

Example. Express the Boolean function $F = x + yz$ as a sum of minterms.

Solution:

$$\begin{aligned}
 F &= x + yz = x + (yz) && \text{AND (multiply) has a higher precedence than OR (add)} \\
 &= x(y+y')(z+z') + (x+x')yz && \text{expand 1}^{\text{st}} \text{ term by ANDing it with } (y + y')(z + z'), \text{ and 2}^{\text{nd}} \text{ term with } (x + x') \\
 &= xy z + xy z' + x y' z + x y' z' + \cancel{x y z} + x' y z \\
 &= m_7 + m_6 + m_5 + m_4 + m_3 \\
 &= \Sigma(3, 4, 5, 6, 7) && \text{sum of 1-minterms}
 \end{aligned}$$

Example. Express the Boolean function $F = x + yz$ as a product of maxterms.

Solution: First, we need to convert the function into the product-of-OR terms by using the distributive law as follows:

$$\begin{aligned}
 F &= x + yz = x + (yz) && \text{AND (multiply) has a higher precedence than OR (add)} \\
 &= (x + y)(x + z) && \text{use distributive law to change to product of OR terms} \\
 &= (x + y + z z')(x + y y' + z) && \text{expand 1}^{\text{st}} \text{ term by ORing it with } z z', \text{ and 2}^{\text{nd}} \text{ term with } y y' \\
 &= (x + y + z)(x + y + z')(\cancel{x + y + z}) && (x + y + z) \\
 &= M_0 \bullet M_1 \bullet M_2 \\
 &= \Pi(0, 1, 2) && \text{product of 0-maxterms}
 \end{aligned}$$

Example. Express $F' = (x + yz)'$ as a sum of minterms.

Solution:

$$\begin{aligned}
 F' &= (x + yz)' = (x + (yz))' && \text{AND (multiply) has a higher precedence than OR (add)} \\
 &= x'(y' + z') && \text{use dual or De Morgan's Law} \\
 &= (x' y') + (x' z') && \text{use distributive law to change to sum of AND terms} \\
 &= x' y' (z + z') + x' (y + y') z' && \text{expand 1}^{\text{st}} \text{ term by ANDing it with } (z + z'), \text{ and 2}^{\text{nd}} \text{ term with } (y + y') \\
 &= x' y' z + x' y' z' + x' y z' + \cancel{x' y' z'} \\
 &= m_1 + m_0 + m_2 \\
 &= \Sigma(0, 1, 2) && \text{sum of 0-minterms}
 \end{aligned}$$

Example. Express $F' = (x + yz)'$ as a product of maxterms.

Solution:

$$\begin{aligned}
 F' &= (x + yz)' = (x + (yz))' && \text{AND (multiply) has a higher precedence than OR (add)} \\
 &= x'(y' + z') && \text{use dual or De Morgan's Law} \\
 &= (x' + y y' + z z')(x' + y' + z') && \text{expand 1}^{\text{st}} \text{ term by ORing it with } y y' \text{ and } z z', \text{ and 2}^{\text{nd}} \text{ term with } x x' \\
 &= (x' + y + z)(x' + y + z')(x' + y' + z)(x' + y' + z')(x' + y' + z')(\cancel{x' + y' + z'}) \\
 &= M_4 \bullet M_6 \bullet M_5 \bullet M_7 \bullet M_3 \\
 &= \Pi(3, 4, 5, 6, 7) && \text{product of 1-maxterms}
 \end{aligned}$$

F and F' are shown in the following truth table:

x	y	z	Minterms	Maxterms	F	F'
0	0	0	$m_0 = x' y' z'$	$M_0 = x + y + z$	0	1
0	0	1	$m_1 = x' y' z$	$M_1 = x + y + z'$	0	1
0	1	0	$m_2 = x' y z'$	$M_2 = x + y' + z$	0	1
0	1	1	$m_3 = x' y z$	$M_3 = x + y' + z'$	1	0
1	0	0	$m_4 = x y' z'$	$M_4 = x' + y + z$	1	0
1	0	1	$m_5 = x y' z$	$M_5 = x' + y + z'$	1	0
1	1	0	$m_6 = x y z'$	$M_6 = x' + y' + z$	1	0
1	1	1	$m_7 = x y z$	$M_7 = x' + y' + z'$	1	0