

# CSI 30 : Computer Graphics

Lecture 9: Texture Mapping

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# There are limits to geometric modeling



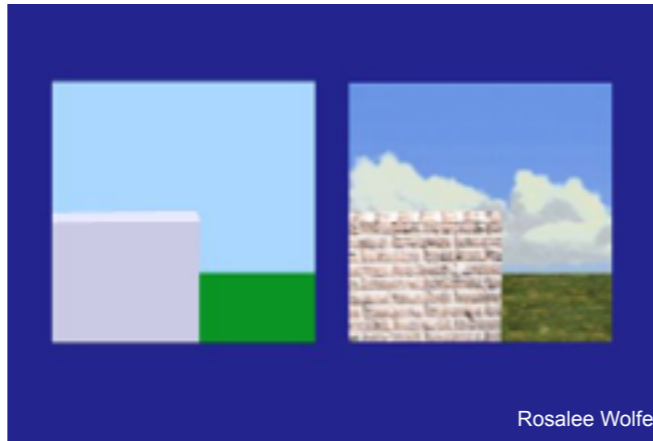
<http://www.beinteriordecorator.com>



National Geographic

Although modern GPUs can render millions of triangles/sec,  
that's not enough sometimes...

# Use texture mapping to increase realism through detail

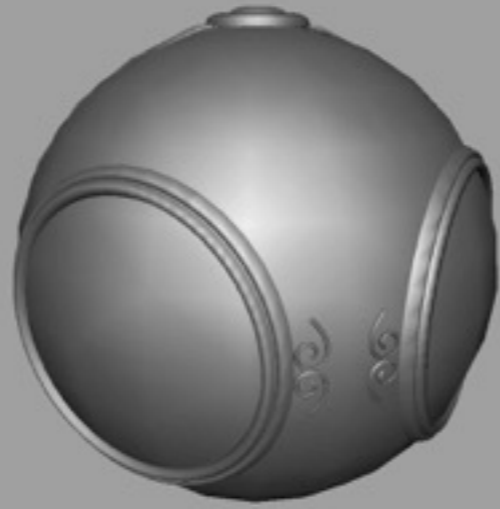


This image is just 8 polygons!

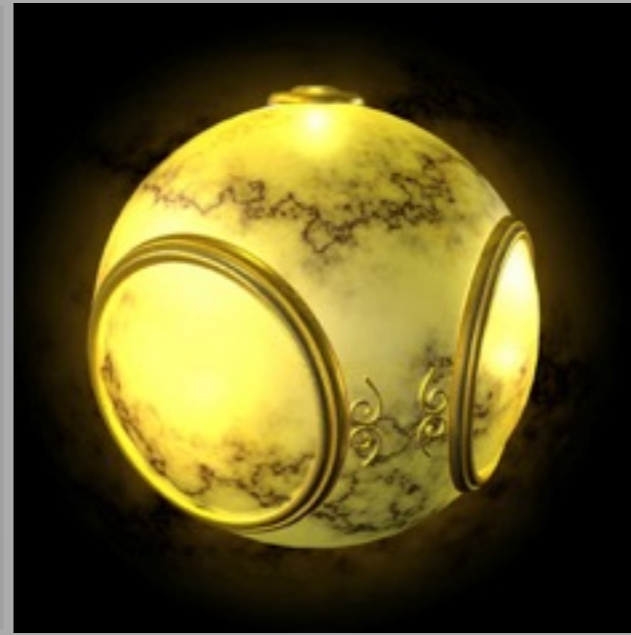
Add visual complexity.

[http://www.siggraph.org/education/materials/HyperGraph/mapping/r\\_wolfe/r\\_wolfe\\_mapping\\_1.htm](http://www.siggraph.org/education/materials/HyperGraph/mapping/r_wolfe/r_wolfe_mapping_1.htm)

[Angel and Shreiner]



No texture

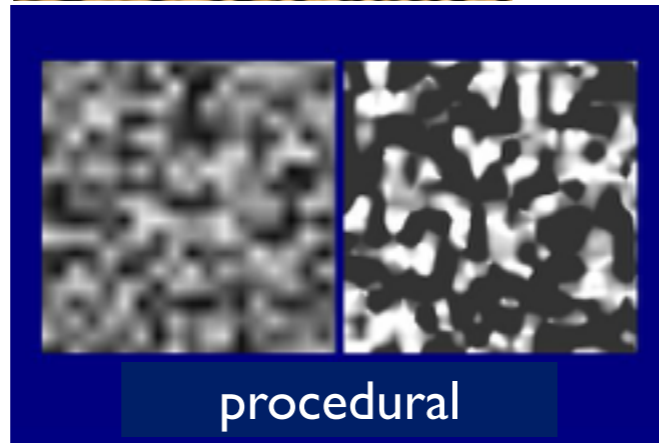
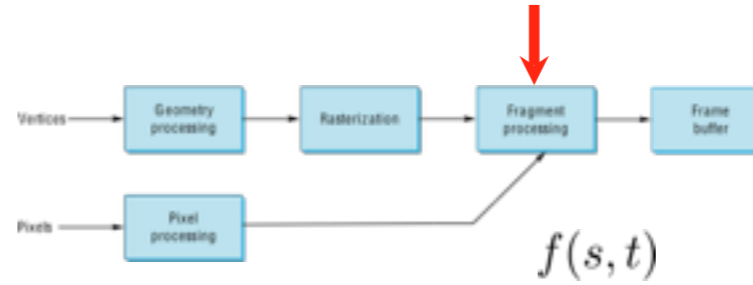
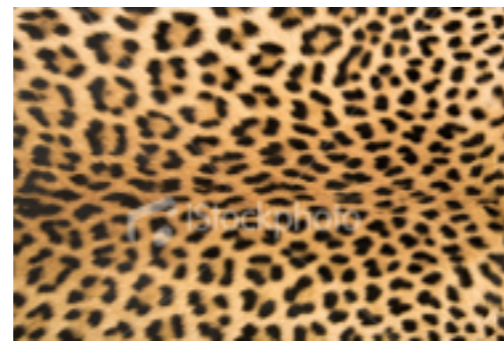


With texture



Pixar - Toy Story

# Store 2D images in buffers and lookup pixel reflectances



photo

Textures can be anything that you can lookup values in -- photo, procedurally generated, or even a function that computes a value on the fly

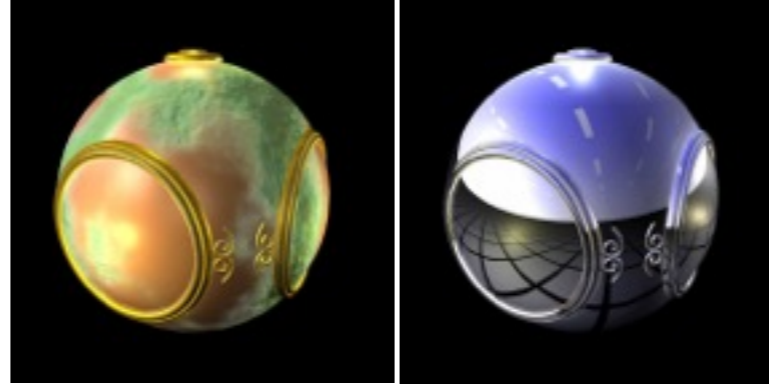
# 3D solid textures



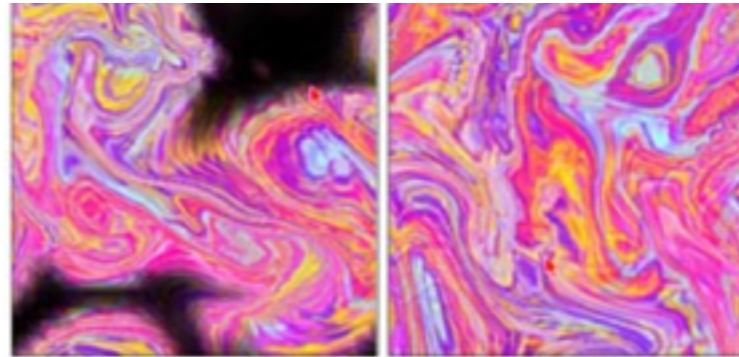
[Dong et al., 2008]

# Other uses of textures...

Light maps  
Shadow maps  
Environment maps  
Bump maps  
Opacity maps  
Animation



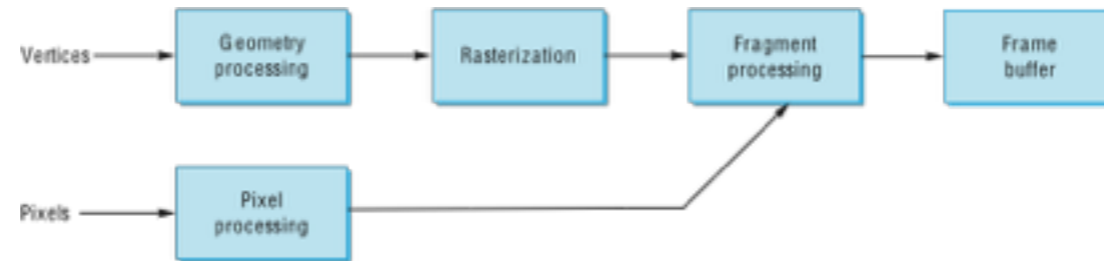
[Angel and Shreiner]



[Stam 99]

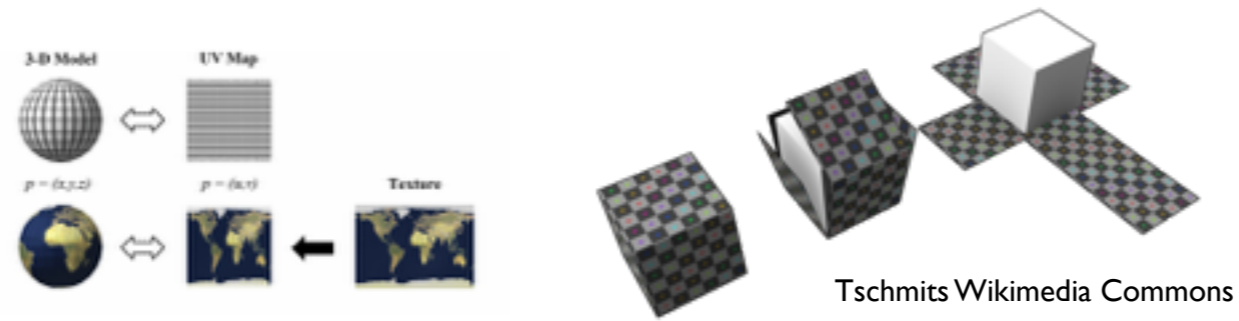


# Texture mapping in the OpenGL pipeline

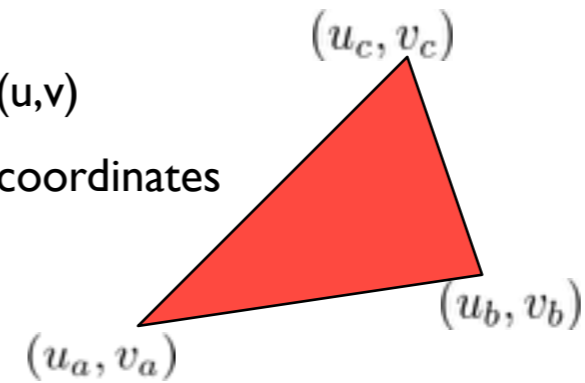


- Geometry and pixels have separate paths through pipeline
- meet in **fragment processing** - where textures are applied
- texture mapping applied at end of pipeline - efficient since relatively few polygons get past clipper

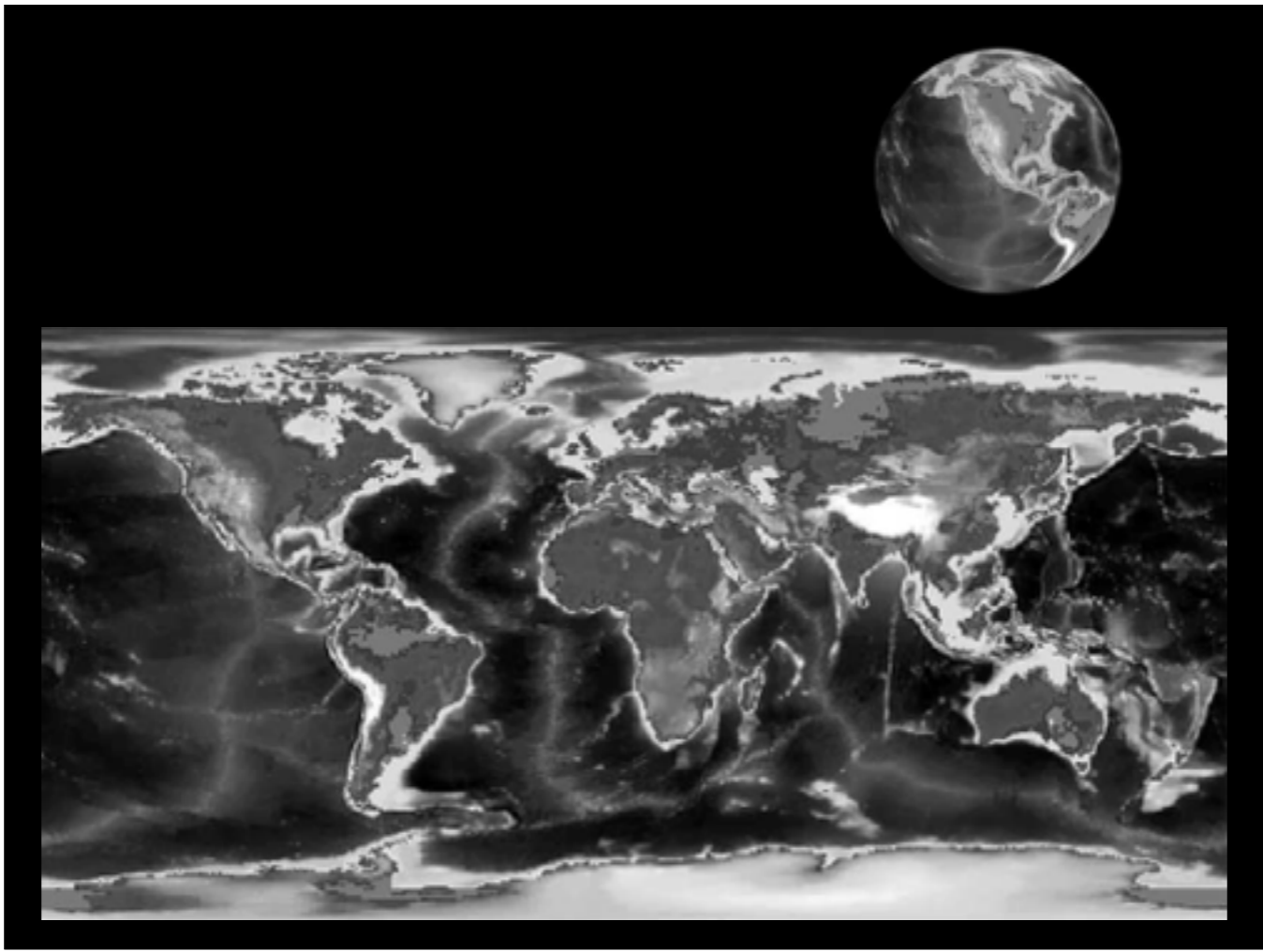
# uv Mapping



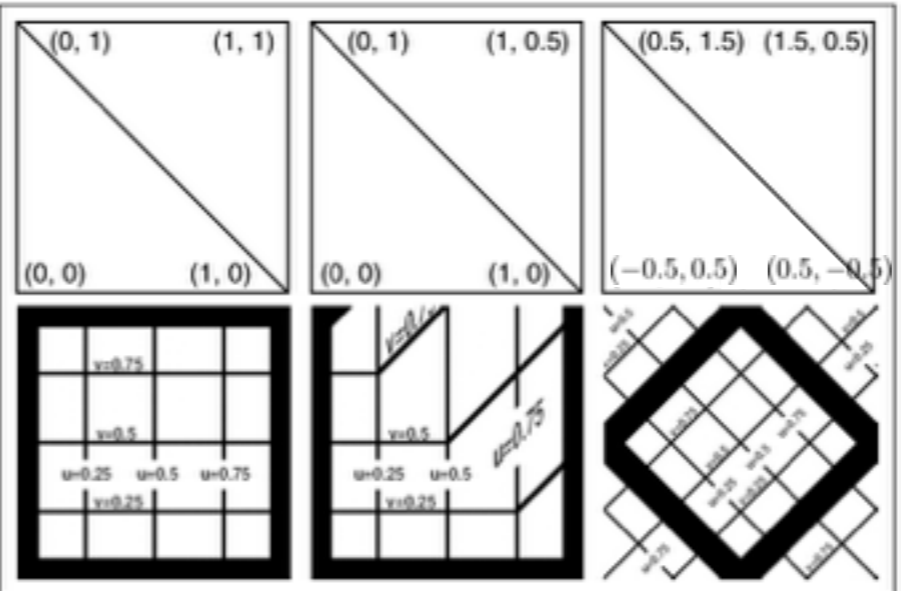
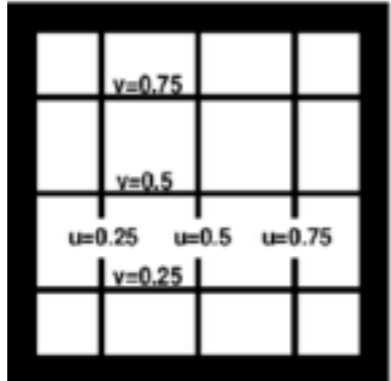
- 2D texture is parameterized by  $(u, v)$
- Assign polygon vertices texture coordinates
- Interpolate within polygon



Texture coordinates are per-vertex data – a position in the  $(u, v)$  space can interpolate tex coordinates with barycentric coordinates



# Texture Calibration

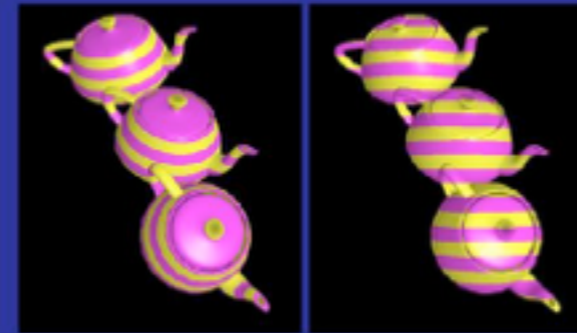


# The major issues in texture mapping...

- What should the actual mapping be?



easy: rectangular surface

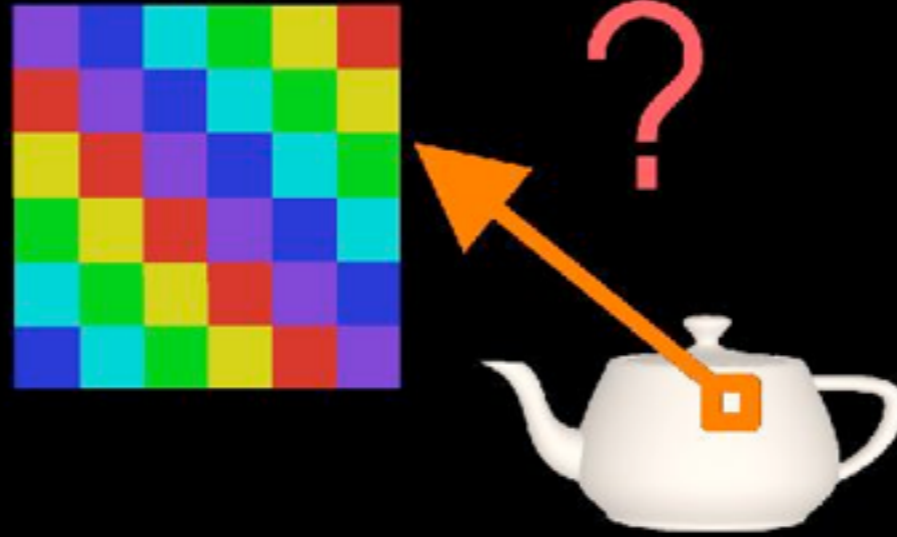


harder: parametric surface

Teapot: Which image looks better? The image on the left uses **object coordinates** in the texture mapping – this makes more sense. The image on the **right** uses **world coordinates** – texture ends up changing relative to the object  
**want a nice map that doesn't look distorted**

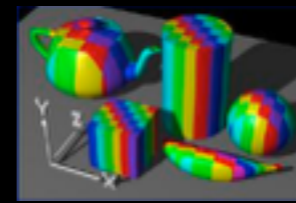
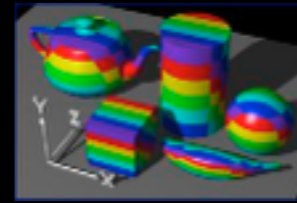
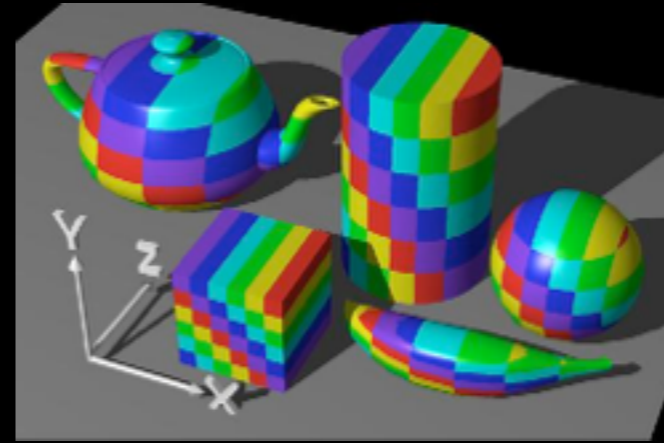
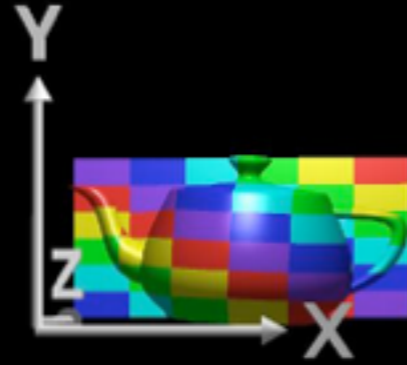
Given a point on the object  $(x,y,z)$ , what point  $(u,v)$  in the texture we use?

[Rosalee Wolfe]



# Example: planar mapping

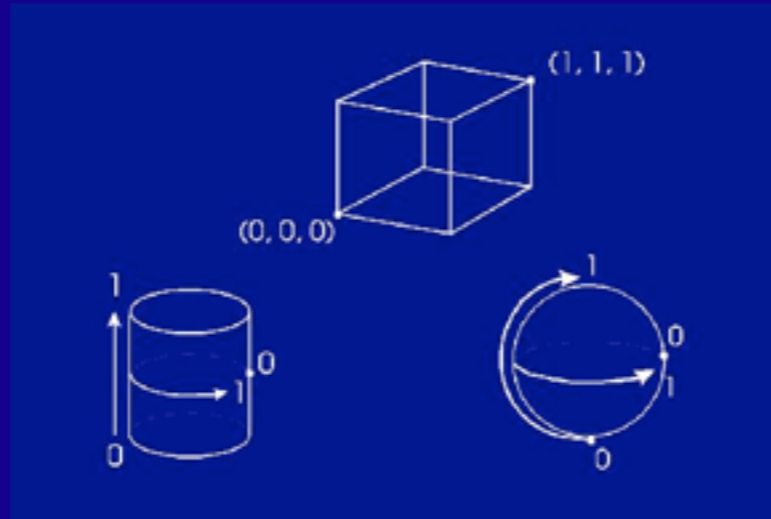
[Rosalee Wolfe]



# Intermediate surfaces

First map the texture to a simpler, intermediate surface

[Rosalee Wolfe]

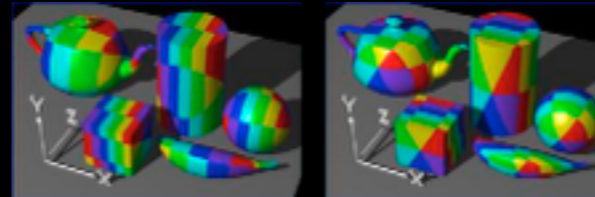
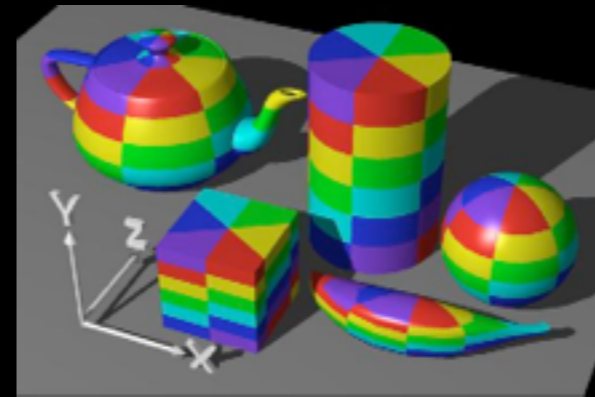




# Cylindrical mapping

$(x,y,z) \rightarrow (\text{theta}, h) \rightarrow (u,v)$

[Rosalee Wolfe]

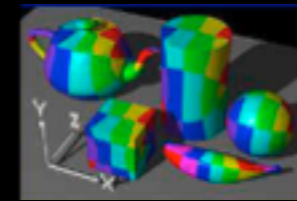
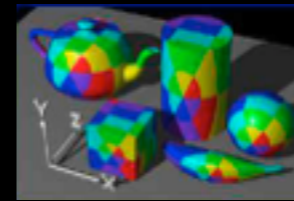
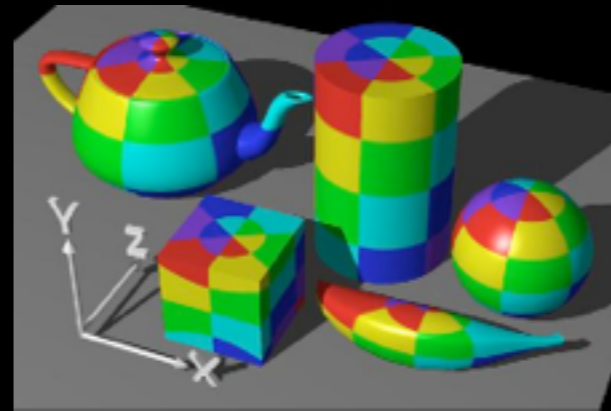
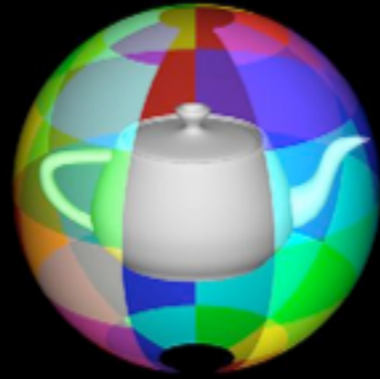


- note "pie slice" phenomena
- which coordinate axis is parallel to the cylinder axis?

# Spherical Mapping

$(x,y,z) \rightarrow (\text{latitude}, \text{longitude})$   
 $\rightarrow (u,v)$

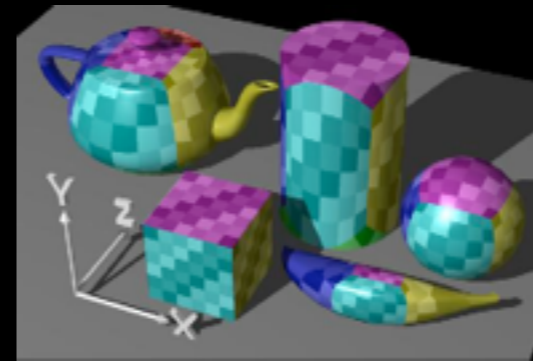
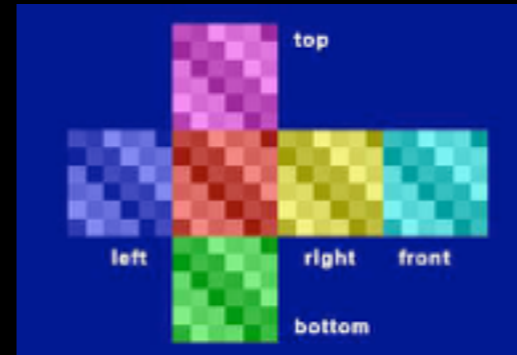
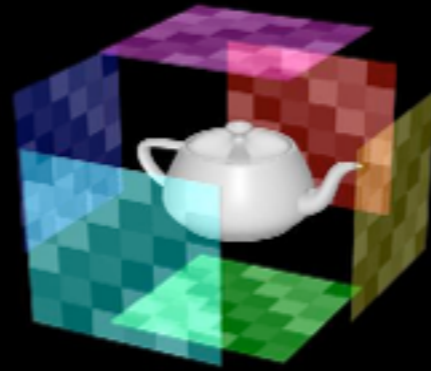
[Rosalee Wolfe]



spherical map stretches squares at equator and squeezes squares at poles

# Box Mapping

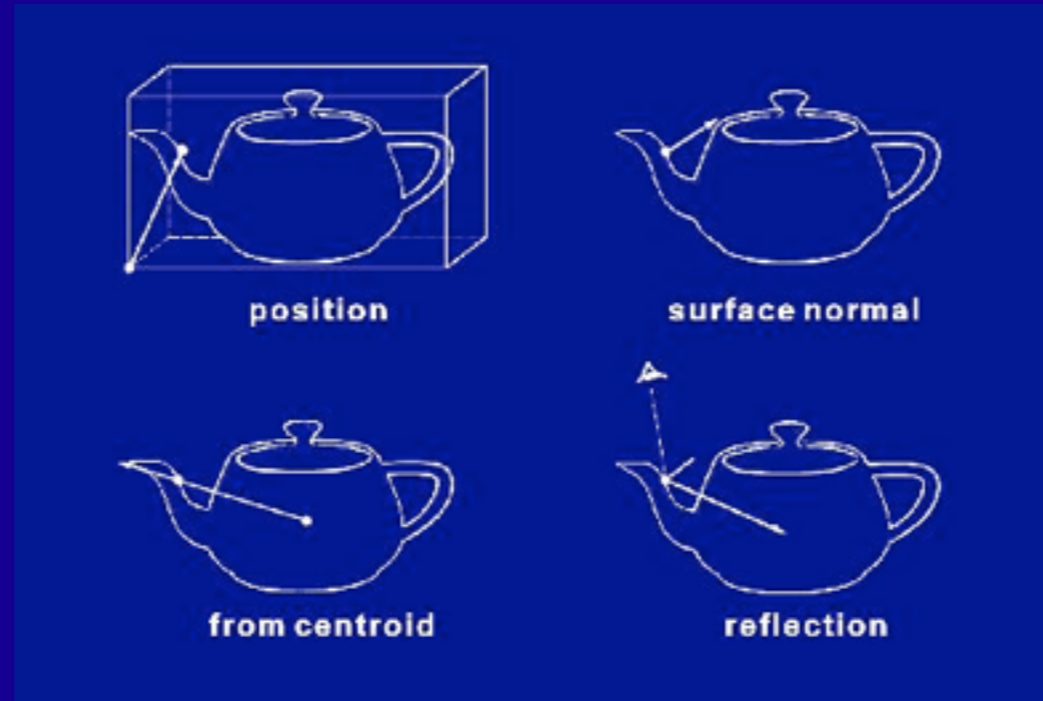
[Rosalee Wolfe]



- similar to planar mapping
- planar projection -- choose which plane to project onto

# How do we map between intermediate and actual objects?

[Rosalee Wolfe]




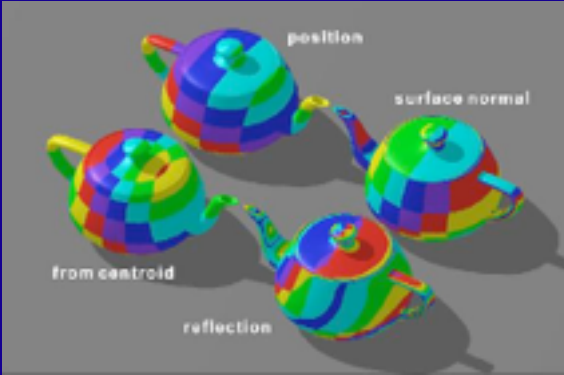
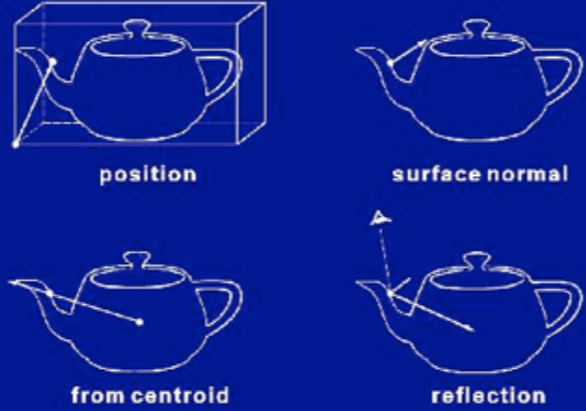
We associated  $(x,y,z)$  on the intermediate object with the texture  $(u,v)$ . But which point on the actual object is this?

We choose both the **intermediate shape** and the **mapping from the actual shape to the intermediate shape**

1. a point on the object relative to its bounding box
2. see where surface normal intersects intermediate surface
3. shoot ray from centroid through surface point to intermediate surface
4. use the reflection vector (depends on the viewer position and normal)

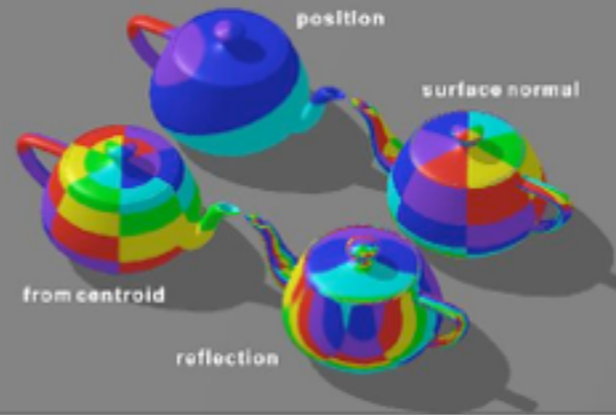
# How do we map between intermediate and actual objects?

[Rosalee Wolfe]

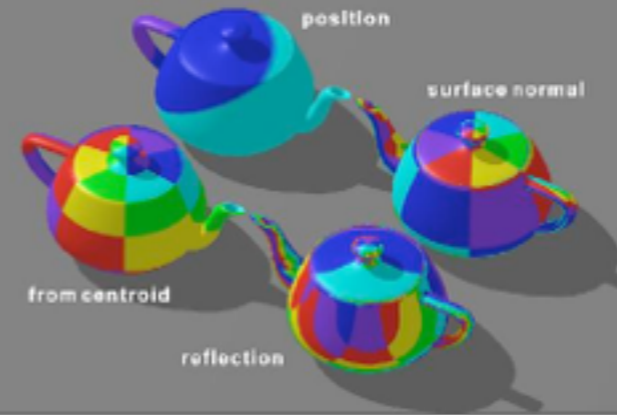


What intermediate shape was used here?

Can you tell what intermediate shape was used?  
Planar map - in xy plane

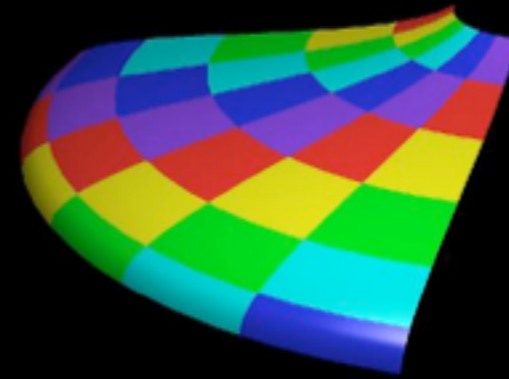
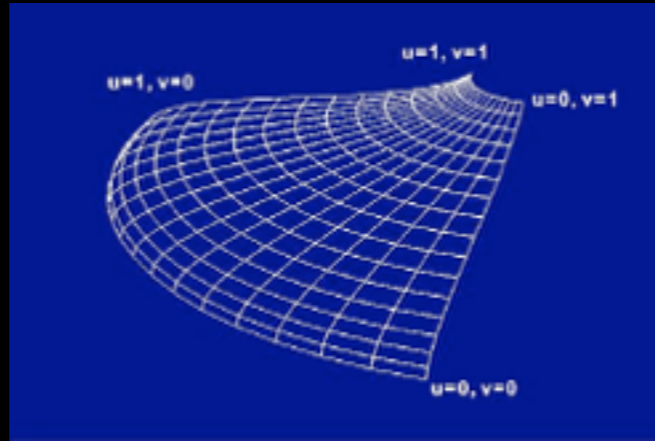


Cylindrical

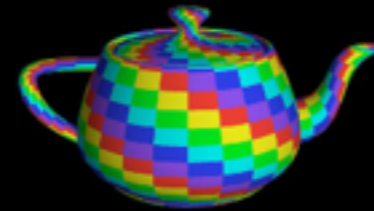


Spherical

# Parametric Surfaces



32 parametric patches



# 3D solid textures

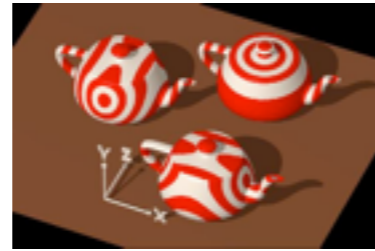
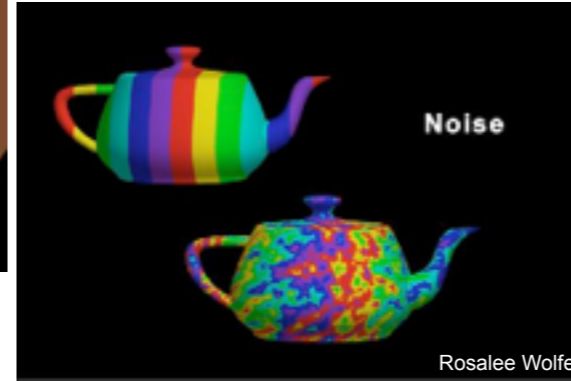
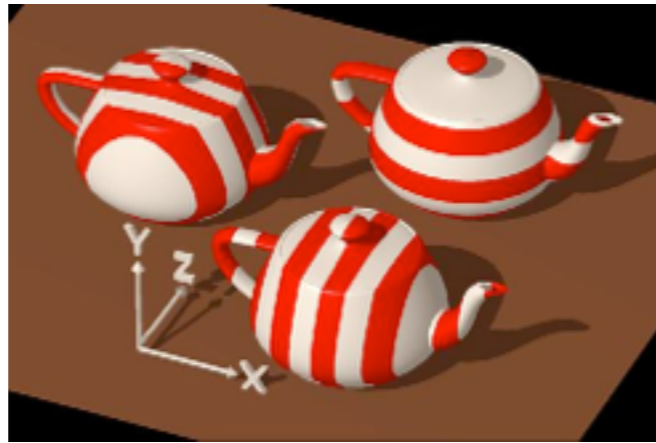


can map object  $(x,y,z)$  directly to texture  $(u,v,w)$

[Dong et al., 2008]



# Procedural textures

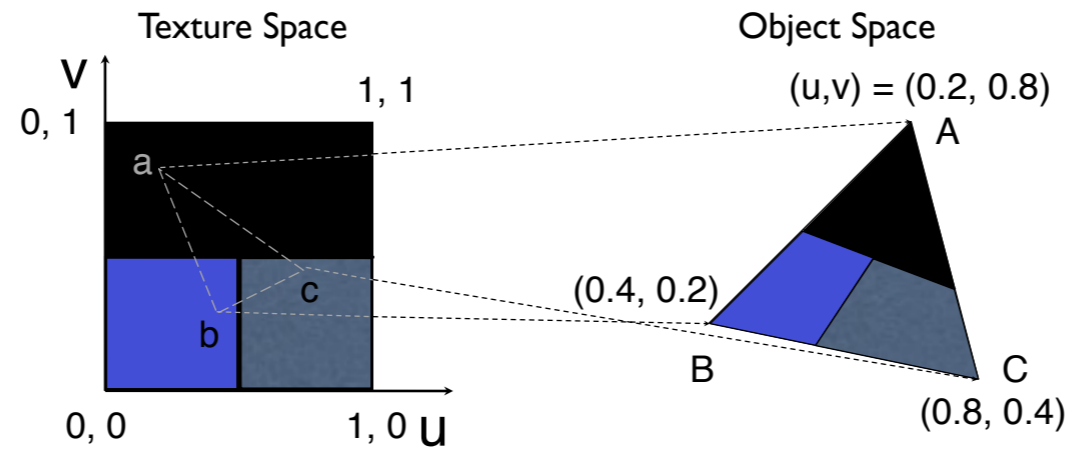


e.g., Perlin noise

# Triangles

# Texturing triangles

- Store  $(u,v)$  at each vertex
- interpolate inside triangles using barycentric coordinates



[Angel and Shreiner]

# Texturing triangles

- Store (u,v) at each vertex
- interpolate inside triangles using barycentric coordinates

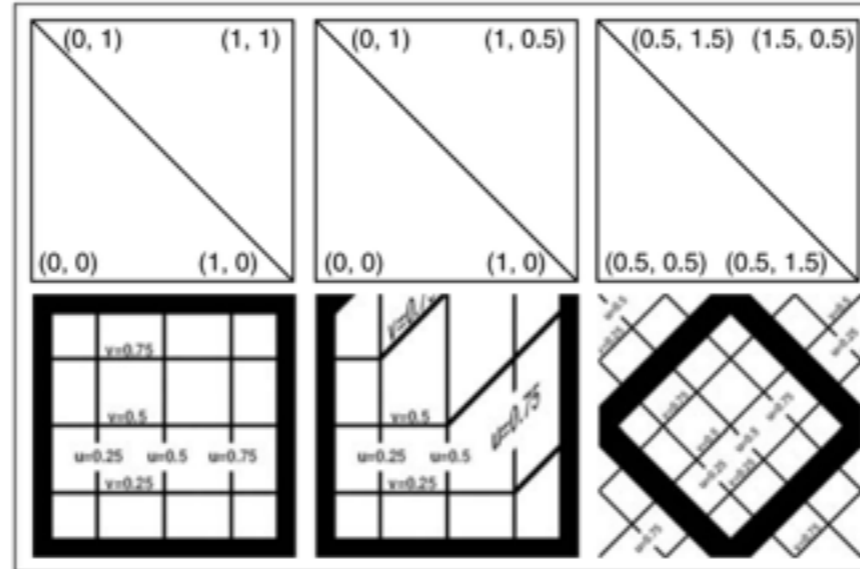
$$\mathbf{p}(\beta, \gamma) = \mathbf{a} + \beta(\mathbf{b} - \mathbf{a}) + \gamma(\mathbf{c} - \mathbf{a}).$$

$$u(\beta, \gamma) = u_a + \beta(u_b - u_a) + \gamma(u_c - u_a),$$

$$v(\beta, \gamma) = v_a + \beta(v_b - v_a) + \gamma(v_c - v_a).$$

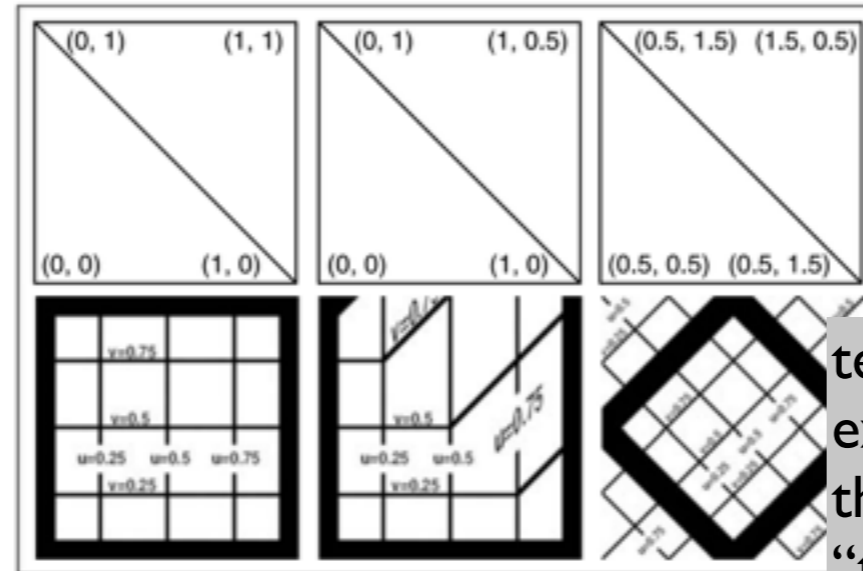
# Texturing triangles

Choice of  $(u,v)$  makes big difference



# Texturing triangles

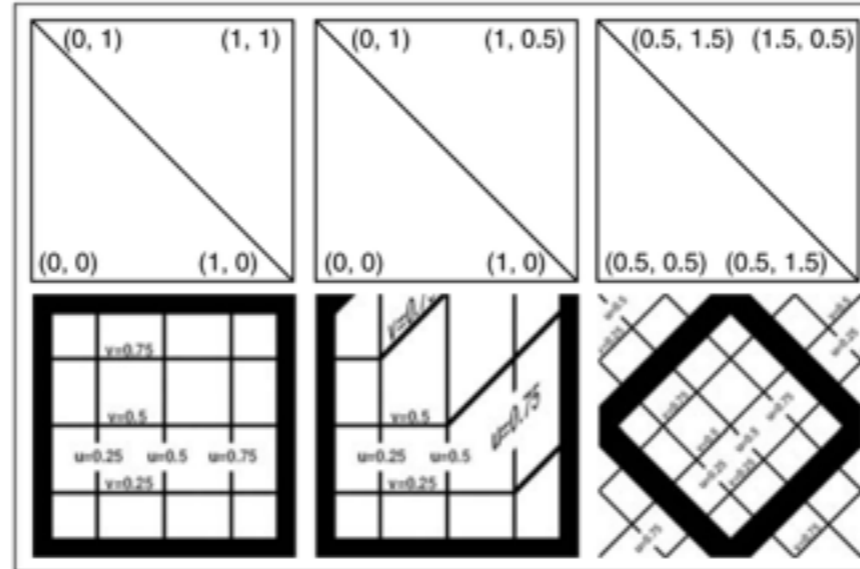
Choice of  $(u,v)$  makes big difference



texture  
extended  
through  
“tiling”

# Texturing triangles

Choice of  $(u,v)$  makes big difference



# Textures in OpenGL

- Assign (u,v) to vertices
- OpenGL then uses interpolation for triangle interior

```
glTexCoord* ()
```



good selection  
of tex coordinates



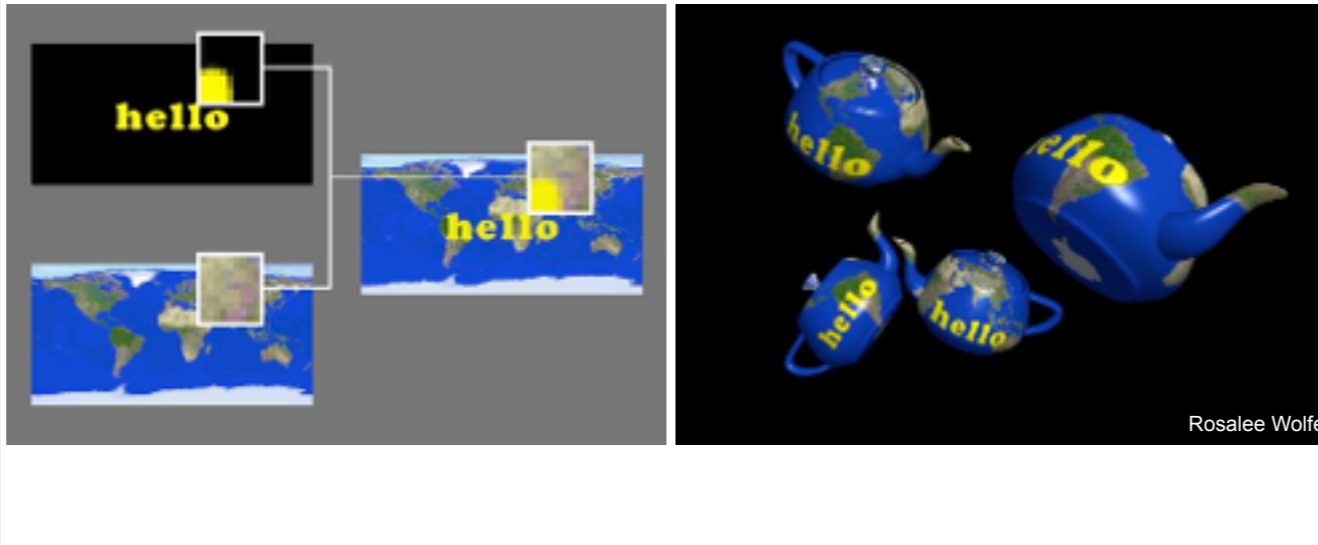
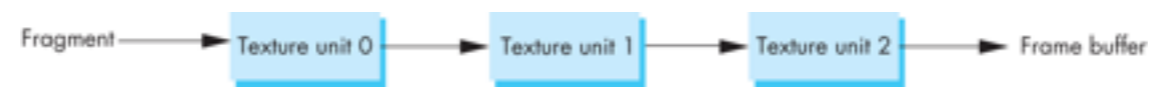
poor selection  
of tex coordinates



texture stretched  
over trapezoid  
showing effects of  
bilinear interpolation

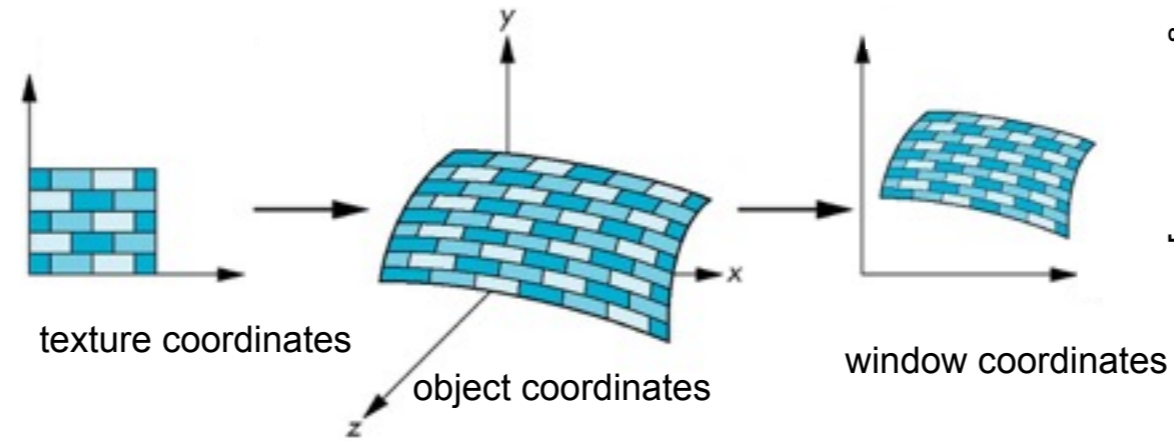
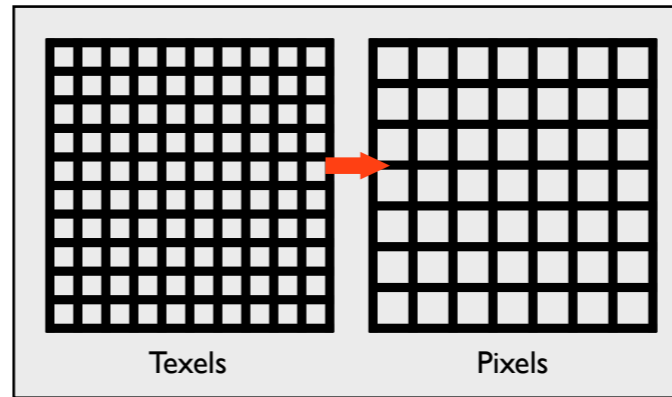


# Multitexturing



# Texture Sampling

# Texture Mapping

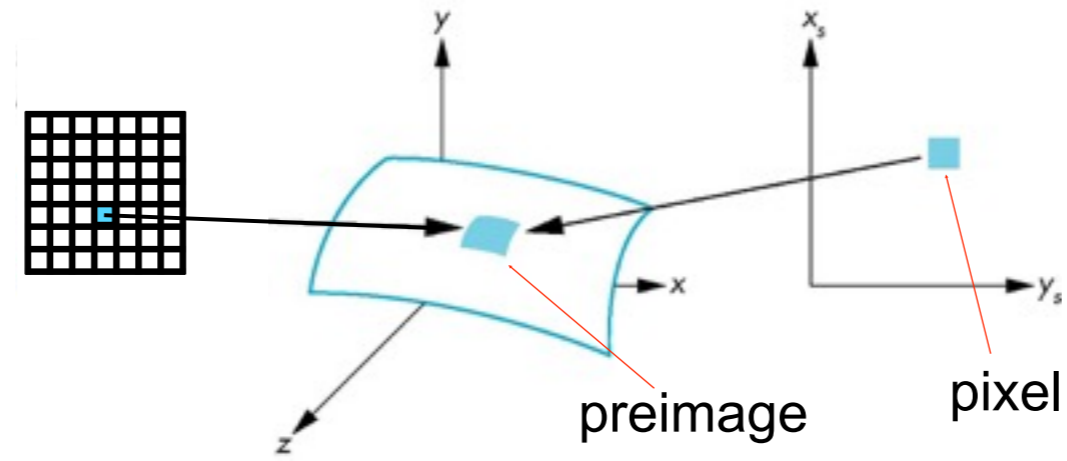


[Angel and Shreiner]

- Texture coordinates: Used to identify points in the image to be mapped
- Object Coordinates: Conceptually, where the mapping takes place
- Window Coordinates: Where the final image is really produced

# Point Sampling

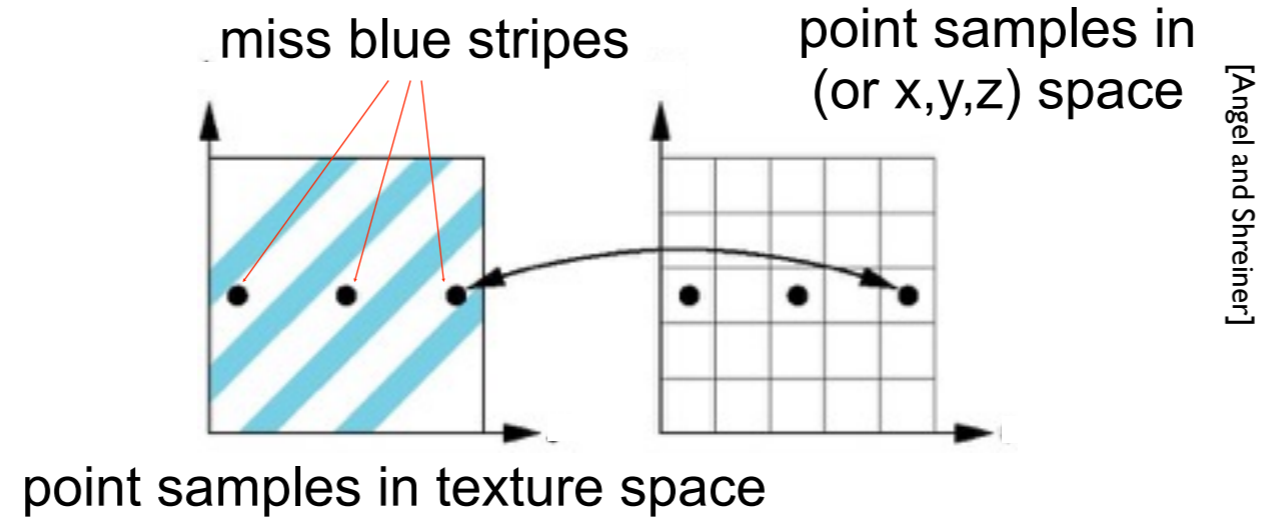
Map back to texture image and use the **nearest texel**



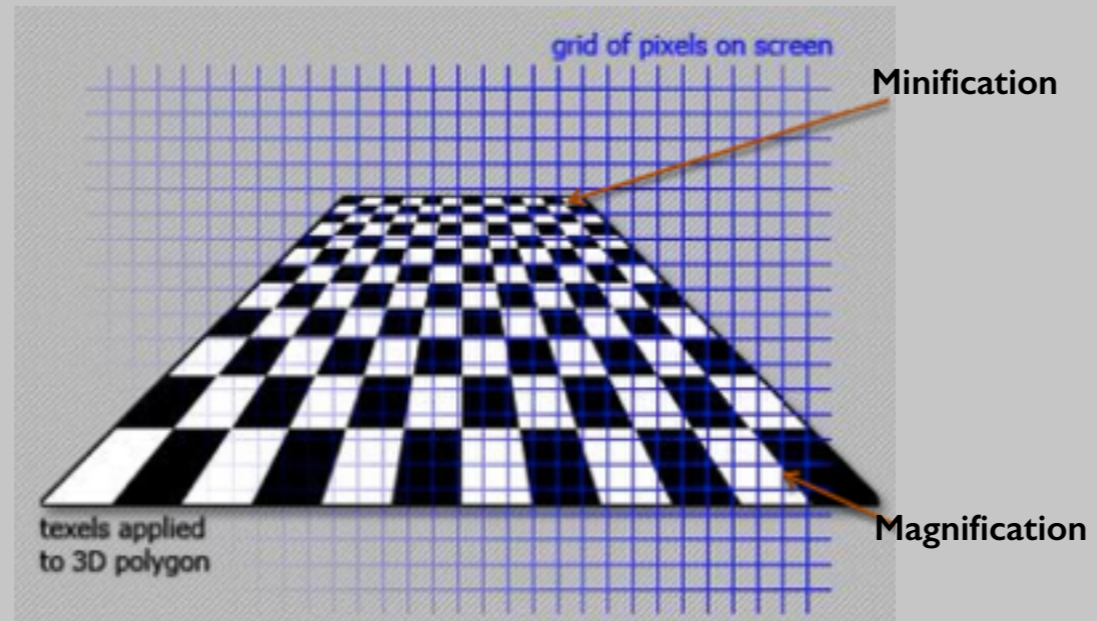
[Angel and Shreiner]

# Aliasing

**Point sampling** of the texture can lead to aliasing artifacts



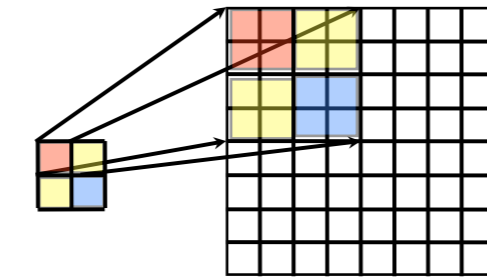
# Magnification and Minification



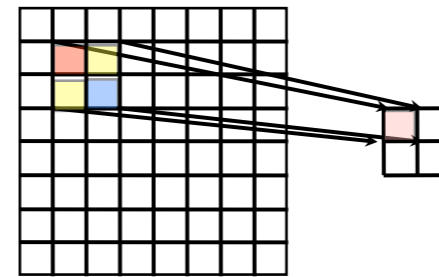
# Magnification and Minification

More than one texel can cover a pixel (*minification*) or more than one pixel can cover a texel (*magnification*)

Can use point sampling (nearest texel) or linear filtering (2 x 2 filter) to obtain texture values

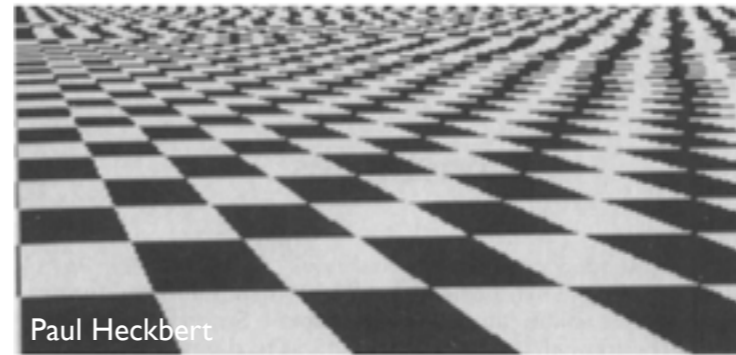


Texture  
Magnification  
Pixels

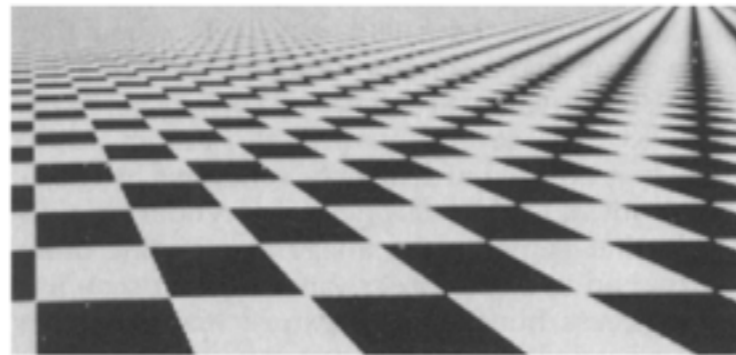


Texture  
Minification  
Pixels

# Aliasing artifacts



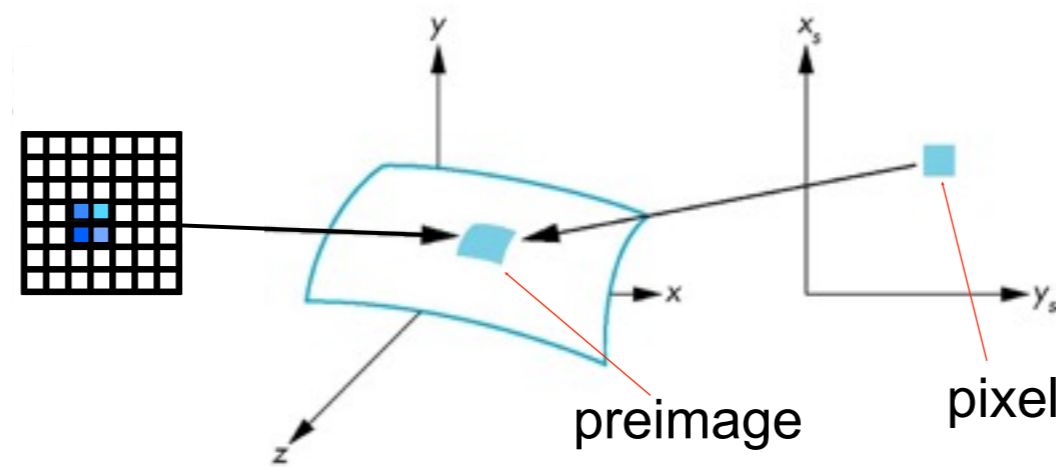
We apply **filtering** to  
reduce aliasing  
artifacts





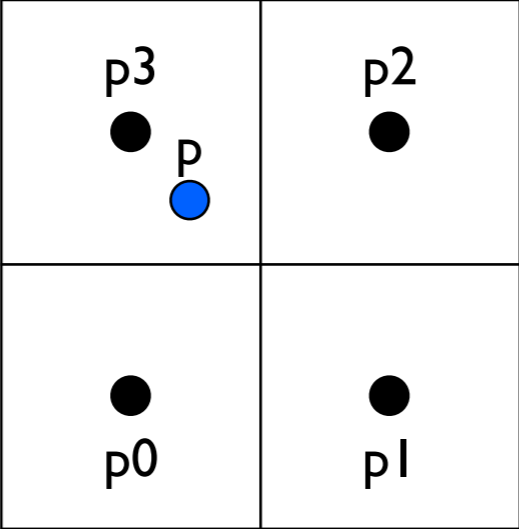
# Area Averaging

A better but slower option is to use **area averaging**



[Angel and Shreiner]

# Use bilinear filtering



$p = ?$



nearest neighbor

bilinear

Wikipedia  
bicubic

mitigate magnification artifacts

smooths out the texture – no sharp boundaries

# Mipmapping



Togikun, Wikimedia Commons

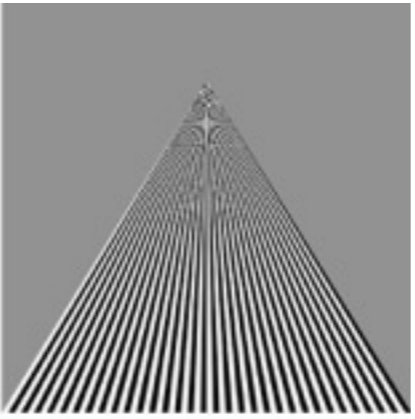
128×128, 64×64, 32×32, 16×16, 8×8, 4×4, 2×2, 1×1

Reduce minification artifacts

Pre-filter the texture to obtain reduced resolutions

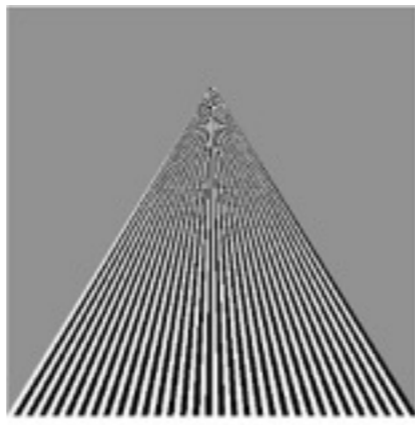
Requires 1/3 more space

Get a texture hierarchy indexed by level

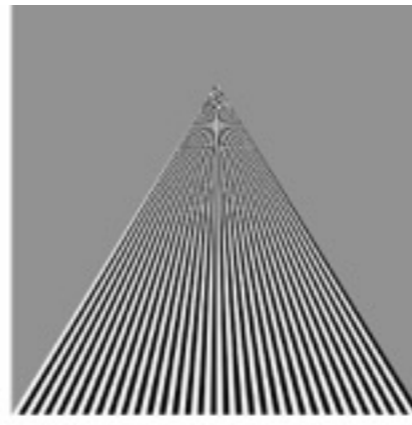


[Angel and Shreiner]

point  
sampling

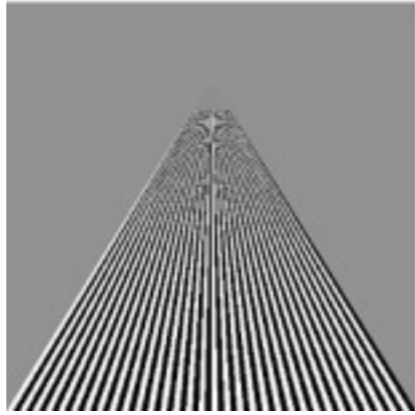


linear  
filtering



[Angel and Shreiner]

mipmapped  
point  
sampling



mipmapped  
linear  
filtering

