

CS 130 : Computer Graphics

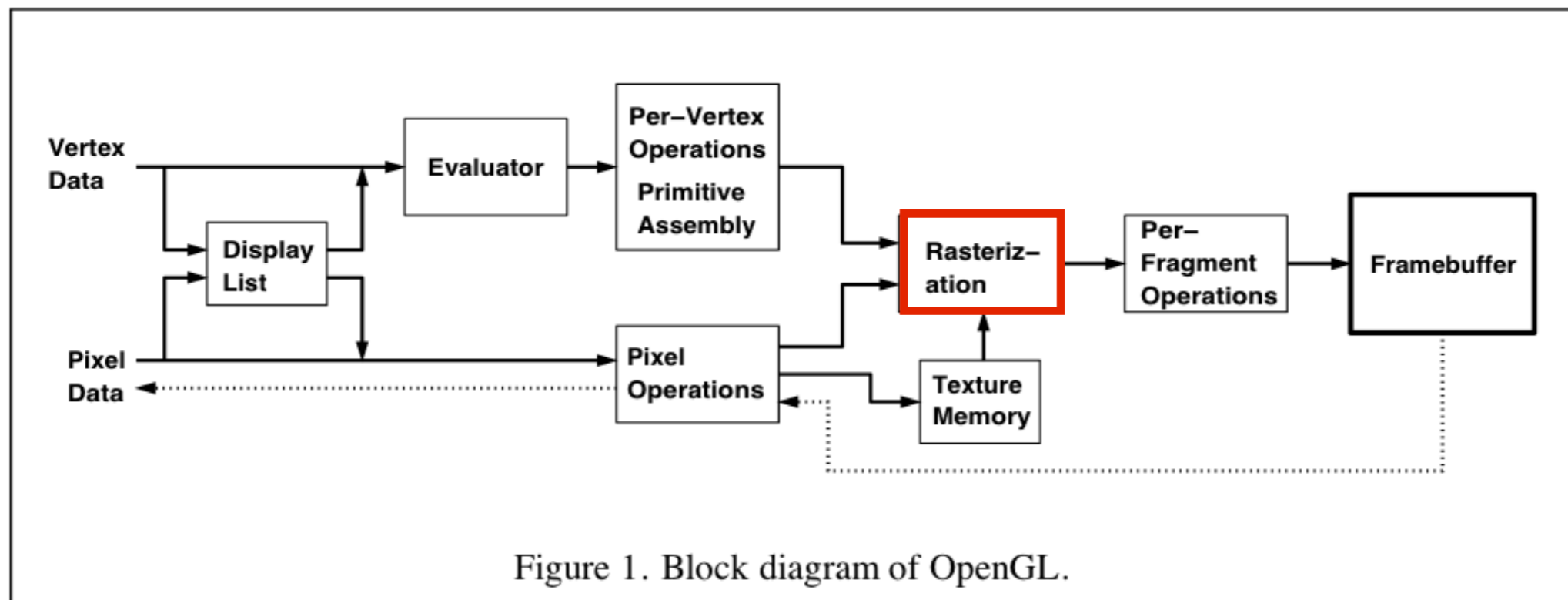
Lecture 5: Rasterizing Triangles

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What is rasterization?

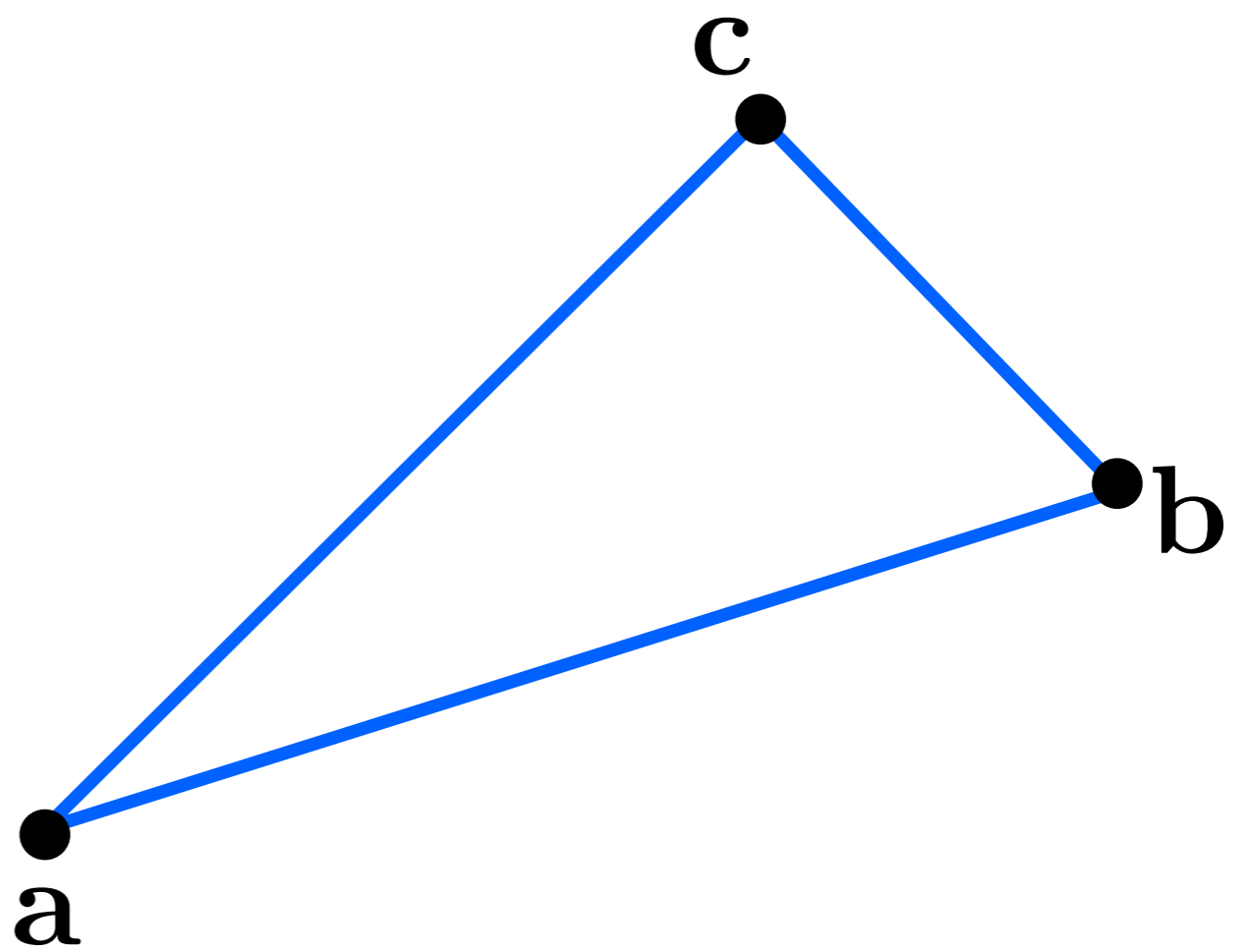


- input: primitives, output: fragments
- enumerate the pixels covered by a primitive
- interpolate attributes across the primitive

- **output** 1 fragment per pixel covered by the primitive

Triangles

barycentric coordinates



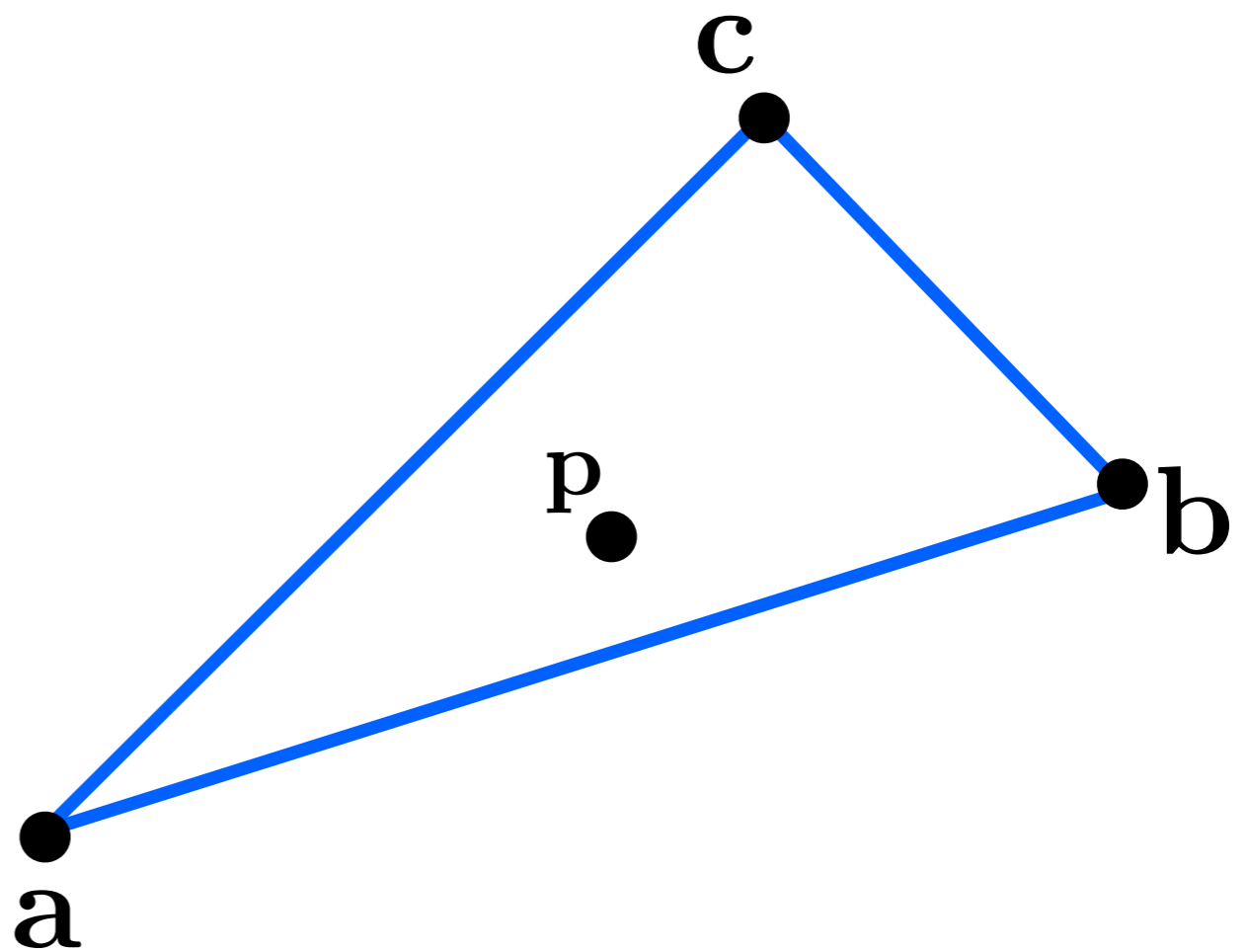
barycentric coordinates

$$\mathbf{p} = f(\mathbf{a}, \mathbf{b}, \mathbf{c})$$

$$\mathbf{p} = \alpha \mathbf{a} + \beta \mathbf{b} + \gamma \mathbf{c}$$

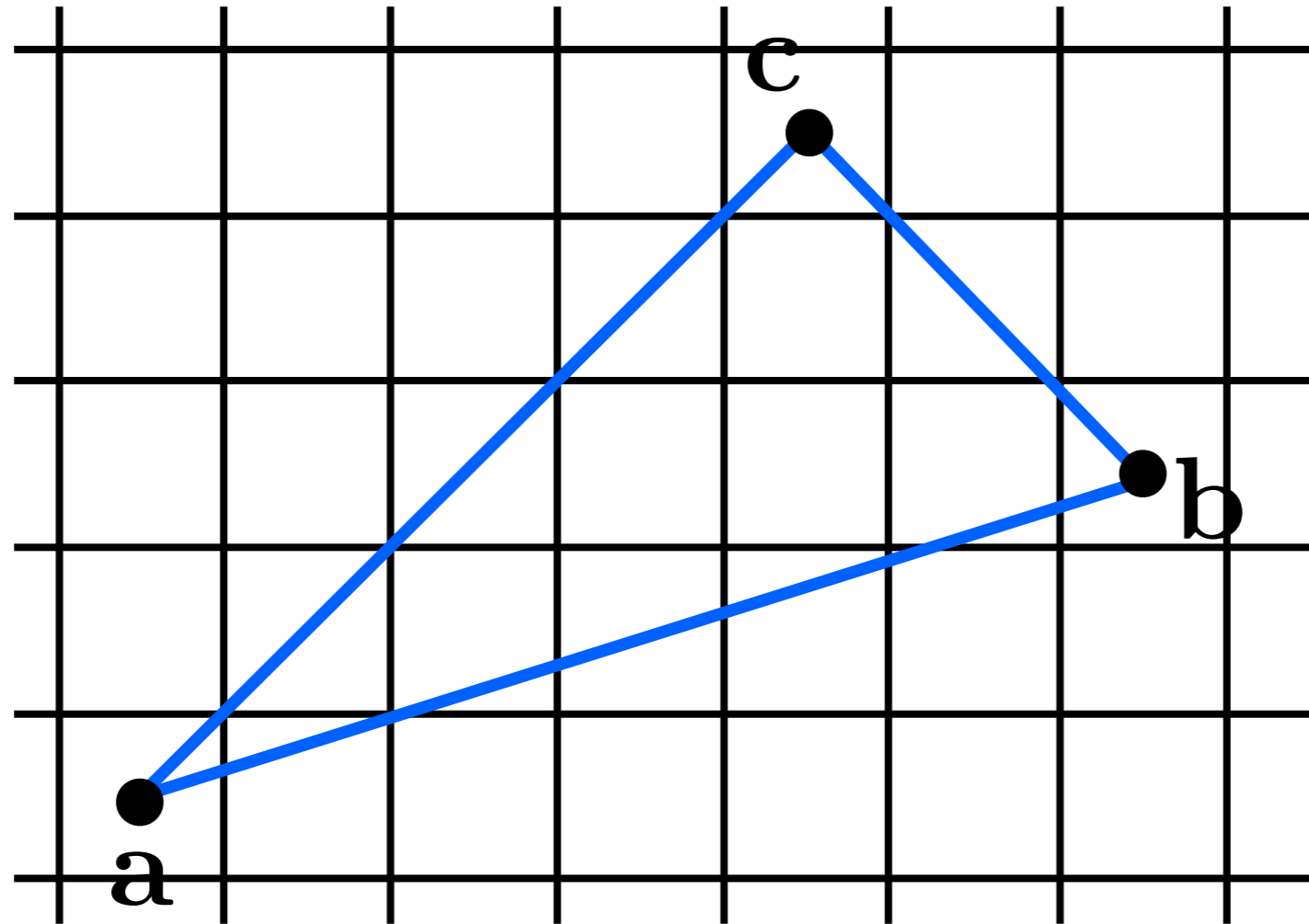
What are (α, β, γ) ?

<whiteboard>

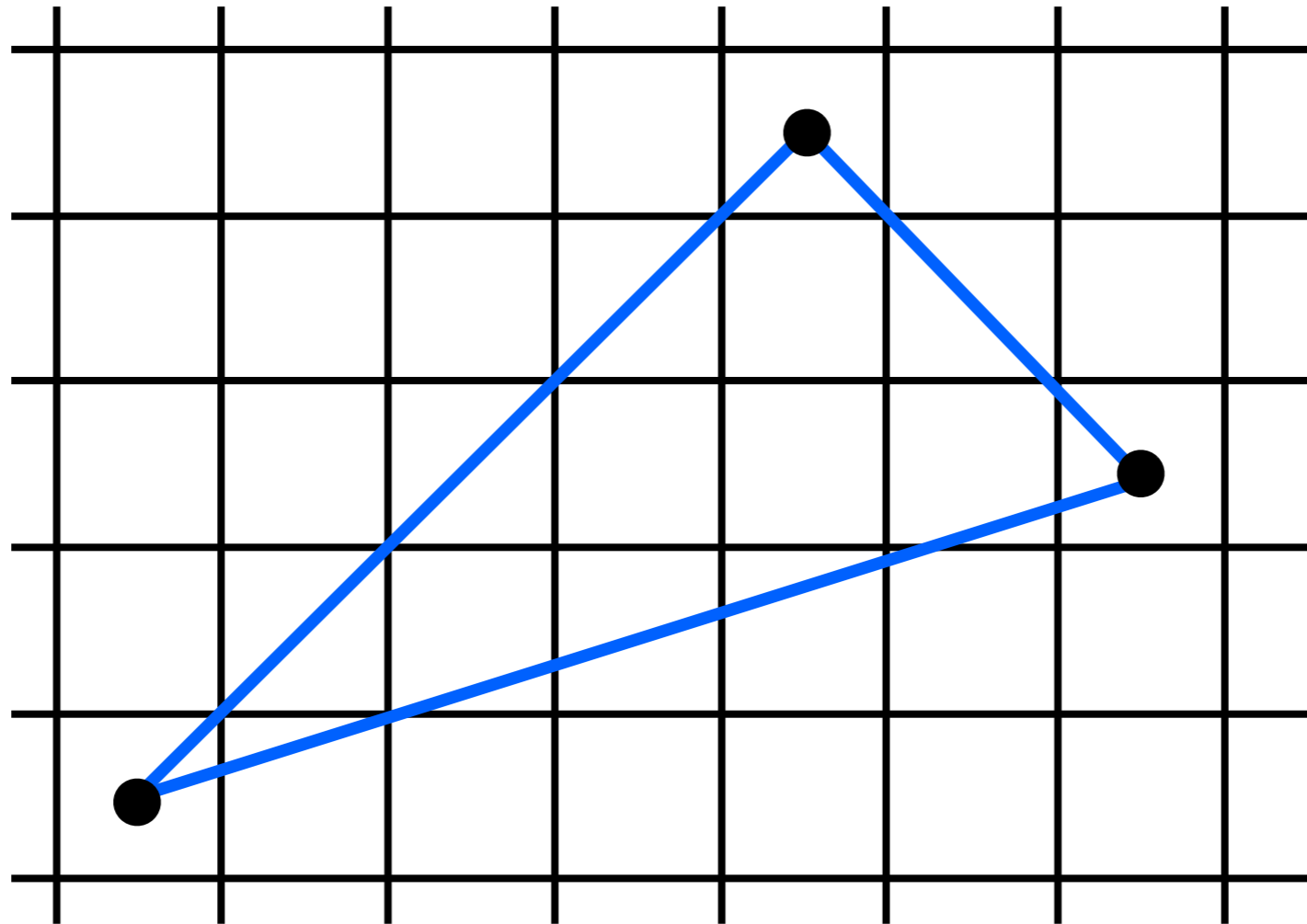


Triangle rasterization

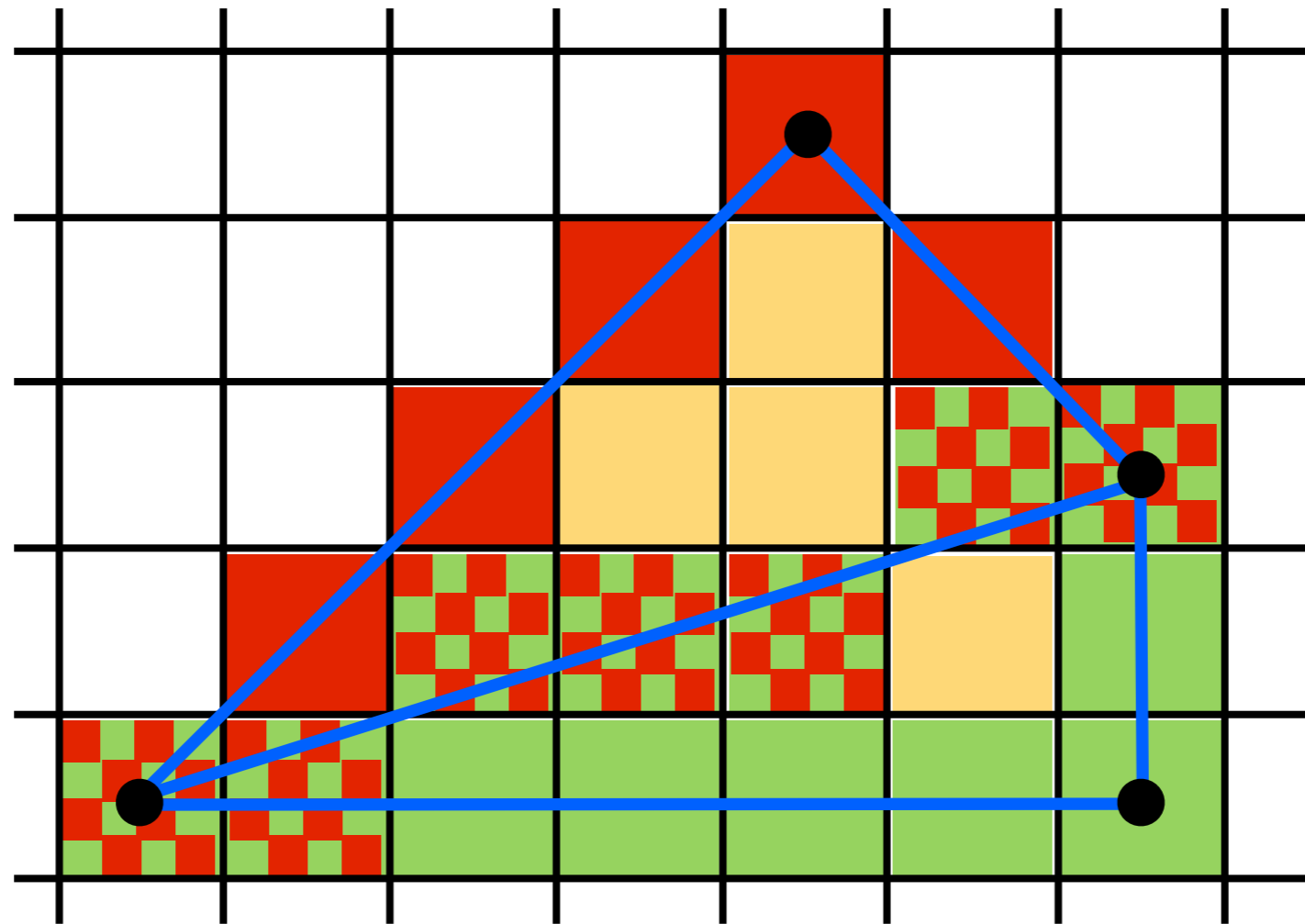
Which pixels should be used to approximate a triangle?



Triangle rasterization issues



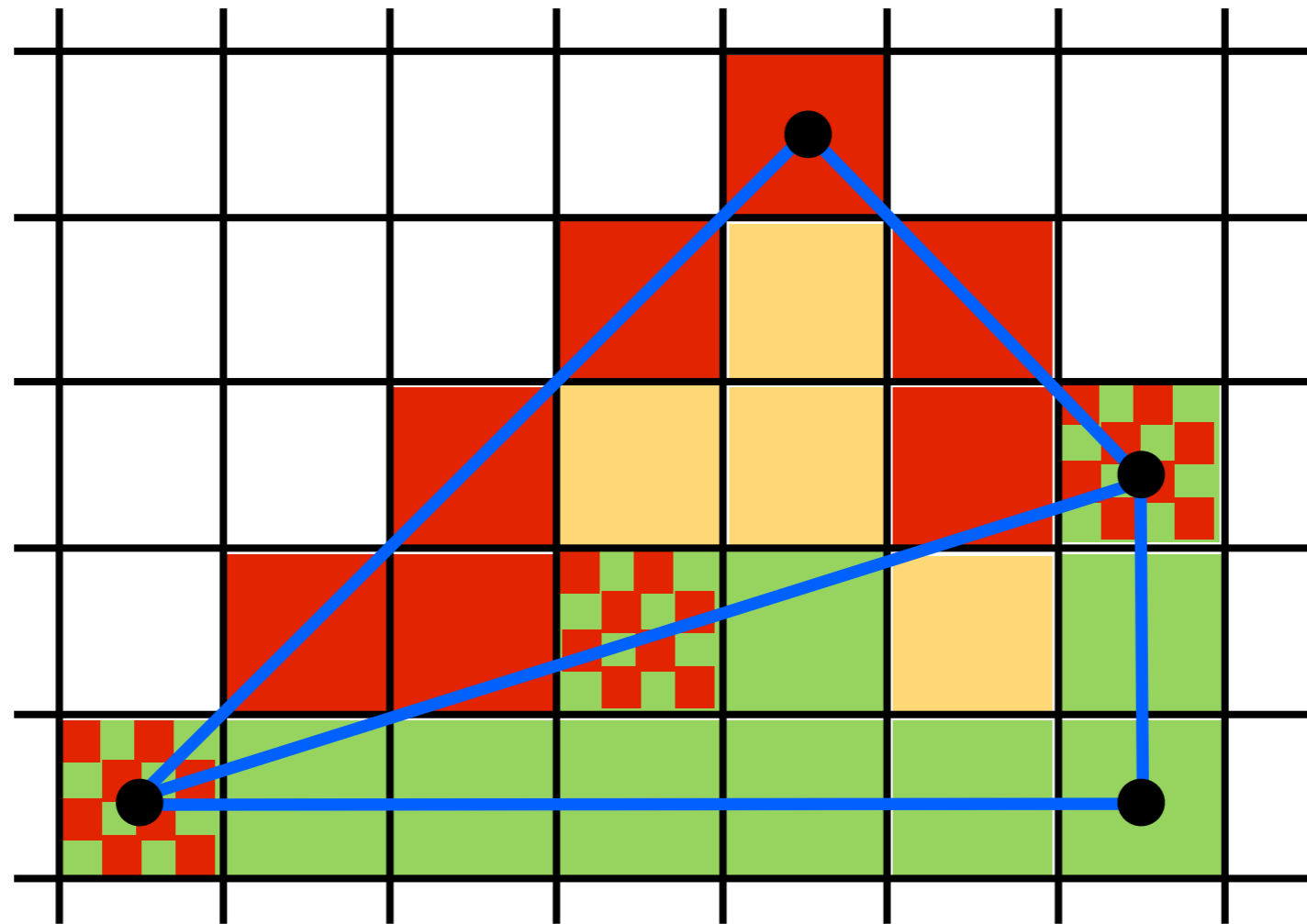
Which pixels should be used to approximate a triangle?



Who should fill in shared edge?

but who should fill in pixels for a shared edge?

Which pixels should be used to approximate a triangle?



Who should fill in shared edge?

give to triangle that contains pixel center

– but we have some **ties**

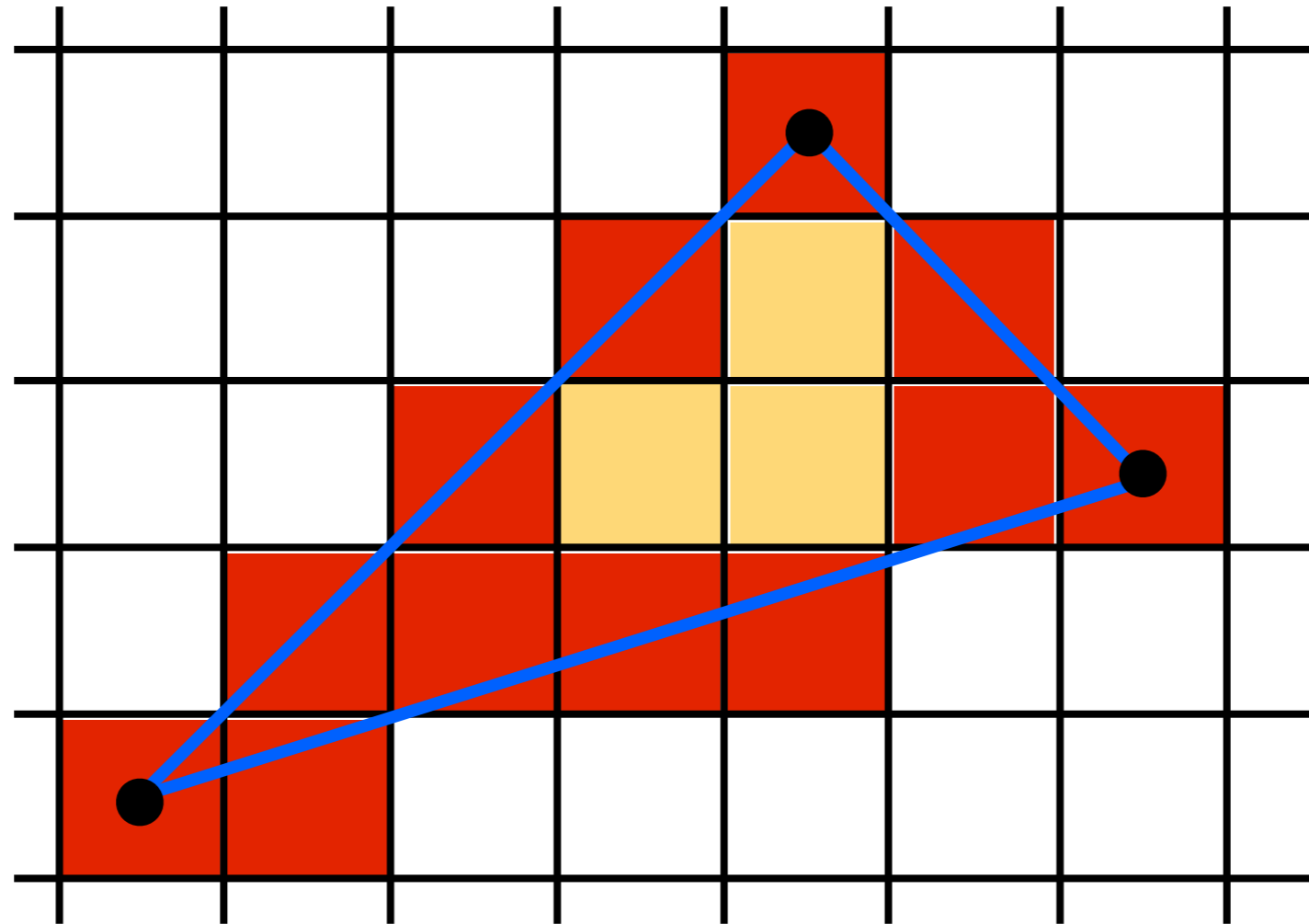
why can't neither/both triangles draw the pixel?

neither: gaps

both: indeterminacy (due to indeterminate drawing order), incorrect, e.g., if both triangles are partially transparent

we want a **unique** assignment

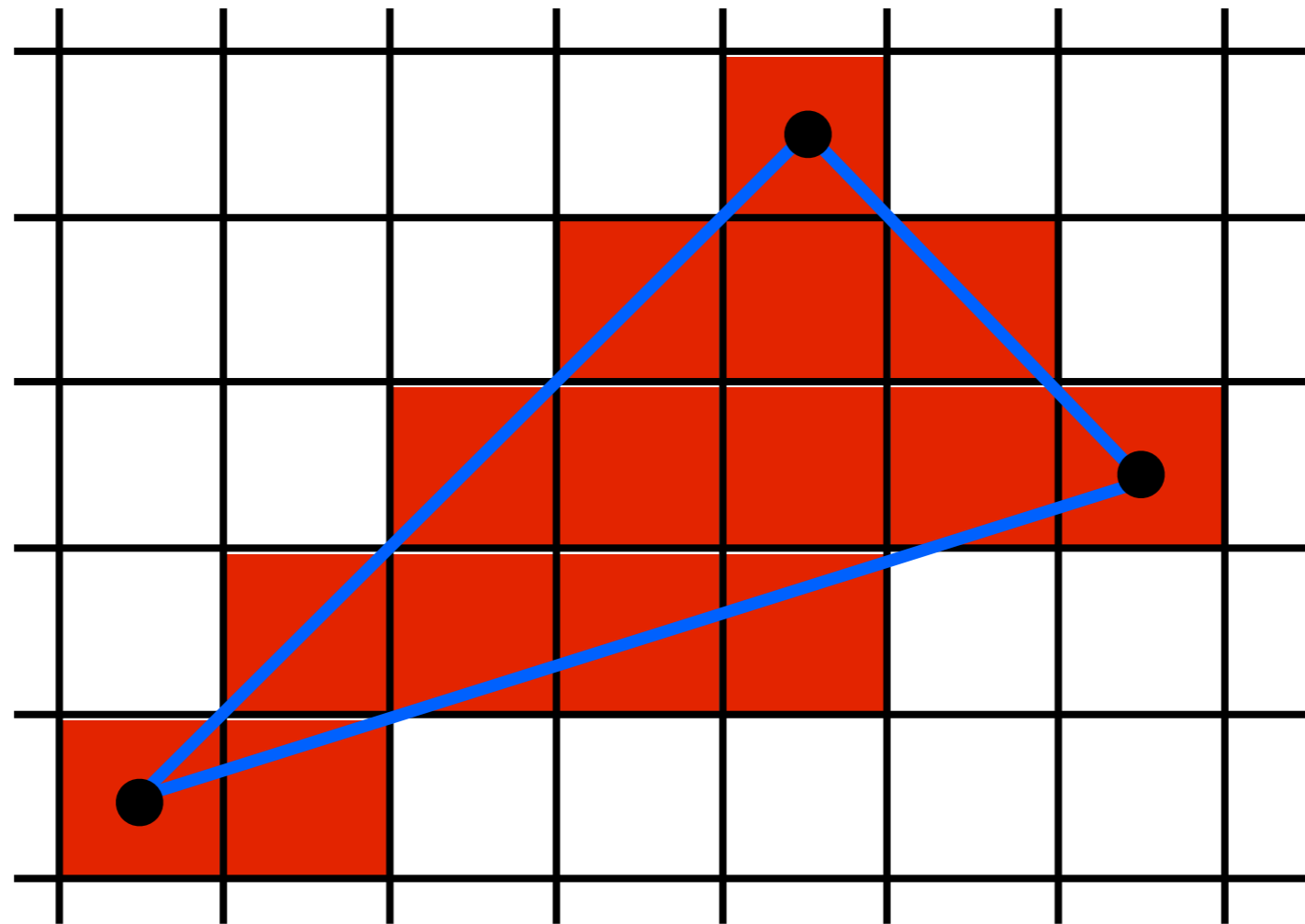
Which pixels should be used to approximate a triangle?



Use Midpoint Algorithm for edges and fill in?

That could be one possibility but we use a different approach based on barycentric coordinates

Which pixels should be used to approximate a triangle?



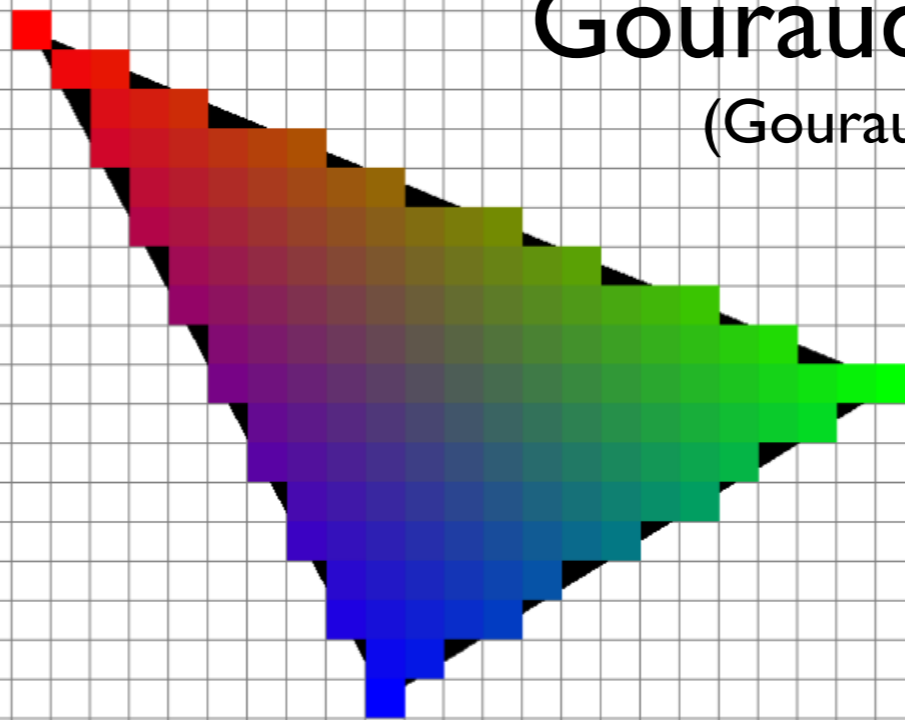
Use an approach based on
barycentric coordinates

For each pixel, we compute its barycentric coordinates
If the coordinates are all ≥ 0 , then the pixel is covered by the triangle

We can interpolate attributes using barycentric coordinates

$$\mathbf{c} = \alpha\mathbf{c}_0 + \beta\mathbf{c}_1 + \gamma\mathbf{c}_2$$

Gouraud shading
(Gouraud, 1971)

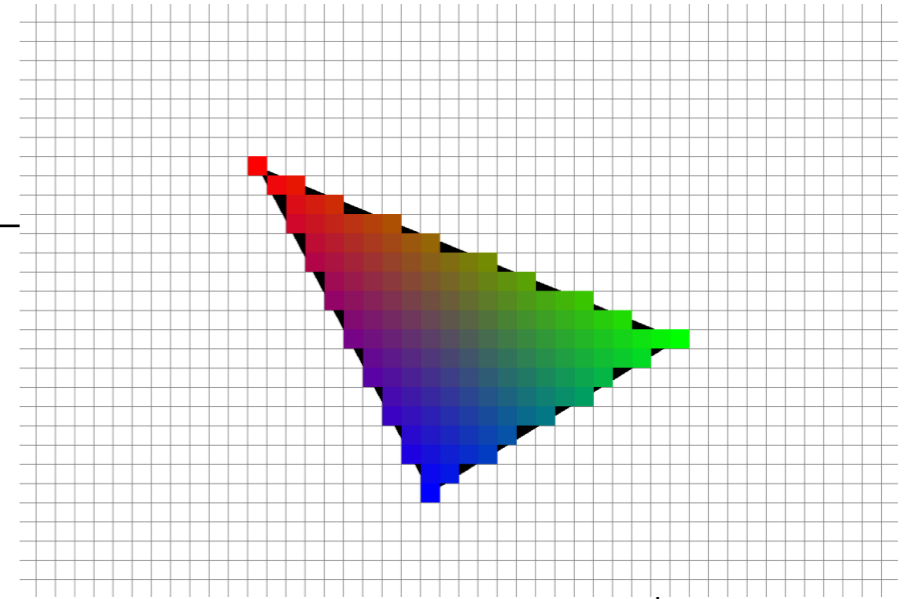


<http://jtibble.dyndns.org/graphics/eecs487/eecs487.html>

Using barycentric coordinates also has the advantage that we can easily interpolate colors or other attributes from triangle vertices

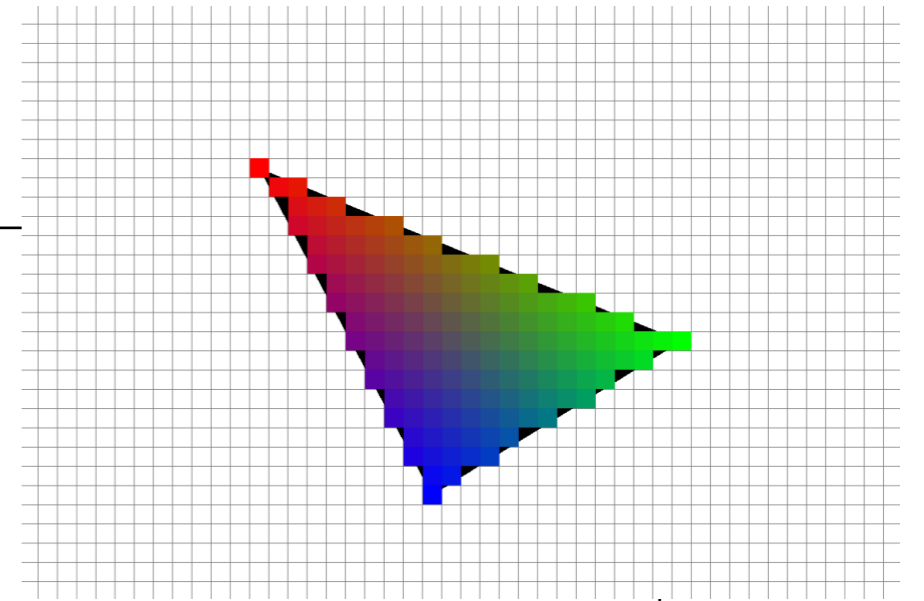
Triangle rasterization algorithm

```
for all x do
  for all y do
    compute  $(\alpha, \beta, \gamma)$  for  $(x, y)$ 
    if  $(\alpha \in [0, 1]$  and  $\beta \in [0, 1]$  and  $\gamma \in [0, 1])$  then
       $\mathbf{c} = \alpha \mathbf{c}_0 + \beta \mathbf{c}_1 + \gamma \mathbf{c}_2$ 
      drawpixel $(x, y)$  with color  $\mathbf{c}$ 
```



Triangle rasterization algorithm

```
for all x do
  for all y do
    compute  $(\alpha, \beta, \gamma)$  for  $(x, y)$ 
    if  $(\alpha \in [0, 1]$  and  $\beta \in [0, 1]$  and  $\gamma \in [0, 1])$  then
       $c = \alpha c_0 + \beta c_1 + \gamma c_2$ 
      drawpixel $(x, y)$  with color c
```

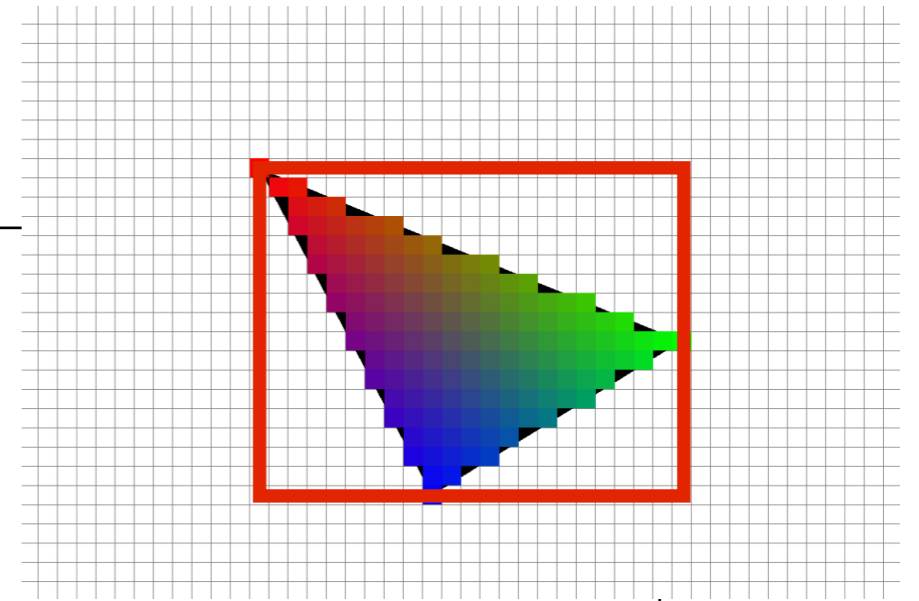


the rest of the algorithm is to make the steps in **red** more **efficient**

Triangle rasterization algorithm

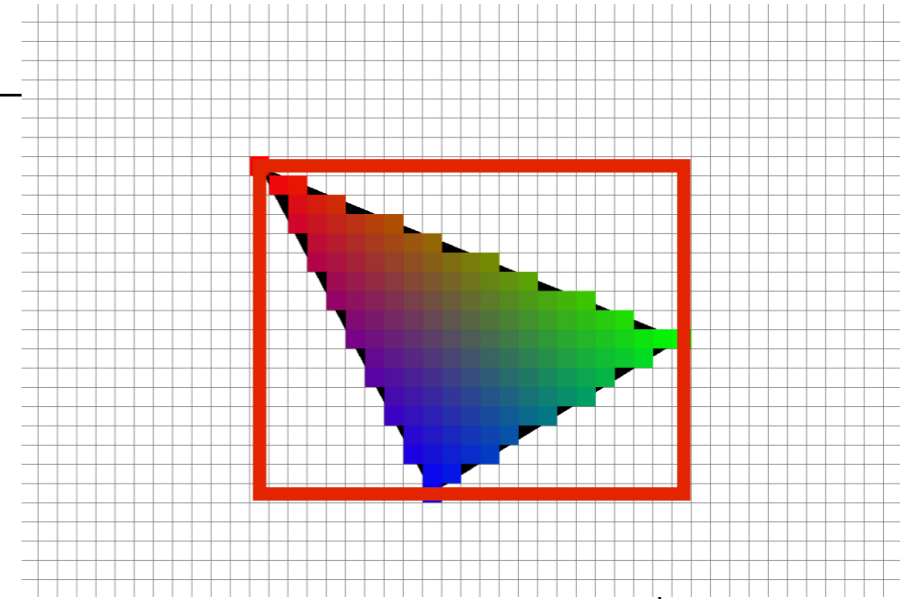
use a bounding rectangle

```
for x in [x_min, x_max]
  for y in [y_min, y_max]
    compute  $(\alpha, \beta, \gamma)$  for  $(x, y)$ 
    if  $(\alpha \in [0, 1]$  and  $\beta \in [0, 1]$  and  $\gamma \in [0, 1])$  then
       $c = \alpha c_0 + \beta c_1 + \gamma c_2$ 
      drawpixel(x, y) with color c
```



Triangle rasterization algorithm

```
for x in [x_min, x_max]
  for y in [y_min, y_max]
     $\alpha = f_{bc}(x, y) / f_{bc}(x_a, y_a)$ 
     $\beta = f_{ac}(x, y) / f_{ac}(x_b, y_b)$ 
     $\gamma = f_{ab}(x, y) / f_{ab}(x_c, y_c)$ 
    if ( $\alpha \in [0, 1]$  and  $\beta \in [0, 1]$  and  $\gamma \in [0, 1]$ ) then
       $\mathbf{c} = \alpha \mathbf{c}_0 + \beta \mathbf{c}_1 + \gamma \mathbf{c}_2$ 
      drawpixel(x,y) with color c
```



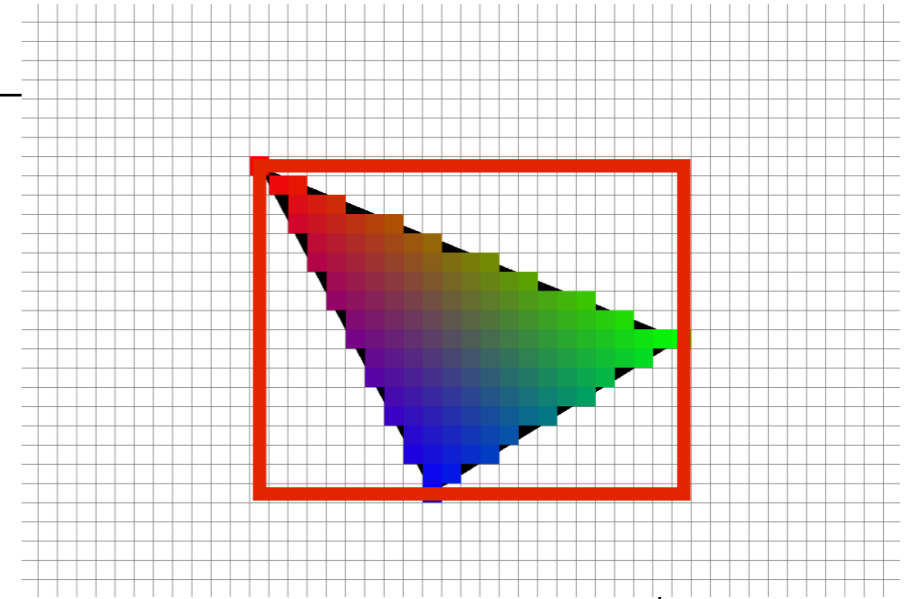
<whiteboard>

<whiteboard> : computing alpha, beta, and gamma

Triangle rasterization algorithm

Optimizations?

```
for x in [x_min, x_max]
  for y in [y_min, y_max]
     $\alpha = f_{bc}(x, y) / f_{bc}(x_a, y_a)$ 
     $\beta = f_{ac}(x, y) / f_{ac}(x_b, y_b)$ 
     $\gamma = f_{ab}(x, y) / f_{ab}(x_c, y_c)$ 
    if ( $\alpha \in [0, 1]$  and  $\beta \in [0, 1]$  and  $\gamma \in [0, 1]$ ) then
       $\mathbf{c} = \alpha \mathbf{c}_0 + \beta \mathbf{c}_1 + \gamma \mathbf{c}_2$ 
      drawpixel(x,y) with color c
```

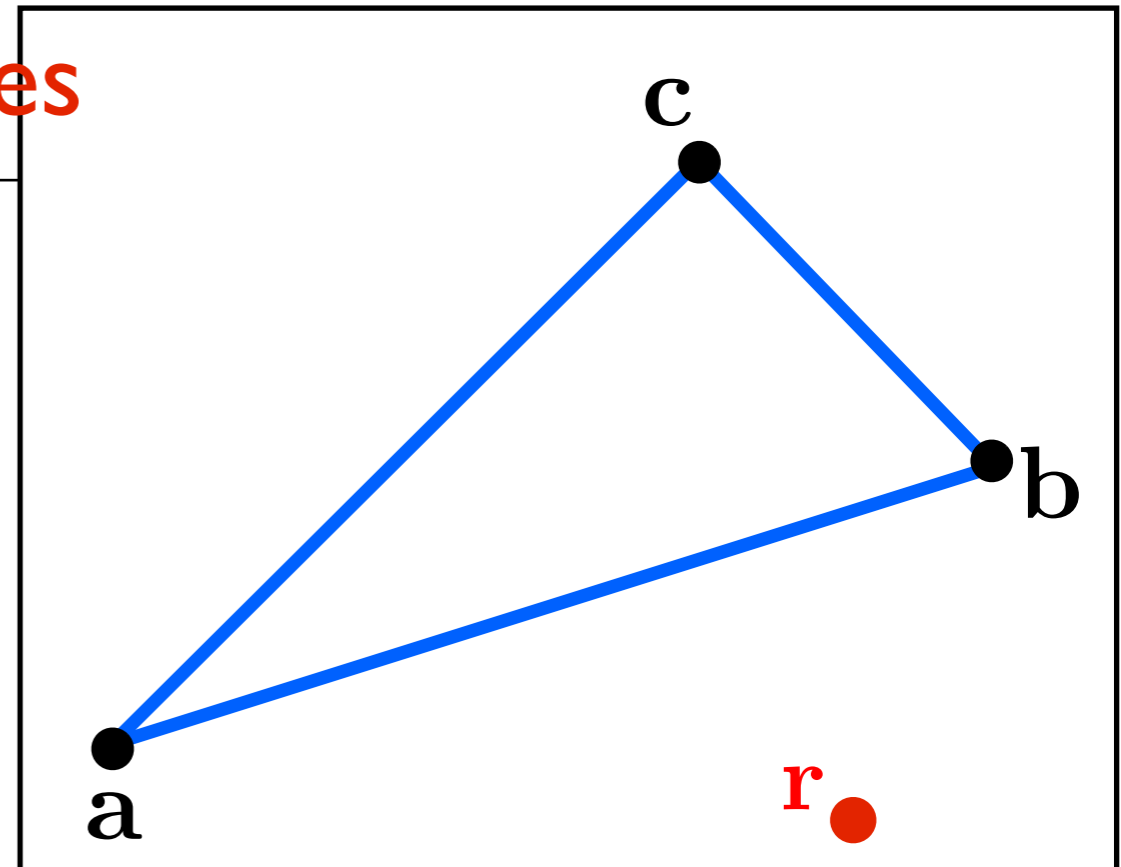


1. can make computation of bary. coords. **incremental**
 - $f(x,y) = Ax + By + C$
 - $f(x+1,y) = f(x,y) + A$
2. **color** computation can also be made **incremental**
3. **alpha > 0 and beta > 0 and gamma > 0** (if true => they are also less than one)

Triangle rasterization algorithm

dealing with shared triangle edges

```
for x in [x_min, x_max]
  for y in [y_min, y_max]
     $\alpha = f_{bc}(x, y) / f_{bc}(x_a, y_a)$ 
     $\beta = f_{ac}(x, y) / f_{ac}(x_b, y_b)$ 
     $\gamma = f_{ab}(x, y) / f_{ab}(x_c, y_c)$ 
    if ( $\alpha \geq 0$  and  $\beta \geq 0$  and  $\gamma \geq 0$ ) then
      if ( $\alpha > 0$  or  $f_{12}(\mathbf{p}_0)f_{12}(\mathbf{r}) > 0$ ) and
         ( $\beta > 0$  or  $f_{20}(\mathbf{p}_1)f_{20}(\mathbf{r}) > 0$ ) and
         ( $\gamma > 0$  or  $f_{01}(\mathbf{p}_2)f_{01}(\mathbf{r}) > 0$ )
        then
           $\mathbf{c} = \alpha\mathbf{c}_0 + \beta\mathbf{c}_1 + \gamma\mathbf{c}_2$ 
          drawpixel(x,y) with color c
```



- compute $f_{12}(\mathbf{r})$, $f_{20}(\mathbf{r})$ and $f_{01}(\mathbf{r})$ and make sure \mathbf{r} doesn't hit a line