Name:

Student ID #:

- You are expected to work on this assignment on your own
- Use pseudocode, Python-like or English to describe your algorithms. Absolutely no C++/C/Java
- When designing an algorithm, you are allowed to use any algorithm or data structure we explained in class, without giving its details, unless the question specifically requires that you give such details
- Always remember to analyze the time complexity of your algorithms
- Homework has to be submitted electronically on Gradescope by the deadline. No late assignments will be accepted
Problem 1. (10 points)

- Go to Gradescope (https://gradescope.com/ or follow the link from the class CS 141 webpage) and sign up using the entry code MZR34G; once you have completed this homework, submit the PDF via Gradescope by October 9th, 2017, 11:59pm

- Go to the Piazza discussion board (https://piazza.com/ucr/fall2017/cs141/ or follow the link from the class CS 141 webpage), register yourself, then select hw1 from the top menu and post a short message to introduce yourself.

Answer:
Problem 2. (20 points)

Analyze the worst-case time complexity of the following method, and give a tight bound using the big-theta notation.

Algorithm WeirdLoop \((n : \text{integer})\)
\[
\text{for } i \leftarrow 1 \text{ to } n \log n \text{ do }
\]
\[
\quad j \leftarrow i
\]
\[
\quad \text{while } j \leq n \text{ do }
\]
\[
\quad \quad \text{“loop body”}
\]
\[
\quad \quad j \leftarrow j + 1
\]

assuming that “loop body” takes \(\Theta(1)\) time.

Answer:
Problem 3. (20 points) Order the following list of functions by the big-Oh notation, i.e., rank them by order of growth. Group together (for example, by underlining) those functions that are big-Theta of one another. Logarithms are base two unless indicated otherwise.

\[
\begin{array}{cccccccc}
3n + 2 & n^3 + n^2 & \log^2 n & \log \log n & 2^{2^n} & 4^{n-1} \\
2^{\log n} & 2\sqrt{2^{\log n}} & \sqrt{n} & n^3 & 1 & 3^{n/3} \\
10000n^2 & 2^{2^{n+1}} & e^n & n^{\log \log n} & \log n & (\log n)^2 \\
2^n & n3^n & 4^{\log n} & 4n^2/\sqrt{n} & \sqrt{\log n} & n \log n \\
\end{array}
\]

Answer:
Problem 4. (50 points)

You are facing a high wall that stretches infinitely in both directions. There is a door in the wall, but you don’t know how far away or in which direction. It is pitch dark, but you have a very dim lighted candle that will enable you to see the door when you are right next to it. Show that there is an algorithm that enables you to find the door by walking at most \( O(n) \) steps, where \( n \) is the number of steps that you would have taken if you knew where the door is and walked directly to it. What is the constant multiple in the big-O bound for your algorithm?

Answer: