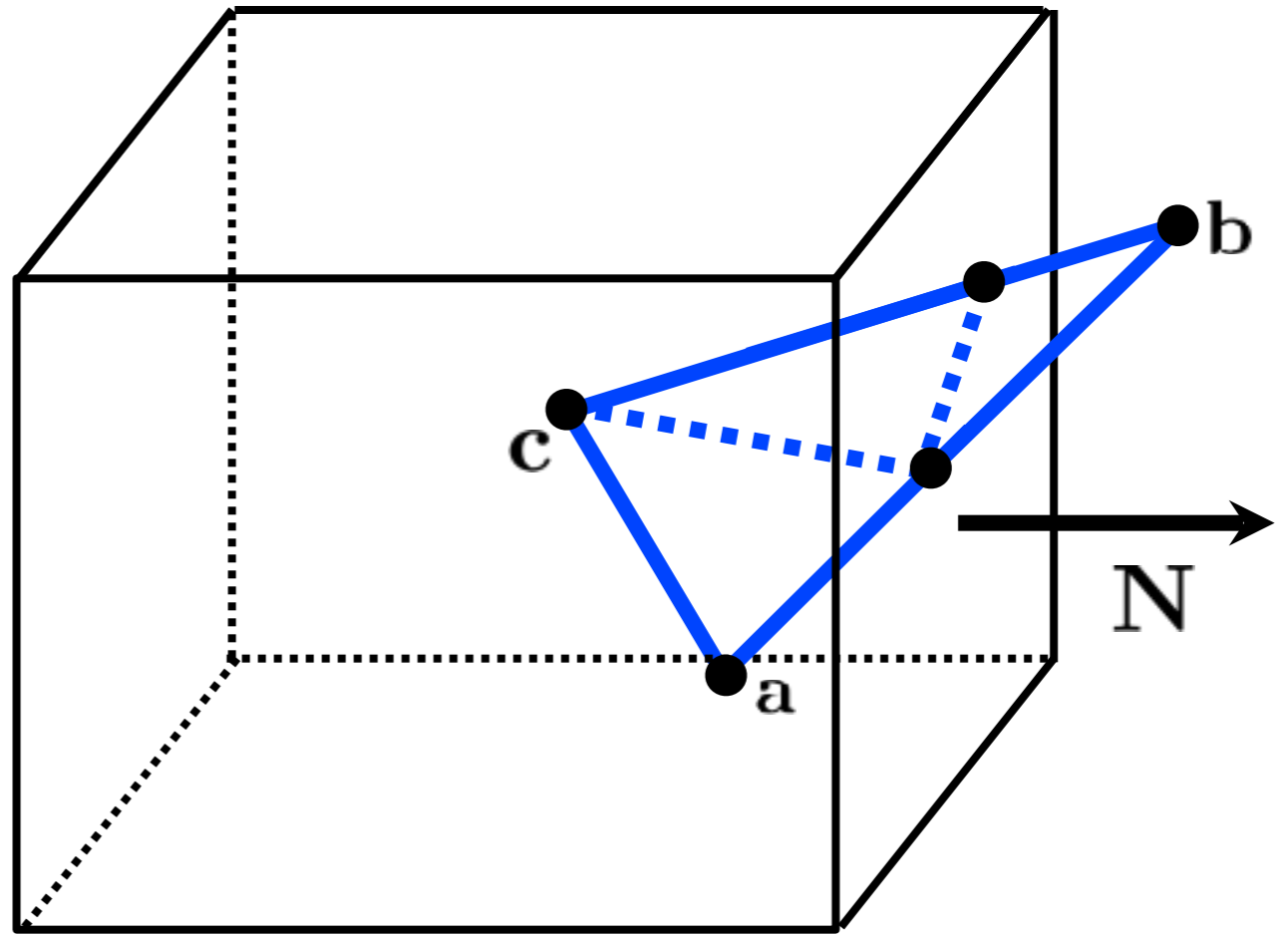
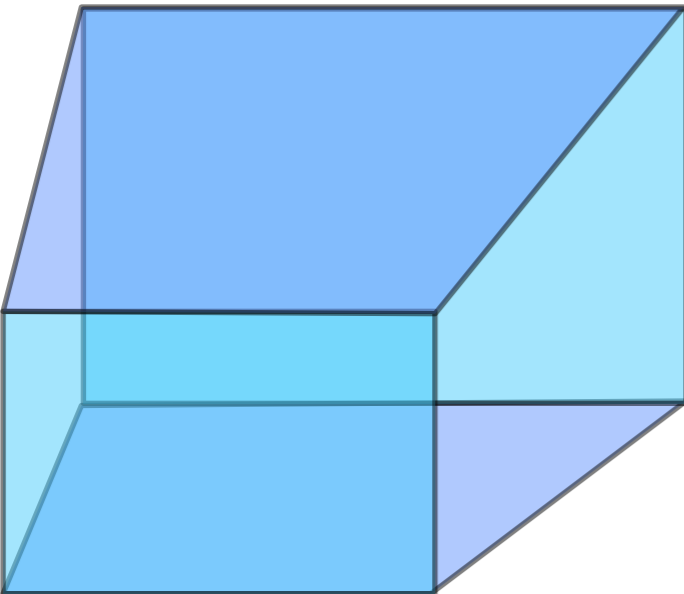
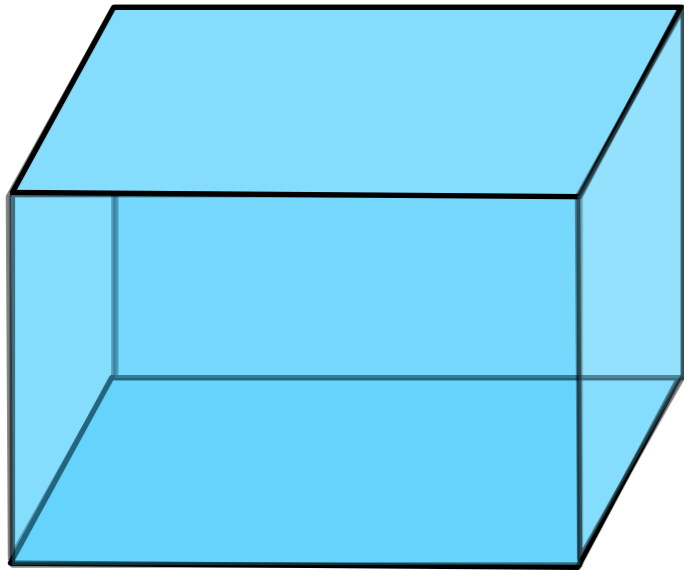
View volume for a perspective projection is a frustum



# Clip

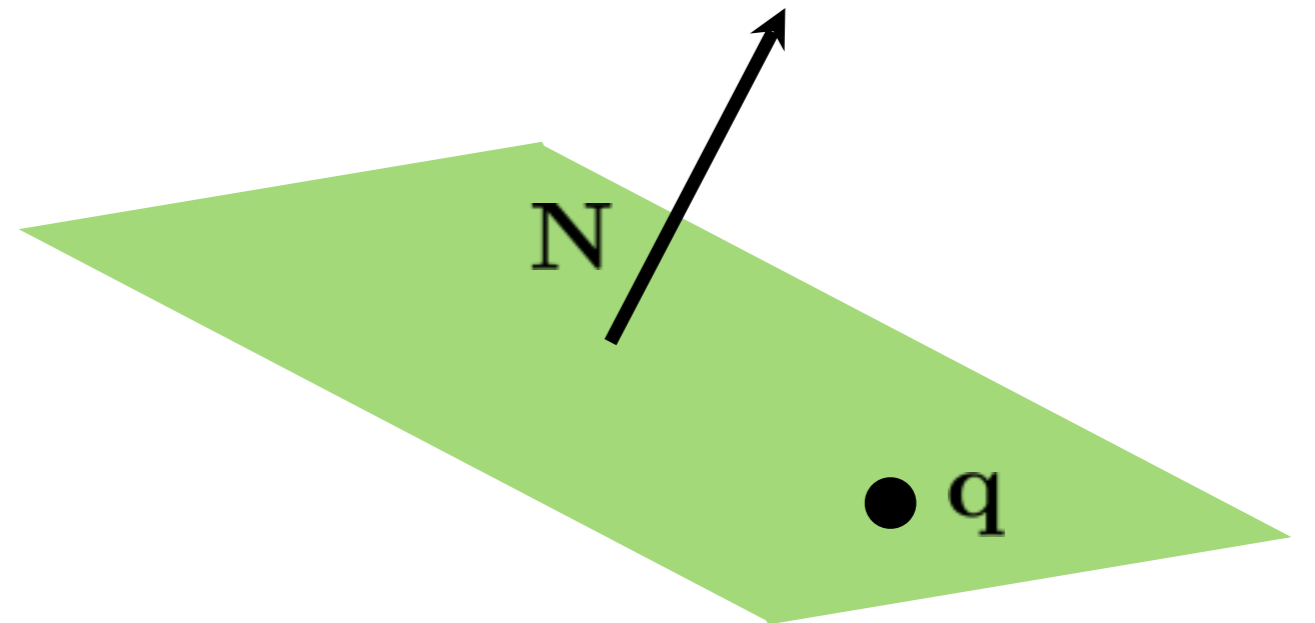


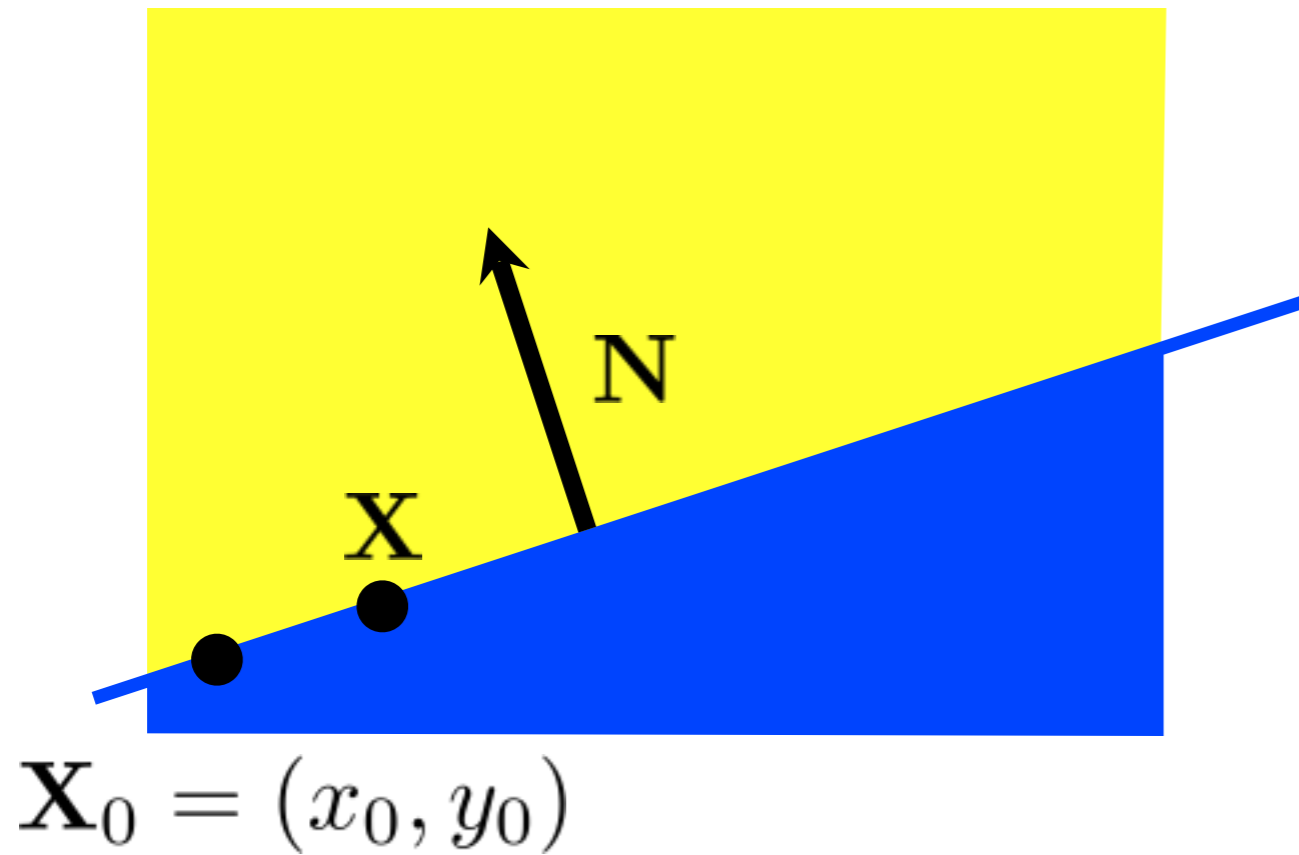
# Clip against view volume



# Clipping against a plane

What's the equation for  
the plane through  $\mathbf{q}$   
with normal  $\mathbf{N}$ ?





implicit line equation:

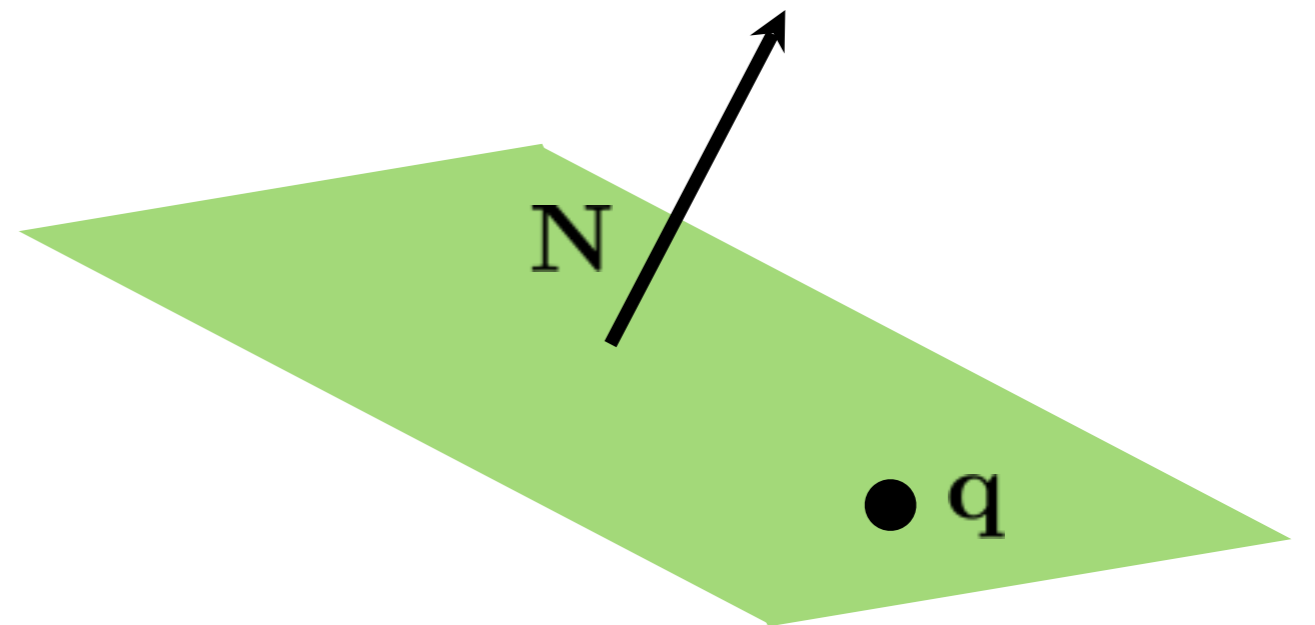
$$f(\mathbf{X}) = \mathbf{N} \cdot (\mathbf{X} - \mathbf{X}_0) = 0$$

# Clipping against a plane

What's the equation for  
the plane through  $\mathbf{q}$   
with normal  $\mathbf{N}$ ?

$$f(\mathbf{p}) = ? = 0$$

<whiteboard>

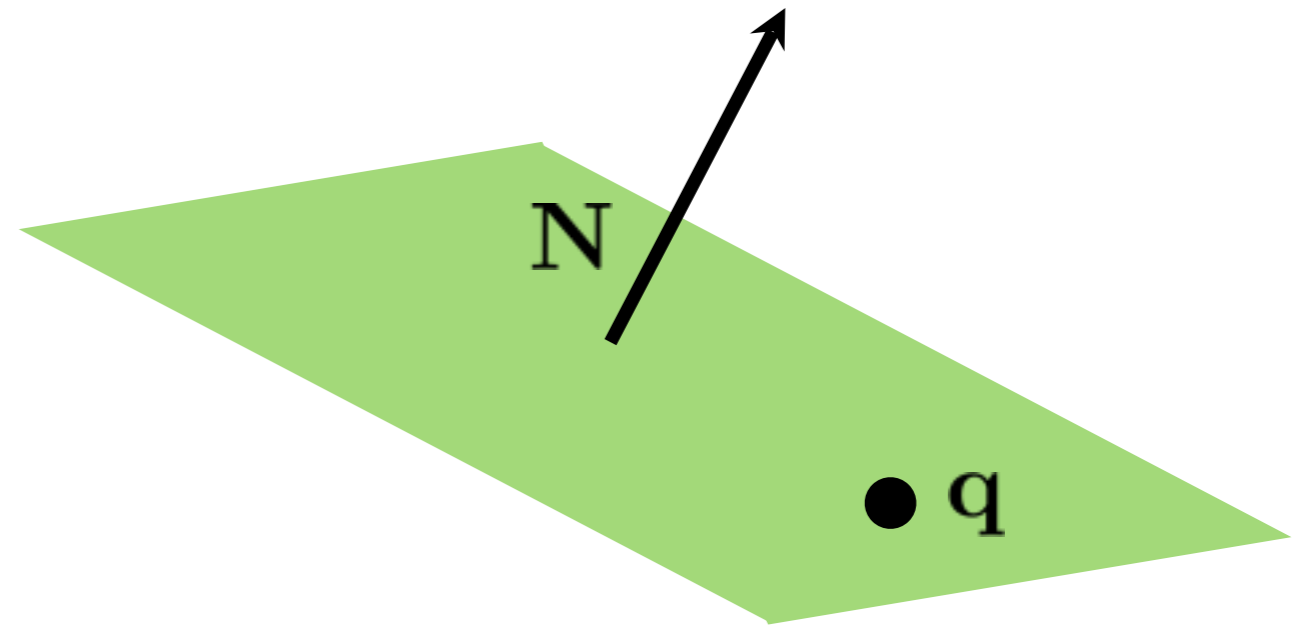




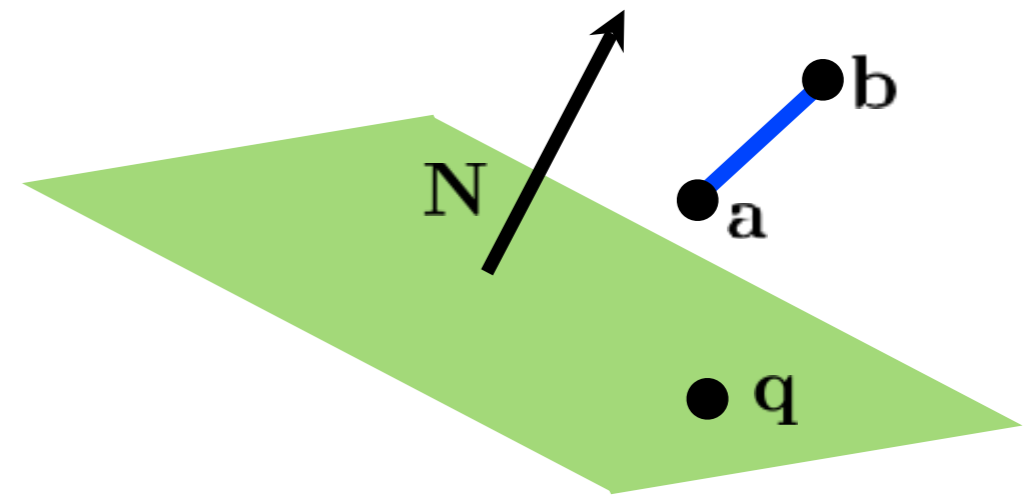
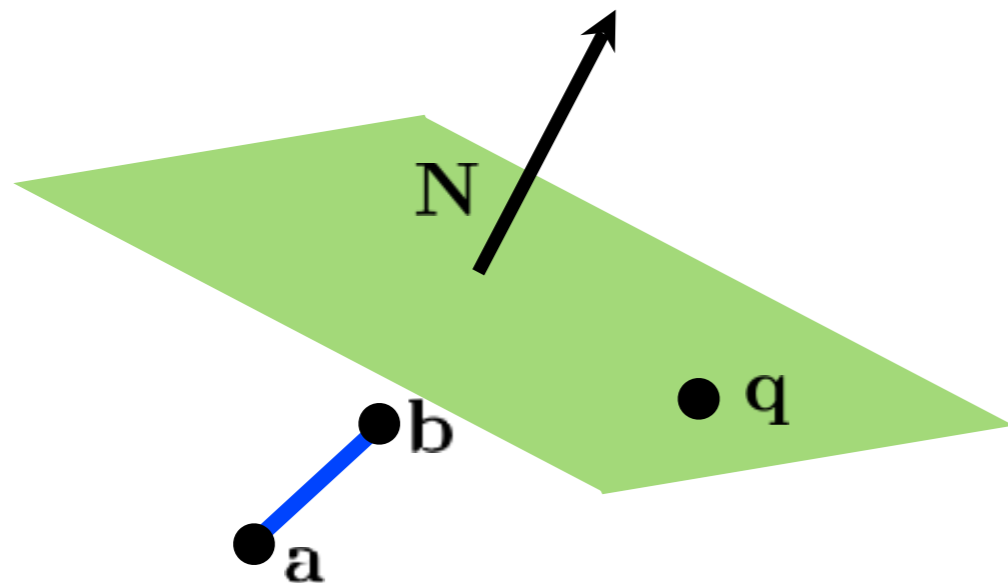
# Clipping against a plane

What's the equation for  
the plane through  $\mathbf{q}$   
with normal  $\mathbf{N}$ ?

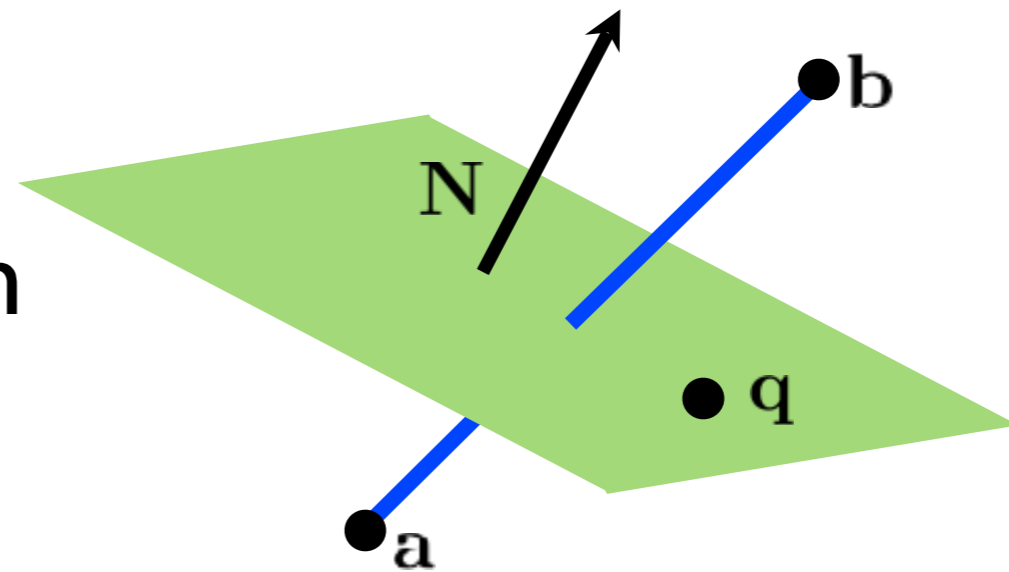
$$f(\mathbf{p}) = \mathbf{N} \cdot (\mathbf{p} - \mathbf{q}) = 0$$



# Intersection of line and plane

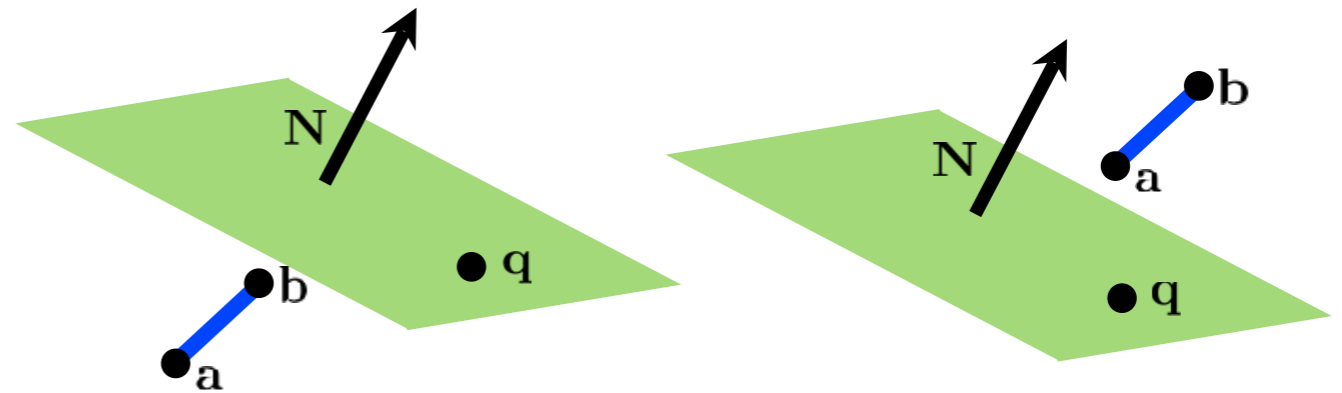


How can we distinguish between these cases?

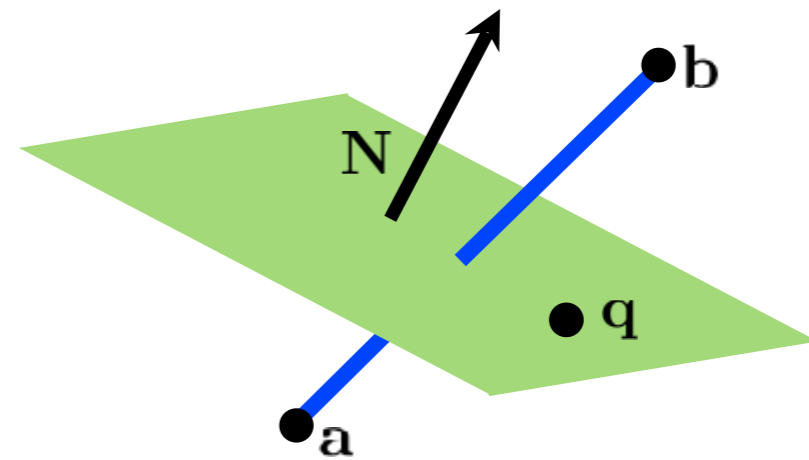


# Intersection of line and plane

$$f(\mathbf{a})f(\mathbf{b}) \geq 0$$

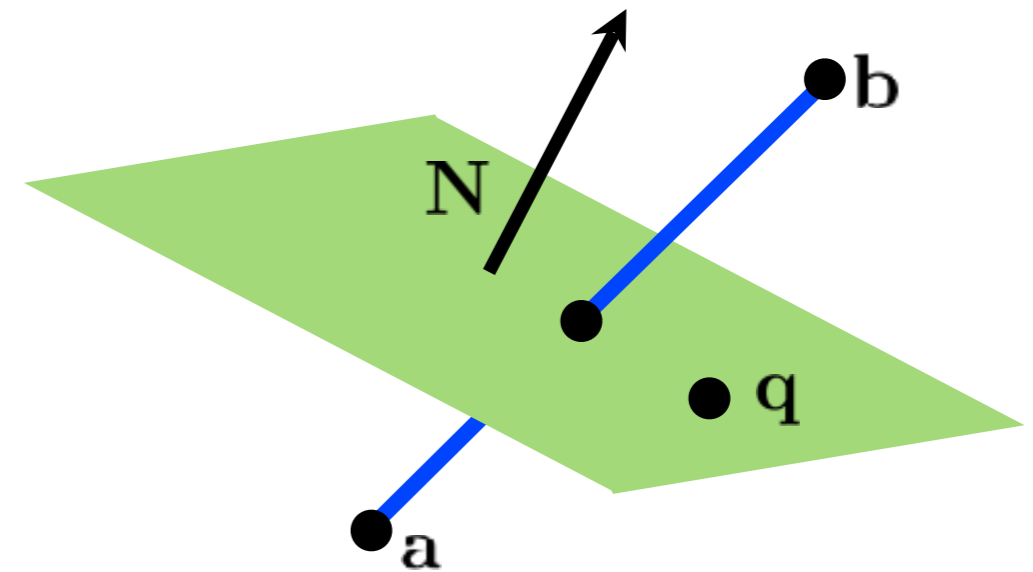


$$f(\mathbf{a})f(\mathbf{b}) < 0$$



# Intersection of line and plane

How can we find the intersection point?



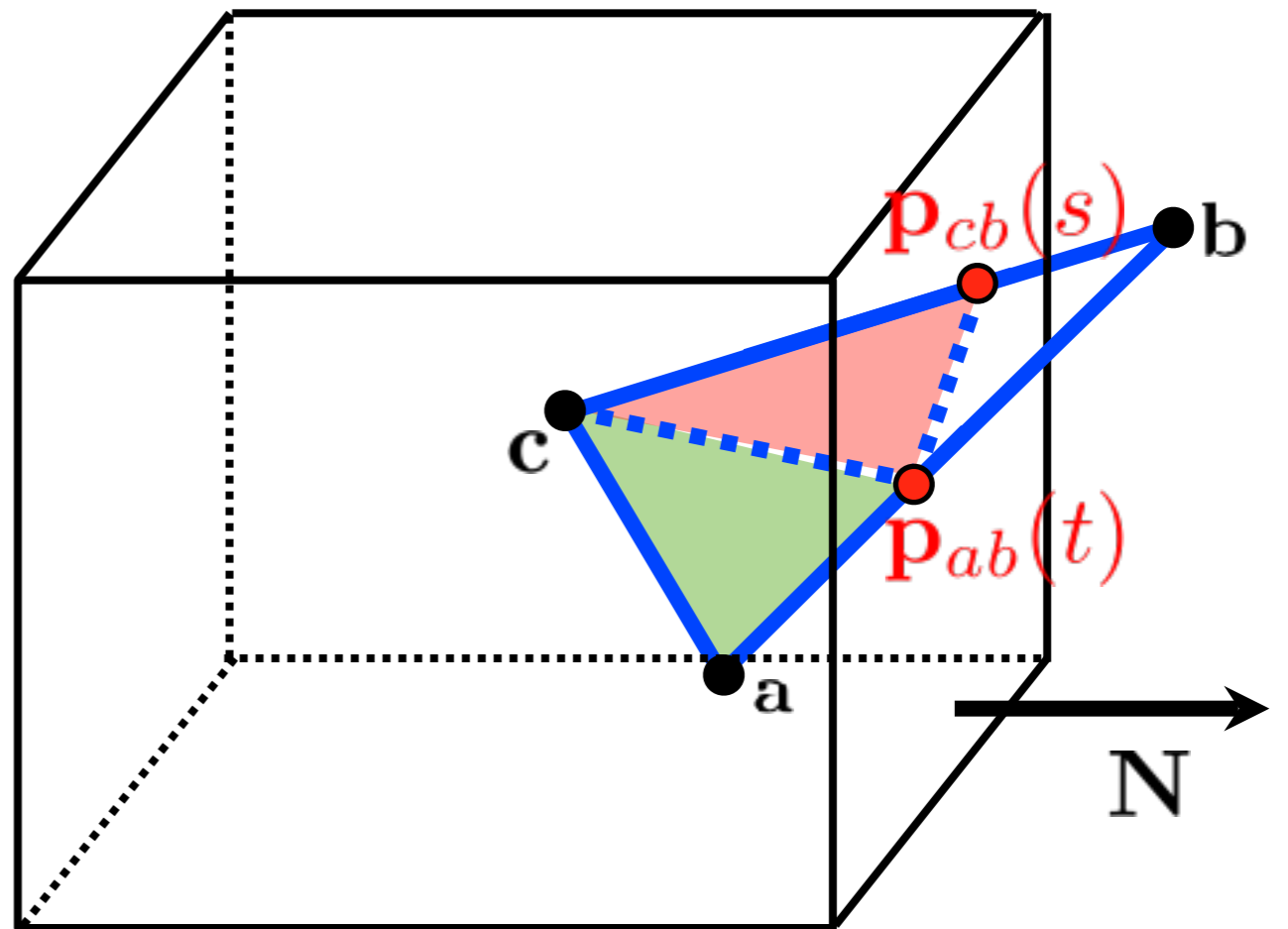
<whiteboard>

# Clip against view volume

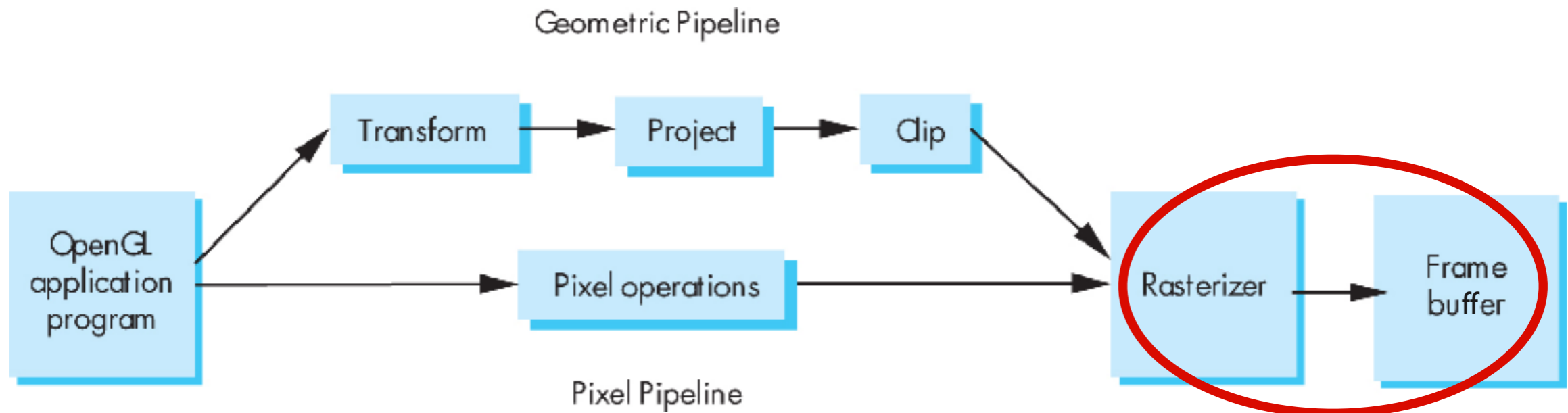
$$s = \frac{\mathbf{N} \cdot (\mathbf{q} - \mathbf{c})}{\mathbf{N} \cdot (\mathbf{b} - \mathbf{c})}$$

$$t = \frac{\mathbf{N} \cdot (\mathbf{q} - \mathbf{a})}{\mathbf{N} \cdot (\mathbf{b} - \mathbf{a})}$$

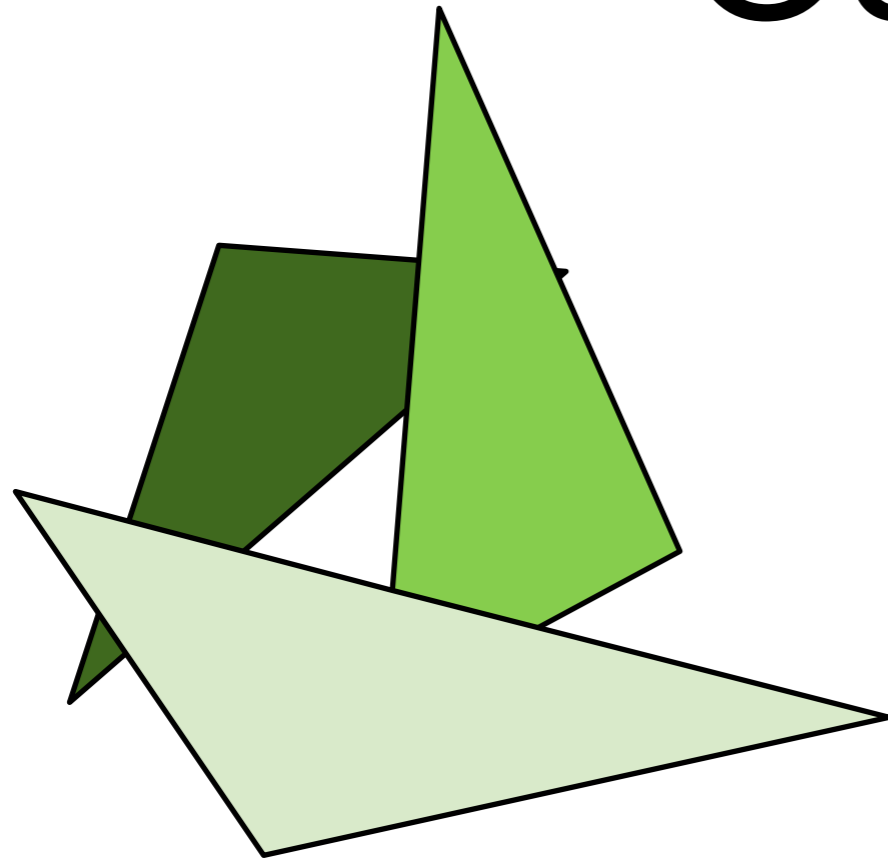
need to generate new  
triangles



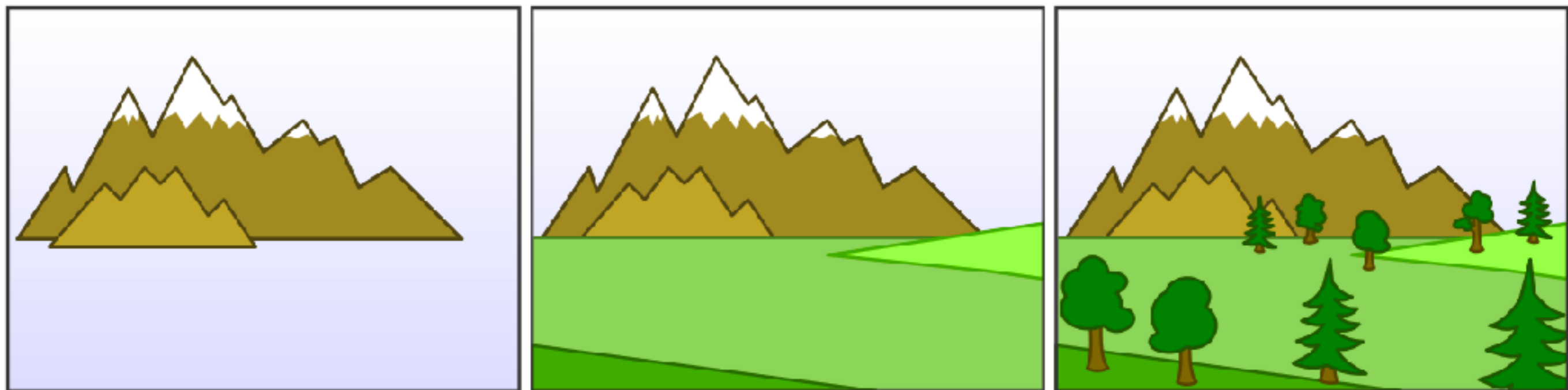
# Hidden Surface Removal



# Occlusion

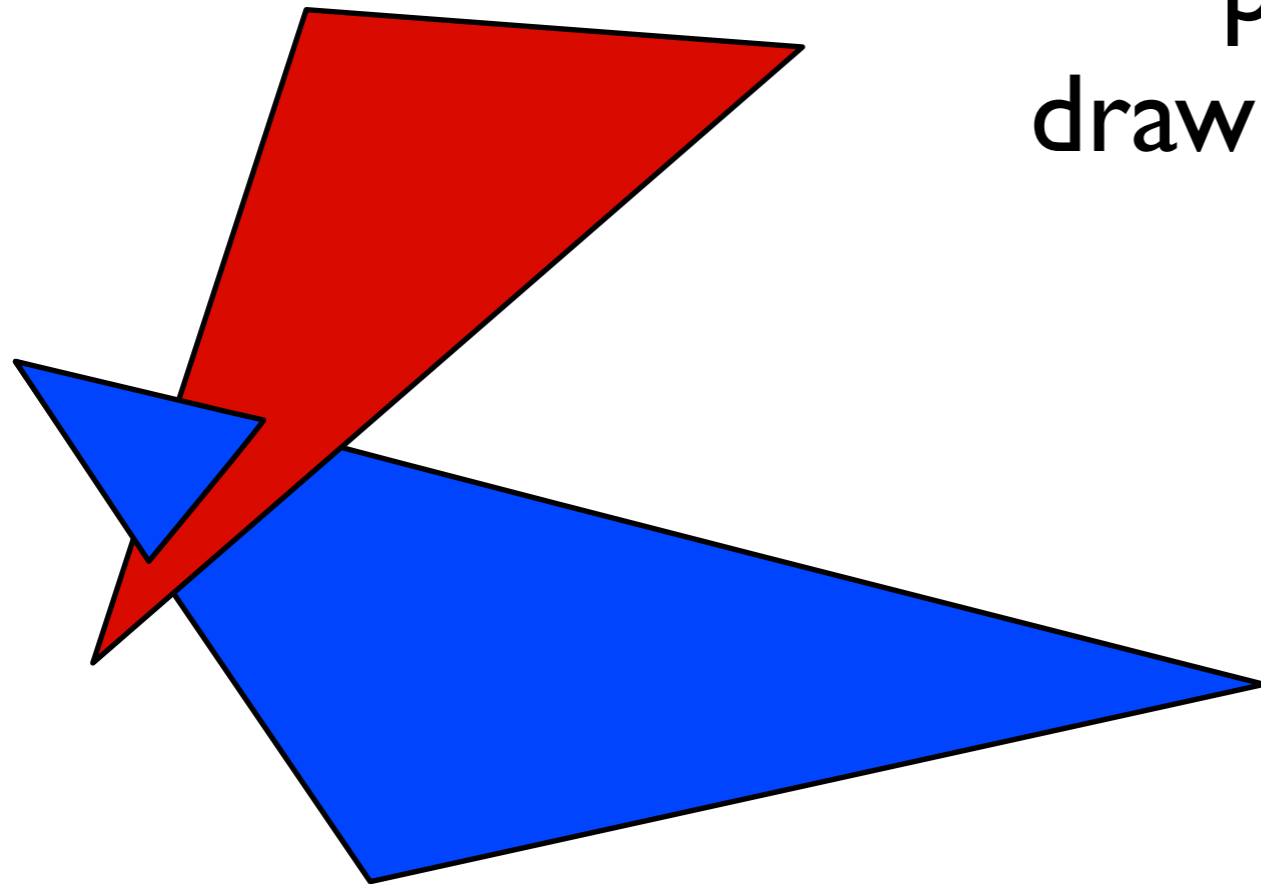


“painter’s algorithm”  
draw primitives in  
back-to-front order



# Occlusion

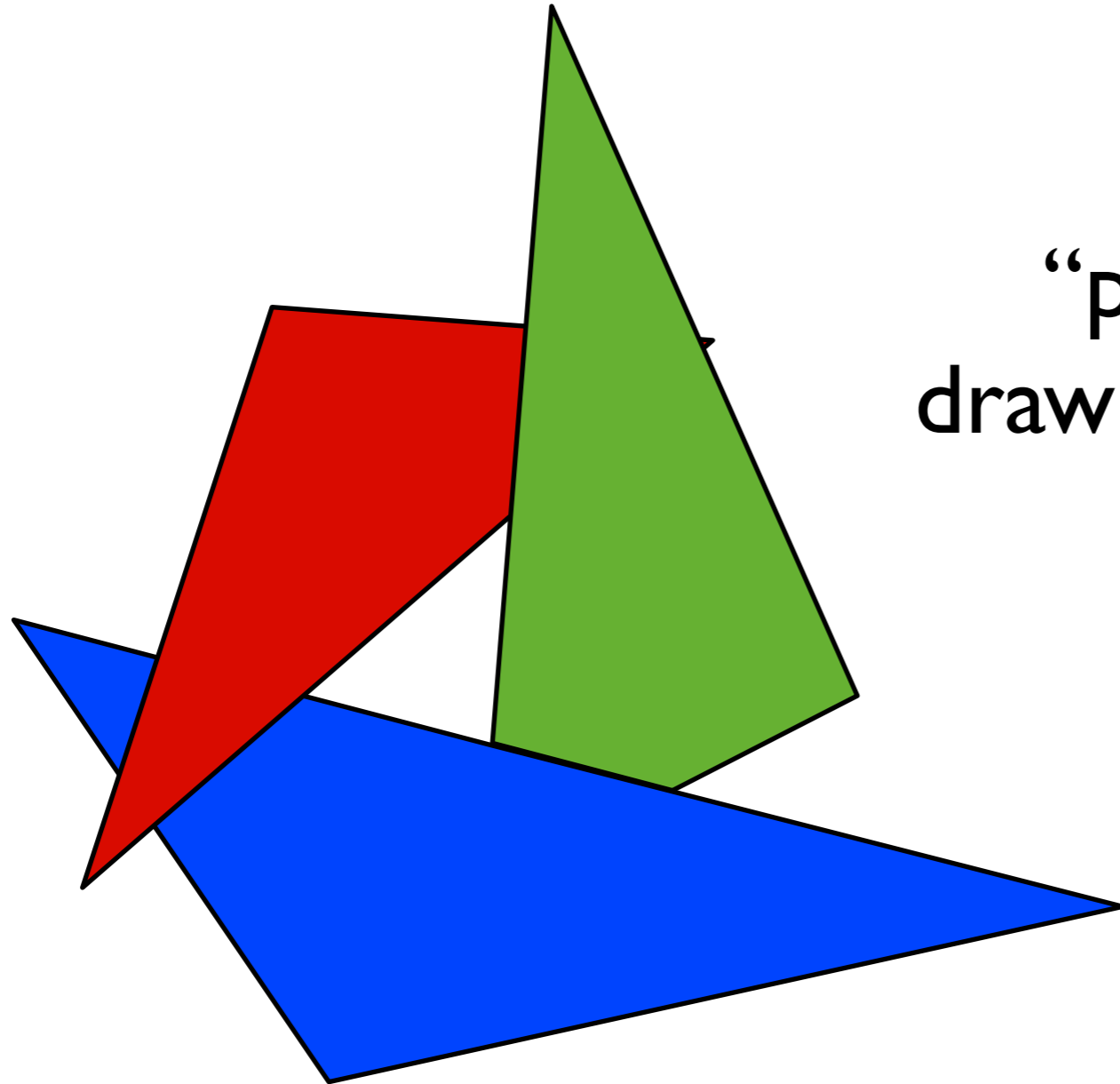
“painter’s algorithm”  
draw primitives in back-to-  
front order



**problem:**  
triangle  
intersection



# Occlusion



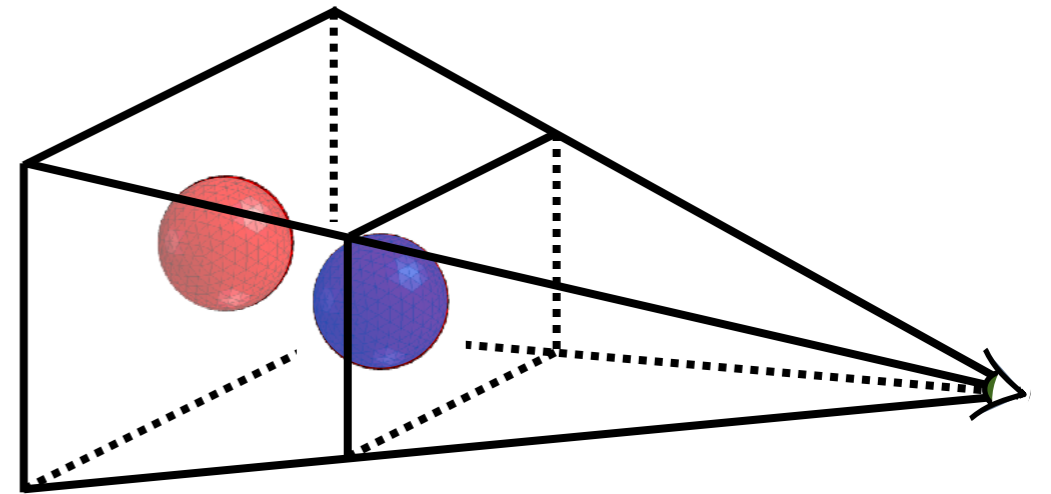
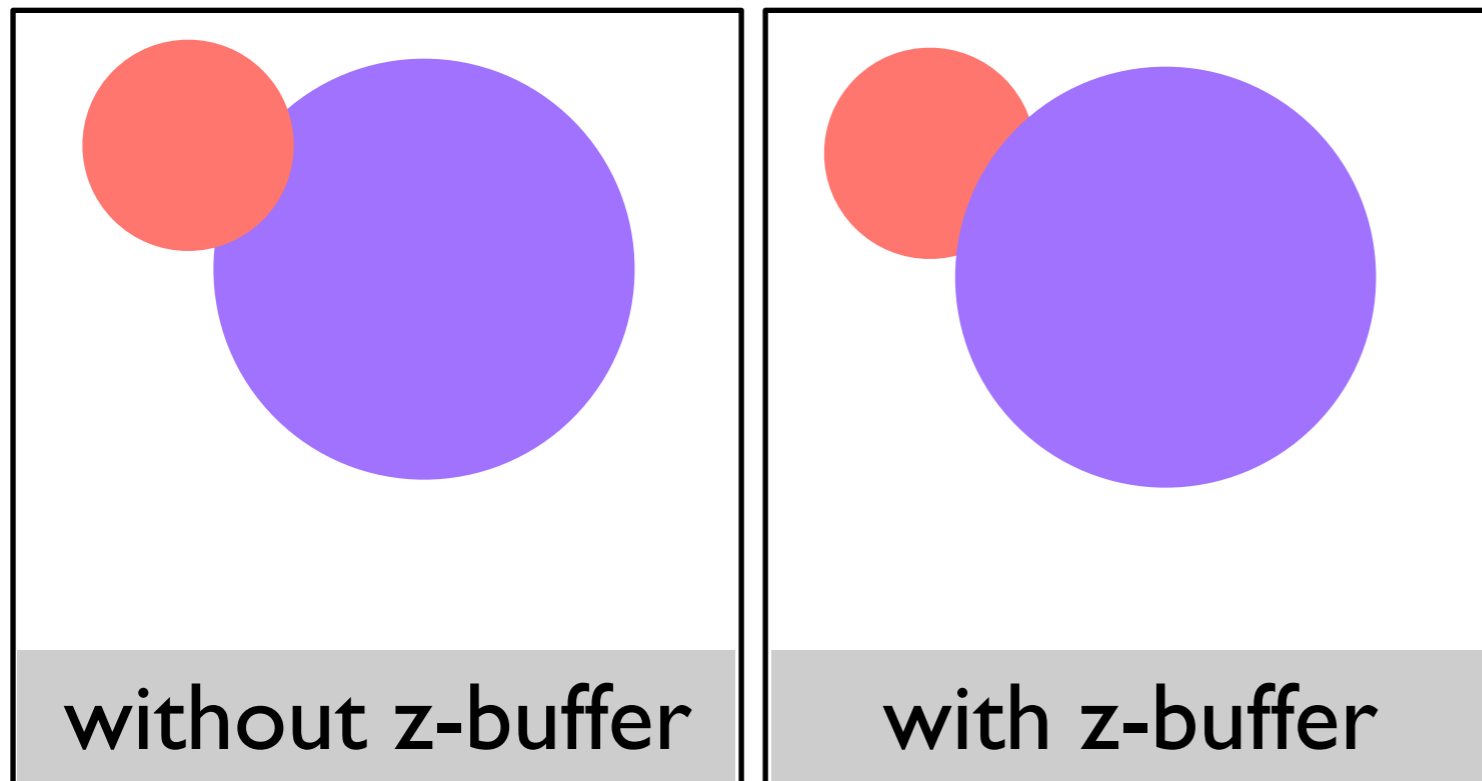
“painter’s algorithm”  
draw primitives in back-to-  
front order

**problem:**  
occlusion cycle

# Use a *z-buffer* for hidden surface removal

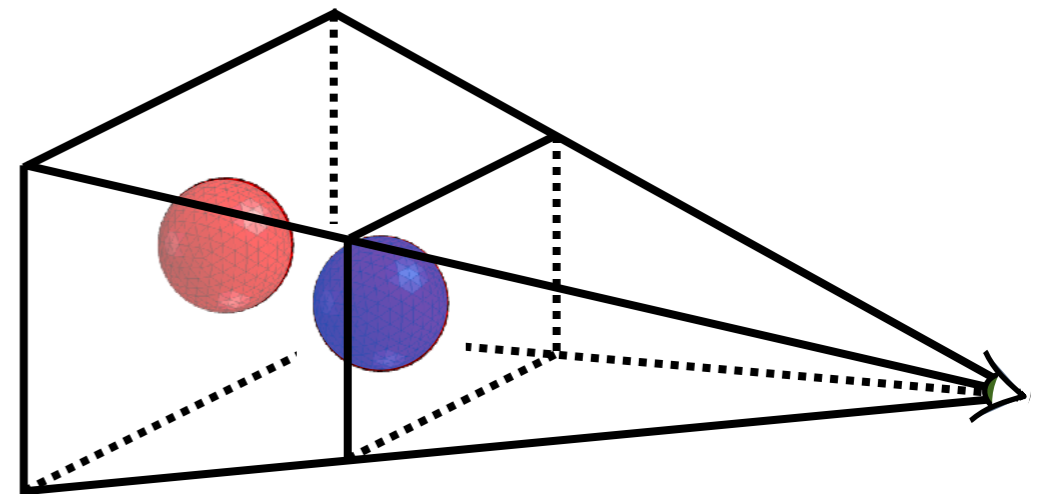
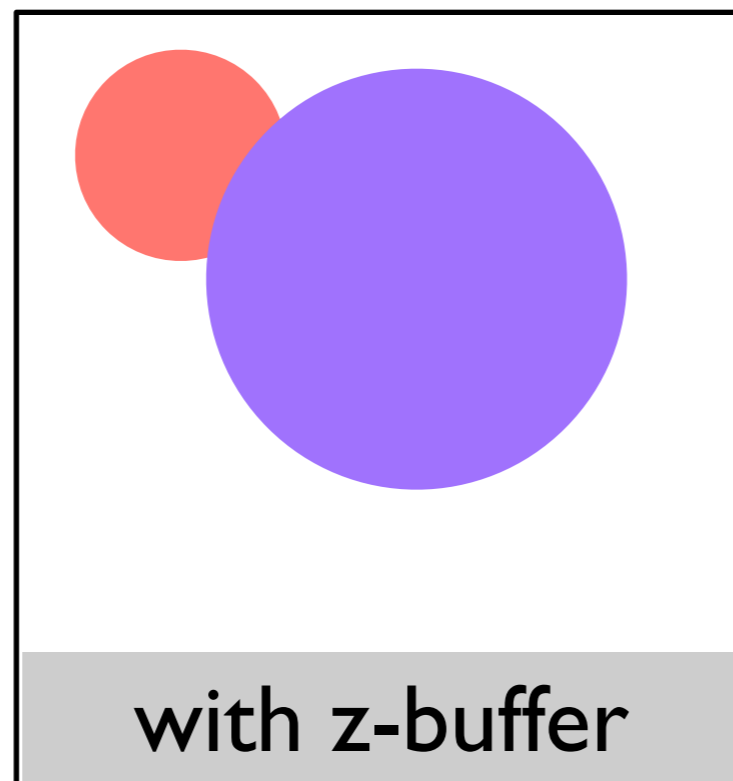
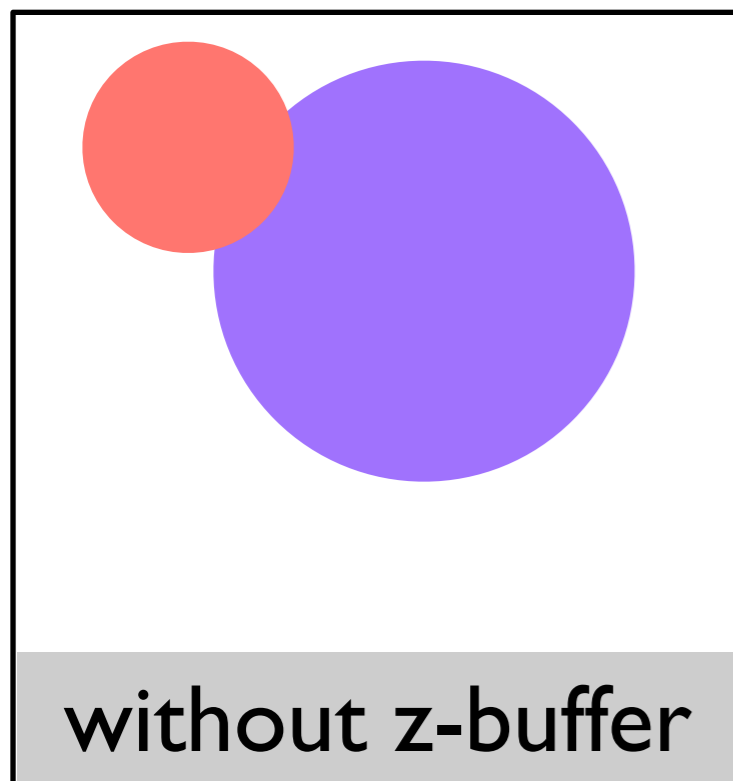
test depth on a pixel by pixel basis

red drawn last

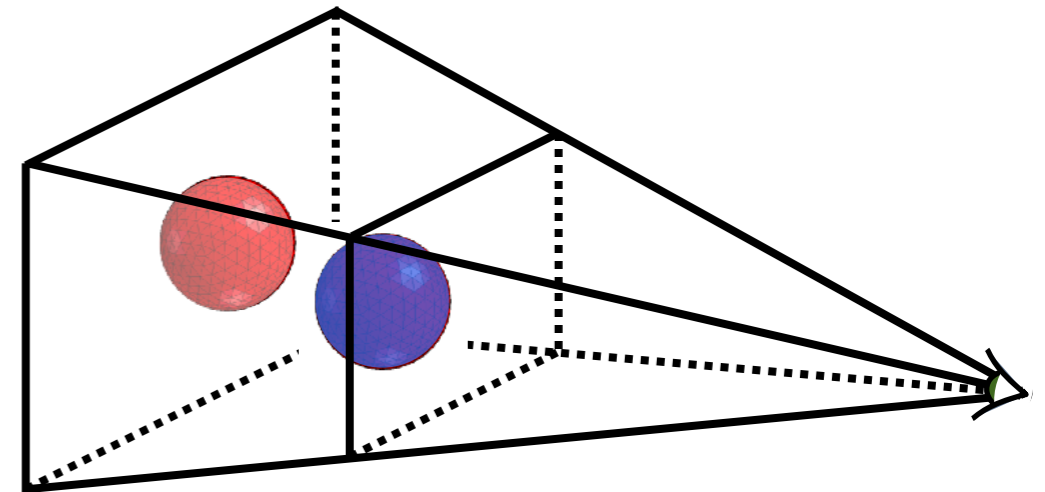
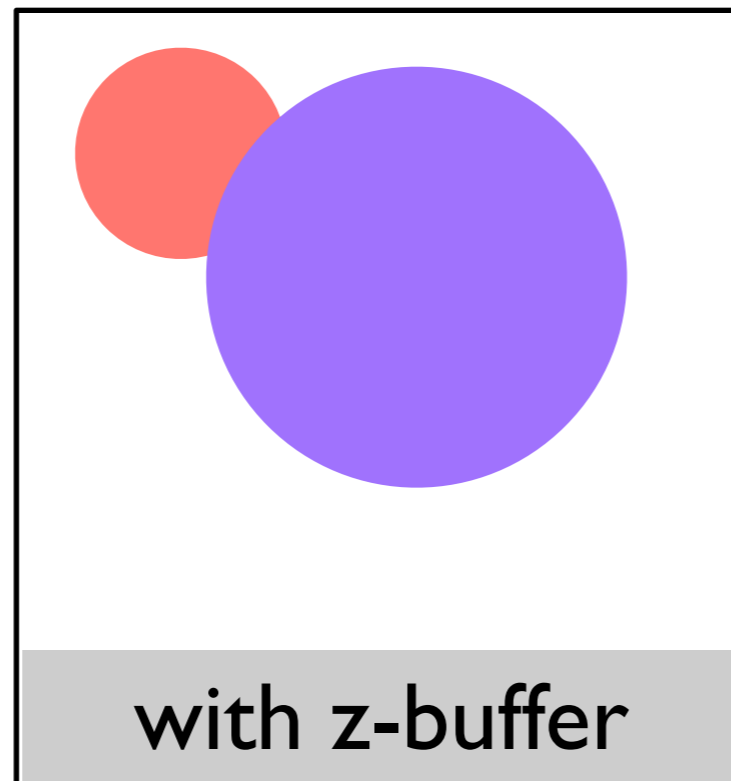
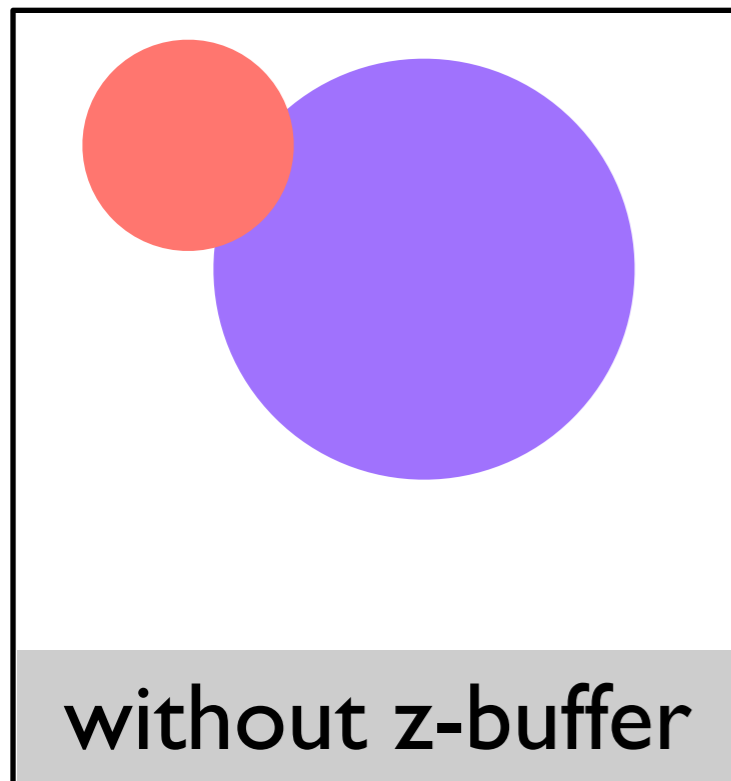
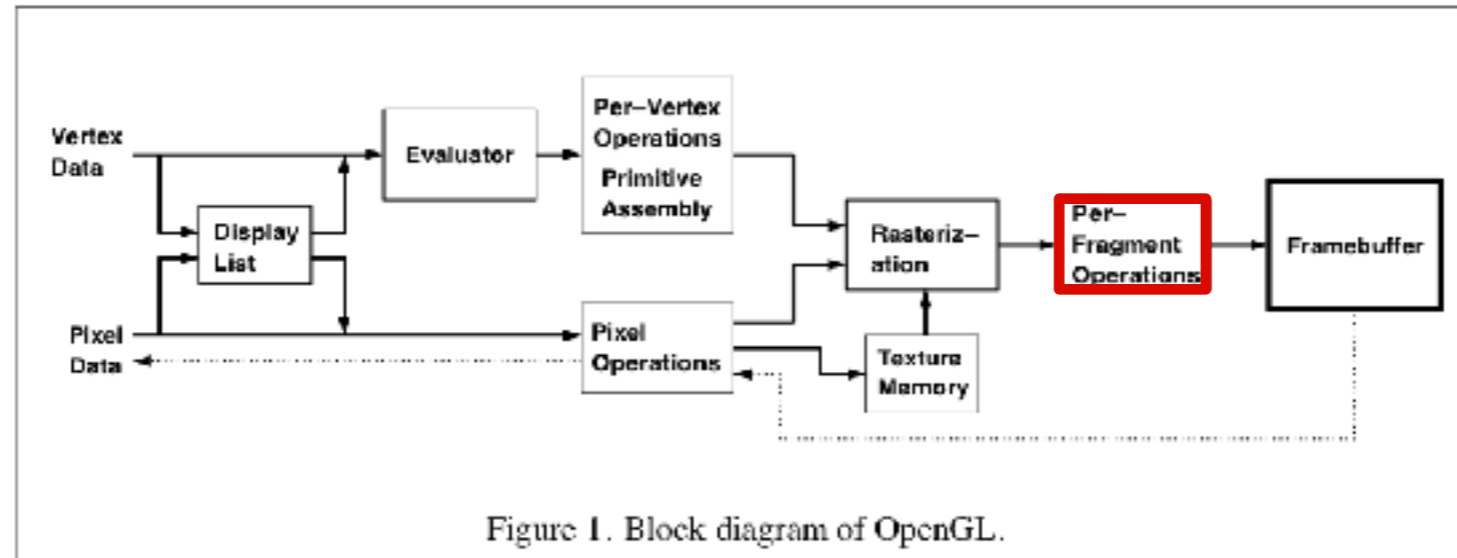


# Use a *z-buffer* for hidden surface removal

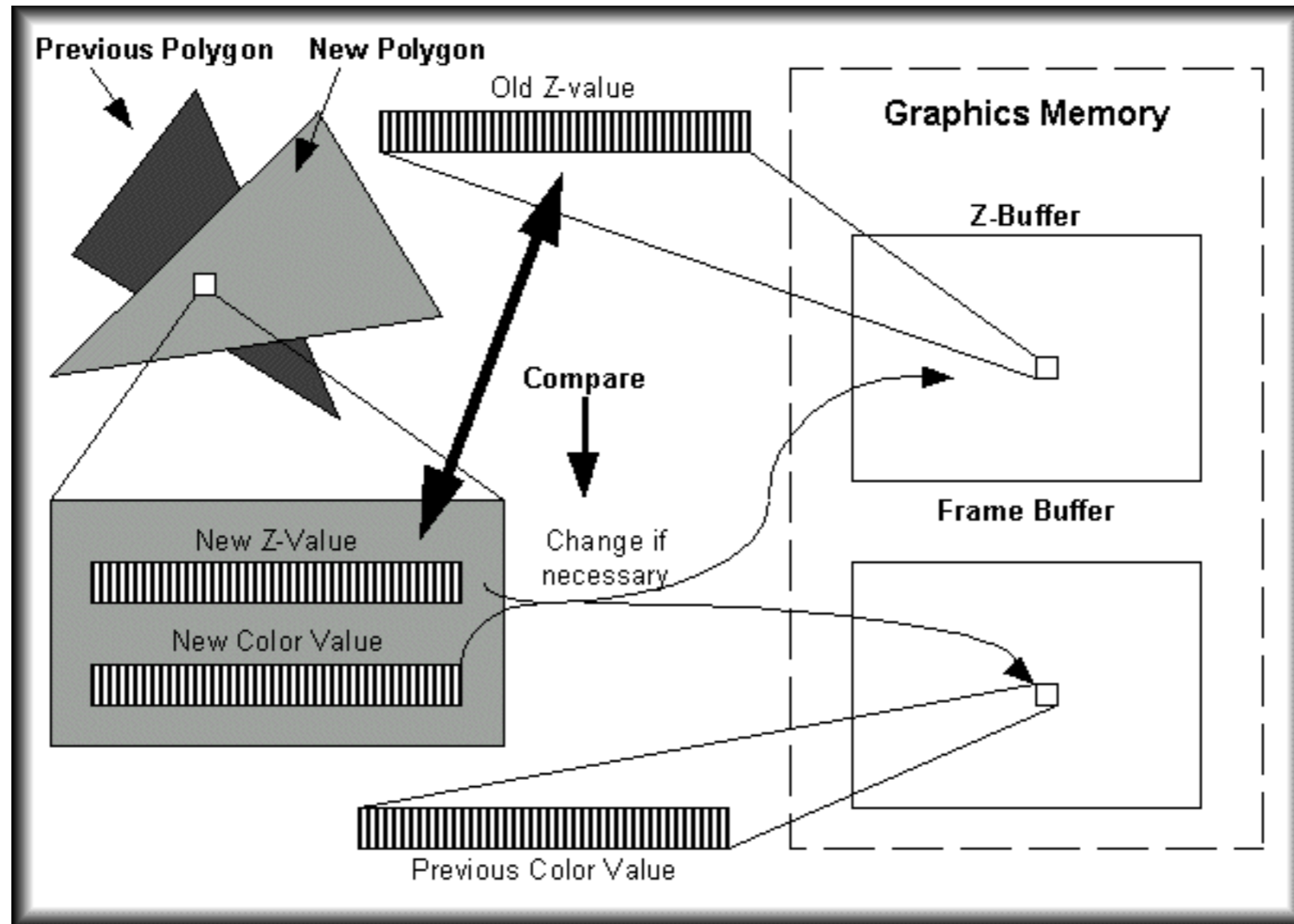
at each pixel, record distance to the closest object that has been drawn in a *depth* buffer



# Use a *z-buffer* for hidden surface removal

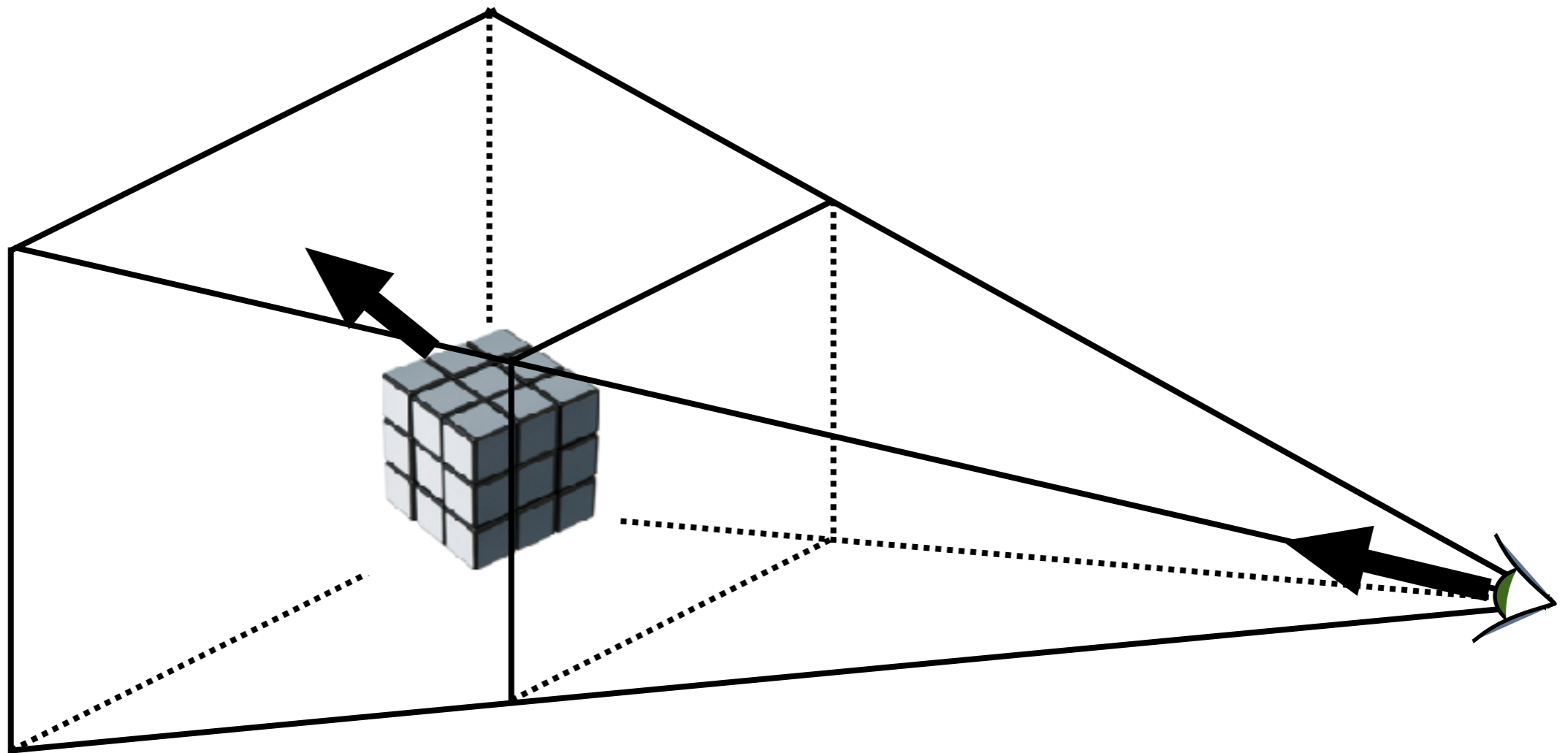


# Use a *z-buffer* for hidden surface removal



<http://www.beyond3d.com/content/articles/41/>

# Backface culling: another way to eliminate hidden geometry



# Hidden Surface Removal in OpenGL

```
glutInitDisplayMode(GLUT_DOUBLE | GLUT_RGB | GLUT_DEPTH);
```

```
glEnable(GL_DEPTH_TEST);
```

```
glEnable(GL_CULL_FACE);
```

For a perspective transformation, there is more precision in the depth buffer for z-values closer to the near plane