## CSI 30 : Computer Graphics

Lecture 7:Viewing Transformations (cont.)
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## Viewing Transformations



## Viewing transformations



- Move objects from their 3D locations to their positions in a 2 D view



## Decomposition of viewing transforms



Viewing transforms depend on: camera position and orientation, type of projection, field of view, image resolution
there are several names for these spaces: "camera space" = "eye space", "canonical view volume" = "clip space"= "normalized device coordinates", "screen space=pixel coordinates"
and for the transforms: "camera transformation" = "viewing transformation"

## Viewport transform



## Viewport transform



## Orthographic Projection Transform



## Camera Transform



## Camera Transform

How do we specify the camera configuration?

## Camera Transform

How do we specify the camera configuration? $\begin{gathered}\text { eye } \\ \text { position }\end{gathered}$


## Camera Transform

How do we specify the camera configuration? | gaze |
| :---: |
| direction |



## Camera Transform

How do we specify the camera configuration? $\begin{gathered}\text { up } \\ \text { vector }\end{gathered}$


## Camera Transform

How do we specify the camera configuration?


## Camera Transform



## Perspective Viewing


rigid - translation and rotation only - parallel lines and angles are preserved affine - scaling, shear, translation, rotation - parallel lines preserved, angles not preserved projective - parallel lines and angles not preserved

## Projective Transformations


note that the height, $y^{\prime}$, in camera space is proportional to y and inversely proportion to z . We want to be able to specify such a transformation with our $4 \times 4$ matrix machinery

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## Projective Transformations



Note: this makes our homogeneous representation for points unique only up to a constant

## Projective Transformations



## Perspective Projection



both $x$ and $y$ get multiplied by $\mathrm{d} / \mathrm{z}$

## Simple perspective projection

$$
\left(\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 1 / d & 0
\end{array}\right)\left(\begin{array}{l}
x \\
y \\
z \\
1
\end{array}\right)=\left(\begin{array}{c}
x \\
y \\
z \\
z / d
\end{array}\right) \Rightarrow\left\{\begin{array}{l}
x^{\prime}=\frac{d}{z} x \\
y^{\prime}=\frac{d}{z} y \\
z^{\prime}=\frac{d}{z} z=d
\end{array}\right.
$$

This achieves a simple perspective projection onto the view plane $z=d$
but we've lost all information about z !
<whiteboard>

This simple projection matrix won't suffice. We need to preserve z information for later hidden surface removal. whiteboard: derive $P$

## Perspective Projection

The perspective transformation does not preserve $\mathbf{z}$ completely, but it preserves $\mathbf{z}=\mathbf{n}, \mathbf{f}$ and is monotone (preserves ordering) with respect to z



So far we've mapped the view frustum to a rectangular box. This rectangular box has the same near face as the view frustum. The far face has been mapped down to the far face of the box. This mapping is given by P. The bottom figure shows how lines in the view frustum get mapped to the rect. box.


We're not quite done yet thought, because the projection transform should map the view frustum to the canonical view volume.


We need a second mapping to get our points into the canonical view volume. This second mapping is a mapping from one box to another. So it's given by an orthographic mapping, M_orth. The final perspective transformation is the composition of P and M_orth.

## OpenGL Perspective Viewing

## glFrustum (xmin,xmax,ymin,ymax, near,far)



Here's how you set up a perspective view in OpenGL. Note that near and far are both negative, but you pass their absolute values to OpenGL.

## Using Field of View

With glFrustum it is often difficult to get the desired view gluPerpective (fovy, aspect, near, far) often provides a better interface



Clipping after the
perspective transformation can cause problems


