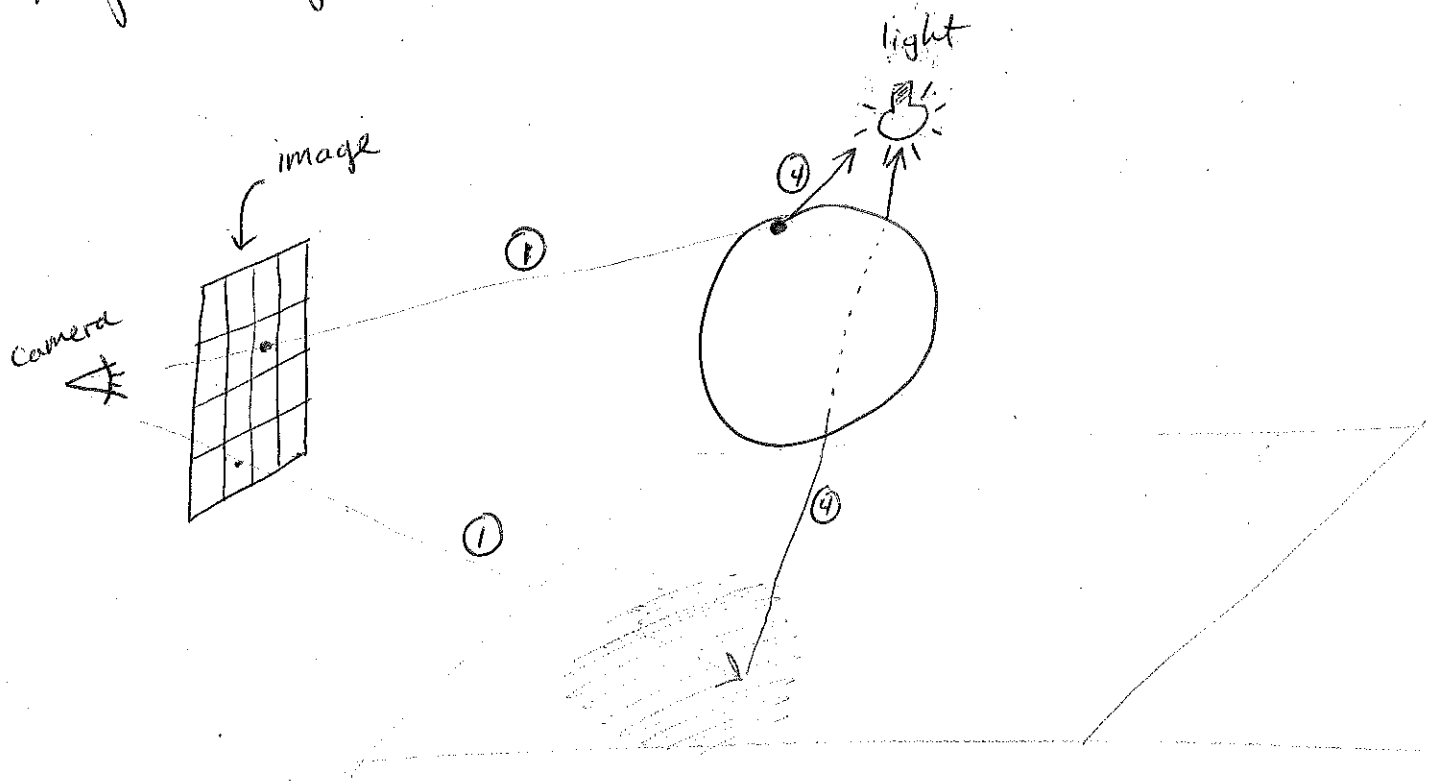


# Ray tracing



- ① for each pixel, cast a ray
- ② identify first object hit by ray
- ③ compute shading of hit object at point ray hit it
- ④ for shadows, cast ray to each light  
→ if hit object before light, ignore the light's contribution to shading

\* if ray hits nothing, use background color  
→ environment mapping, use environment map rather than background color

\* important primitive operations  
→ intersect (ray, object)  
→ shade object

Phong shading needs

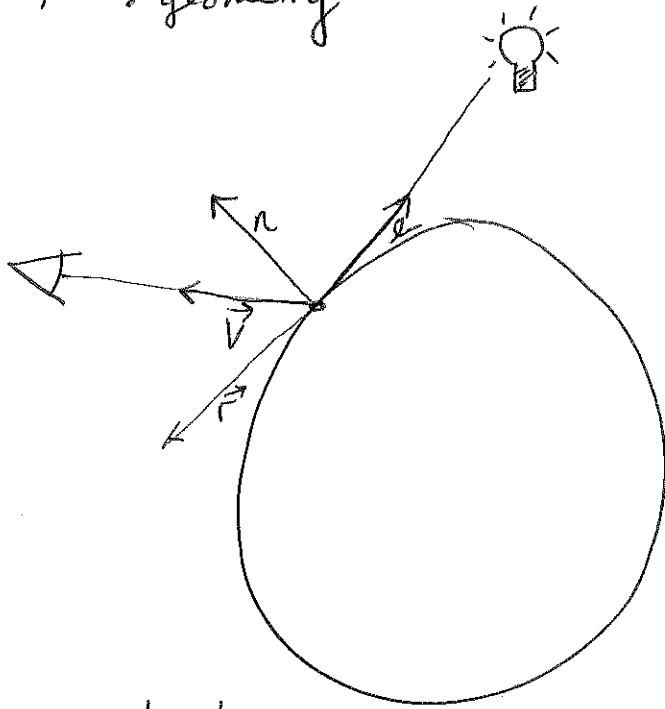
$$I = L_a R_a + L R_d (\vec{n} \cdot \vec{l}) + L R_s (\vec{r} \cdot \vec{v})^e$$

inputs:  $L_a, L$  → from lights

$R_d, R_s, e$  → from shader (material properties)

↳ objects have shaders to describe their appearance

$\vec{l}, \vec{n}, \vec{r}, \vec{v}$  : geometry



$\vec{n}$ : object can compute this given intersection location

$\vec{v}$ : from camera and intersection locations

$\vec{l}$ : from light and intersection locations

$\vec{r}$ : from  $\vec{n}$  and  $\vec{l}$

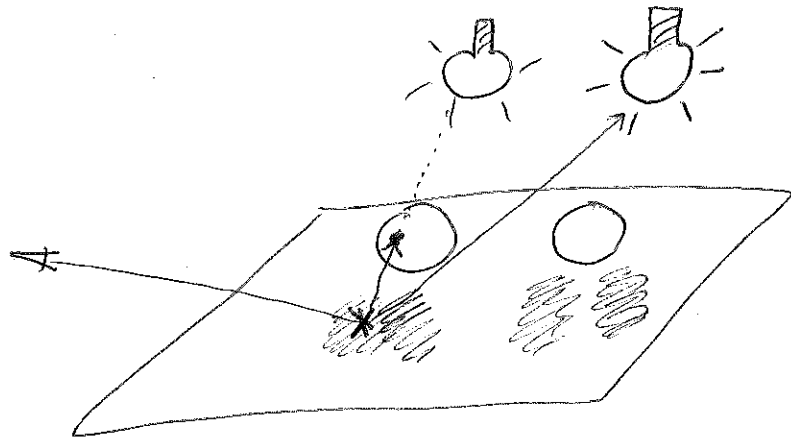
## Lights

note that  $L$ ,  $L_a$ ,  $\vec{l}$  are per light

compute for each light, sum  
shading

## Shadows

is light visible? cast ray to light and see (reuse existing routine)



## Other types of shaders

Flat shader  $\rightarrow$  fixed color (ignore lights)

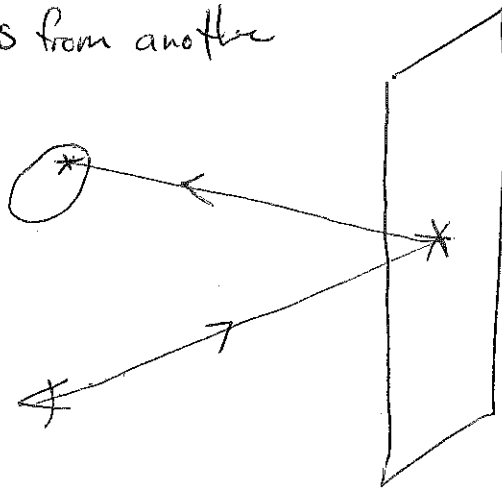
good for debugging but little else

# Reflective Shader

Shiny surface

~~light reflects from object~~

light from one object reflects from another  
and reaches you  
→ indirect light



\* Cast a new ray from  
intersection point in  
reflection direction

\* reflectivity  $\beta$   $0 \leq \beta \leq 1$

\* surface shade

↳ surface appearance ignoring reflection  $\Rightarrow I_0$

\* color from reflected ray  $\Rightarrow I_r$

\* effective color  $\Rightarrow I_0 + \beta(I_r - I_0)$

note:  $\beta=0 \Rightarrow I=I_0$

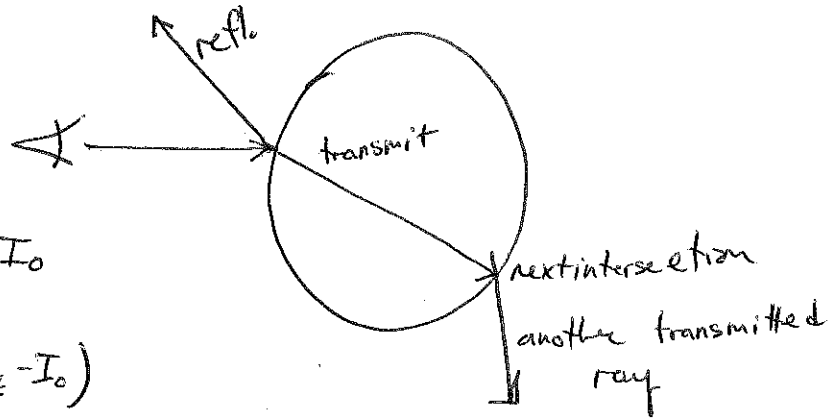
$\beta=1 \Rightarrow I=I_r$

# Transmission

\* Cast two rays

→ reflected ray  $\Rightarrow I_r$

→ transmitted ray  $I_t$



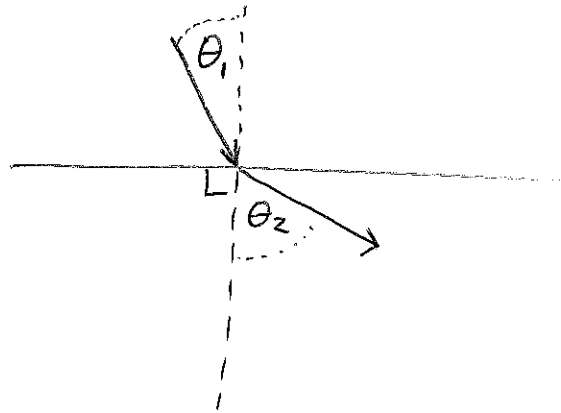
\* combine with object shade  $I_o$

$$I = I_o + \beta(I_r - I_o) + \gamma(I_t - I_o)$$

$$\beta + \gamma \leq 1$$

\* direction of transmitted ray given by snell's law

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_1}{n_2}$$



$n_1, n_2$  index of refraction

air:  $n \approx 1.00$

glass:  $n \approx 1.46$

water:  $n \approx 1.33$

vacuum:  $n = 1$

diamond:  $n \approx 2.42$

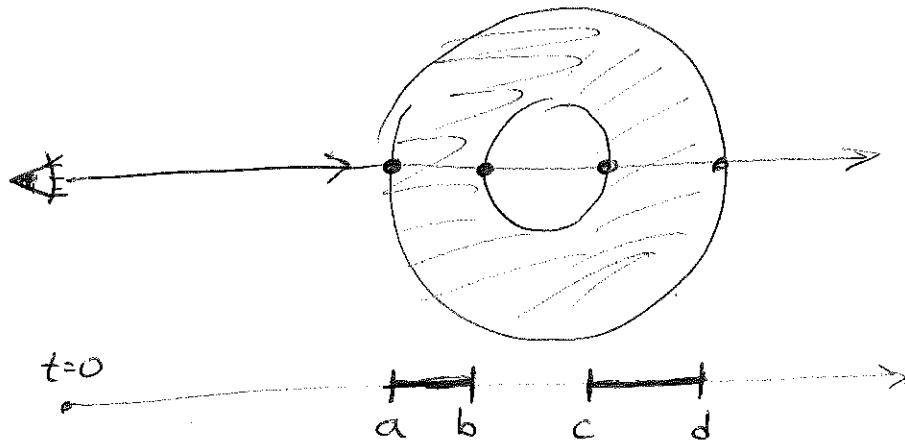
$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

\* what if  $\sin \theta_2 > 1$ ?

↳ complete internal reflection

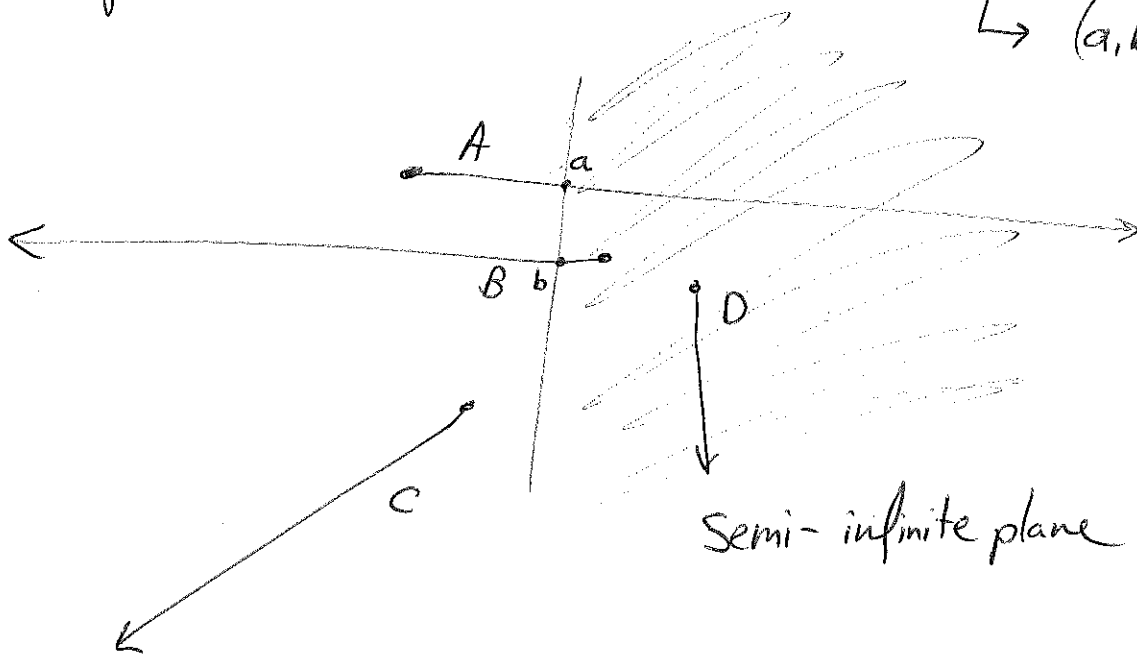
$$\gamma = 0$$

# Intersections



ray intersects object for  $t \in [a, b]$  and  $t \in [c, d]$

$\hookrightarrow (a, b, c, d)$



$$A \rightarrow [a, \infty) \rightarrow (a)$$

$$B \rightarrow [0, b] \rightarrow (0, b)$$

$$C \rightarrow \emptyset \rightarrow ()$$

$$D \rightarrow [0, \infty) \rightarrow (0)$$

# Intersections II

why not just store first intersection?

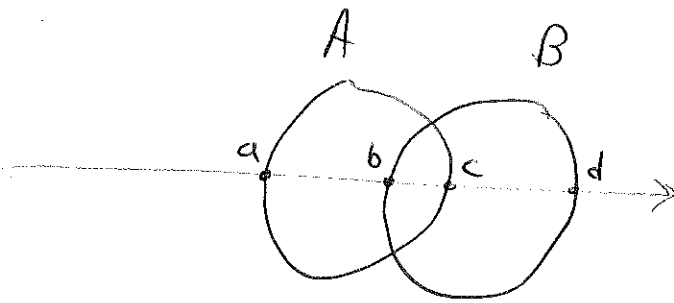
→ booleans

first hit on  $A = a$

first hit on  $B = b$

first hit on  $B-A = c$

$c$  cannot be deduced from  $a$  or  $b$



$B-A$

