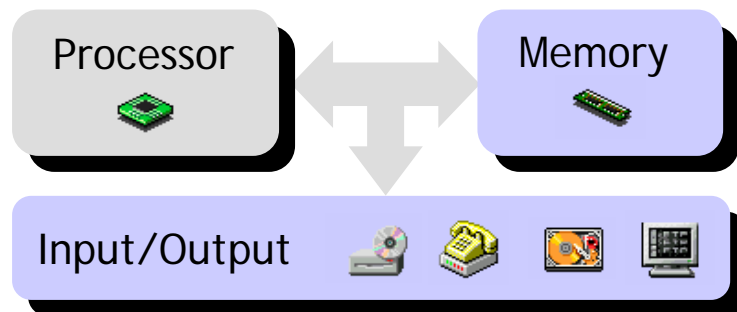


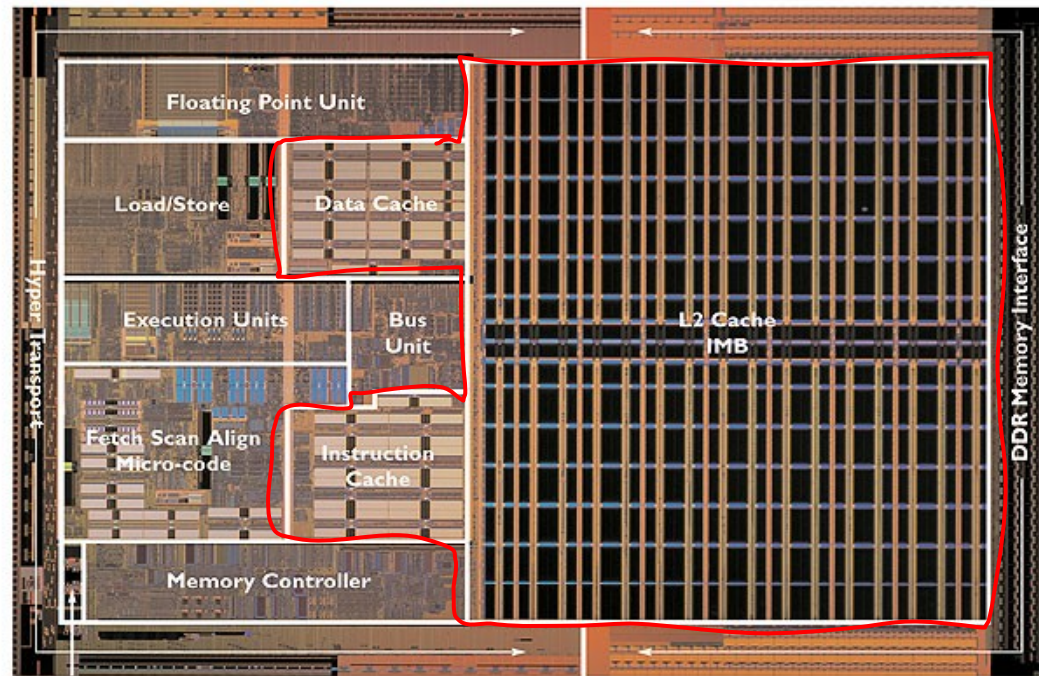
Welcome to Part 3: Memory Systems and I/O

- ❑ We've already seen how to make a fast processor. How can we supply the CPU with enough data to keep it busy?
- ❑ We will now focus on **memory** issues, which are frequently bottlenecks that limit the performance of a system.
- ❑ We'll start off by looking at memory systems for the next two weeks.



Cache introduction

- Today we'll answer the following questions.
 - What are the challenges of building big, fast memory systems?
 - What is a cache?
 - Why caches work? (answer: locality)
 - How are caches organized?
 - Where do we put things -and- how do we find them?



Large and fast

- ❑ Today's computers depend upon large and fast storage systems.
 - **Large** storage capacities are needed for many database applications, scientific computations with large data sets, video and music, and so forth.
 - **Speed** is important to keep up with our pipelined CPUs, which may access both an instruction and data in the same clock cycle. Things get even worse if we move to a superscalar CPU design.
- ❑ So far we've assumed our memories can keep up and our CPU can access memory in one cycle, but as we'll see that's a simplification.



Small or slow

- ❑ Unfortunately there is a tradeoff between speed, cost and capacity.

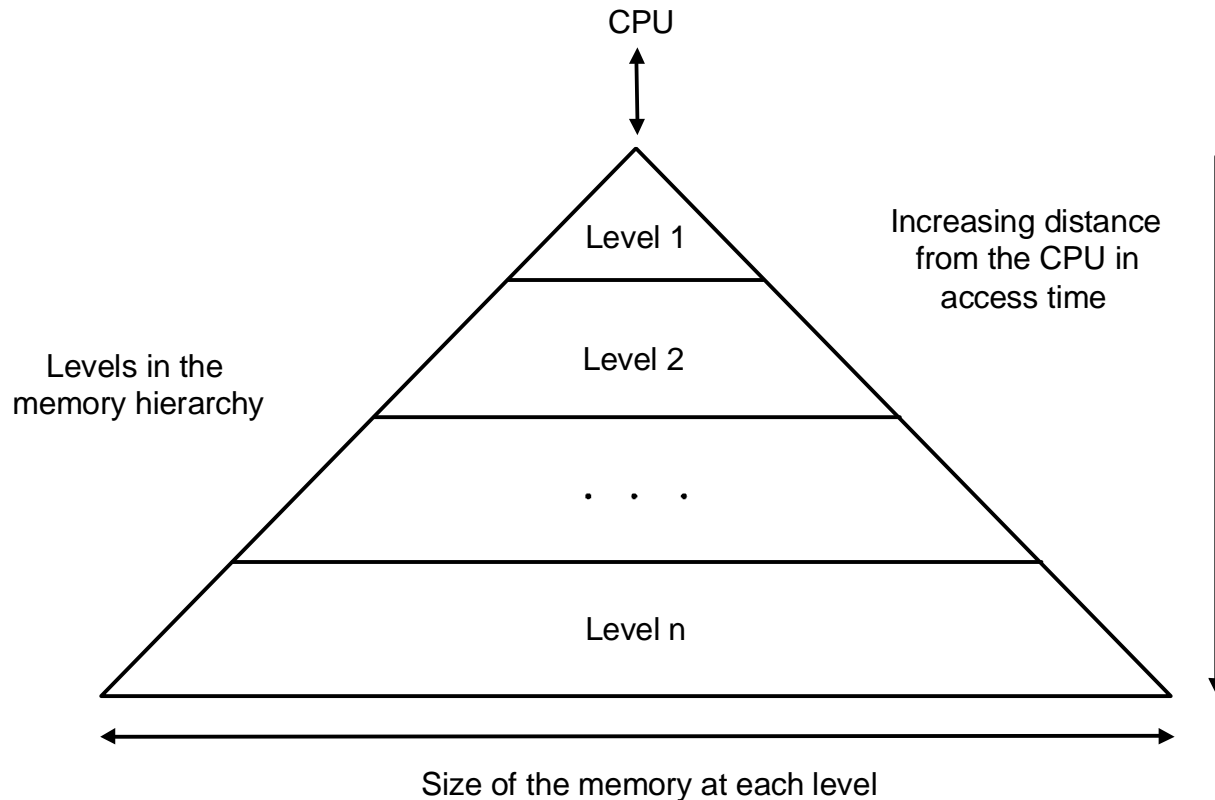
Storage	Speed	Cost	Capacity
Static RAM	Fastest	Expensive	Smallest
Dynamic RAM	Slow	Cheap	Large
Hard disks	Slowest	Cheapest	Largest

- ❑ Fast memory is too expensive for most people to buy a lot of.
- ❑ But dynamic memory has a much longer delay than other functional units in a datapath. If every lw or sw accessed dynamic memory, we'd have to either increase the cycle time or stall frequently.
- ❑ Here are rough estimates of some current storage parameters.

Storage	Delay	Cost/MB	Capacity
Static RAM	1-10 cycles	~\$10	128KB-2MB
Dynamic RAM	100-200 cycles	~\$0.20	128MB-4GB
Hard disks	10,000,000 cycles	~\$0.001	20GB-200GB

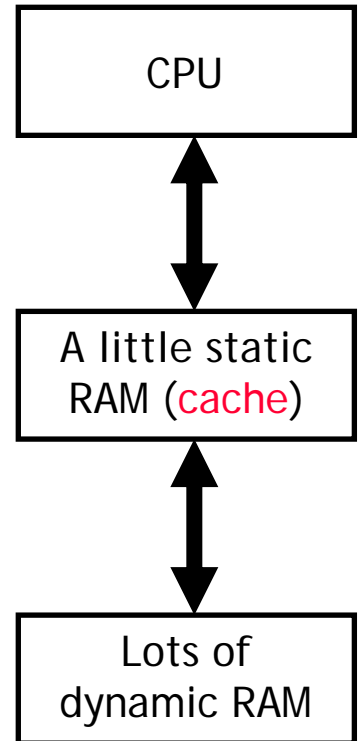
How to Create the Illusion of Big and Fast

- ❑ Memory hierarchy – put small and fast memories closer to CPU, large and slow memories further away



Introducing caches

- ❑ Introducing a **cache** – a small amount of fast, expensive memory.
 - The cache goes between the processor and the slower, dynamic main memory.
 - It keeps a copy of the most frequently used data from the main memory.
- ❑ Memory access speed increases overall, because we've made the common case faster.
 - Reads and writes to the most frequently used addresses will be serviced by the cache.
 - We only need to access the slower main memory for less frequently used data.



The principle of locality

- ❑ Why does the hierarchy work?

- ❑ Because most programs exhibit *locality*, which the cache can take advantage of.
 - The principle of **temporal locality** says that if a program accesses one memory address, there is a good chance that it will access the same address again.
 - The principle of **spatial locality** says that if a program accesses one memory address, there is a good chance that it will also access other nearby addresses.

Temporal locality in *instructions*

- ❑ **Loops** are excellent examples of temporal locality in programs.
 - The loop body will be executed many times.
 - The computer will need to access those same few locations of the instruction memory repeatedly.
- ❑ **For example:**

```
Loop:  lw    $t0, 0($s1)
       add  $t0, $t0, $s2
       sw   $t0, 0($s1)
       addi $s1, $s1, -4
       bne $s1, $0, Loop
```

- Each instruction will be fetched over and over again, once on every loop iteration.

Temporal locality in *data*

- ❑ Programs often access the same **variables** over and over, especially within loops. Below, **sum** and **i** are repeatedly read and written.

```
sum = 0;
for (i = 0; i < MAX; i++)
    sum = sum + f(i);
```

- ❑ Commonly-accessed variables can sometimes be kept in **registers**, but this is not always possible.
 - There are a limited number of registers.
 - There are situations where the data must be kept in memory, as is the case with shared or dynamically-allocated memory.

Spatial locality in *instructions*

```
sub  $sp, $sp, 16
sw   $ra, 0($sp)
sw   $s0, 4($sp)
sw   $a0, 8($sp)
sw   $a1, 12($sp)
```

- ❑ Nearly every program exhibits spatial locality, because instructions are usually executed **in sequence** — if we execute an instruction at memory location i , then we will probably also execute the next instruction, at memory location $i+1$.
- ❑ Code fragments such as loops exhibit *both* temporal and spatial locality.

Spatial locality in *data*

- ❑ Programs often access data that is stored contiguously.
 - Arrays, like **a** in the code on the top, are stored in memory contiguously.
 - The individual fields of a record or object like **employee** are also kept contiguously in memory.

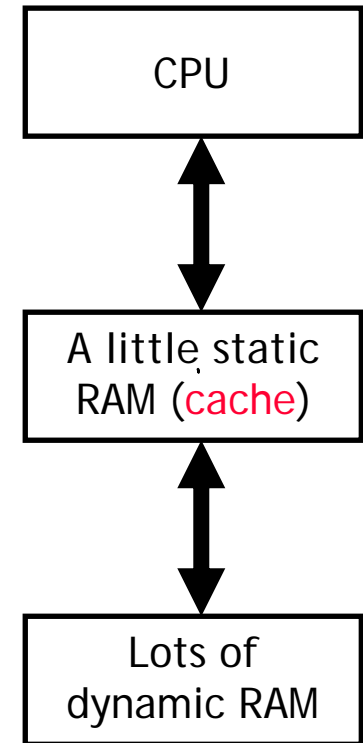
```
sum = 0;  
for (i = 0; i < MAX; i++)  
    sum = sum + a[i];
```

```
employee.name = "Homer Simpson";  
employee.boss = "Mr. Burns";  
employee.age = 45;
```



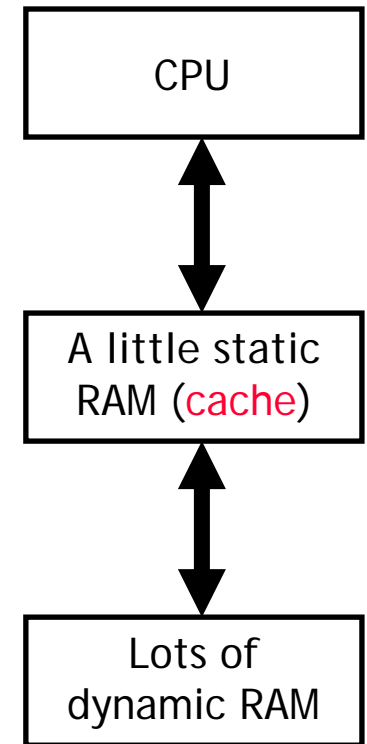
How caches take advantage of temporal locality

- ❑ The first time the processor reads from an address in main memory, a copy of that data is also stored in the cache.
 - The next time that same address is read, we can use the copy of the data in the cache *instead* of accessing the slower dynamic memory.
 - So the first read is a little slower than before since it goes through both main memory and the cache, but subsequent reads are much faster.
- ❑ This takes advantage of temporal locality—commonly accessed data is stored in the faster cache memory.



How caches take advantage of spatial locality

- ❑ When the CPU reads location i from main memory, a copy of that data is placed in the cache.
- ❑ But instead of just copying the contents of location i , we can copy **several** values into the cache at once, such as the four bytes from locations i through $i + 3$.
 - If the CPU later does need to read from locations $i + 1$, $i + 2$ or $i + 3$, it can access that data from the cache and not the slower main memory.
 - For example, instead of reading just one array element at a time, the cache might actually be loading four array elements at once.
- ❑ Again, the initial load incurs a performance penalty, but we're gambling on spatial locality and the chance that the CPU will need the extra data.

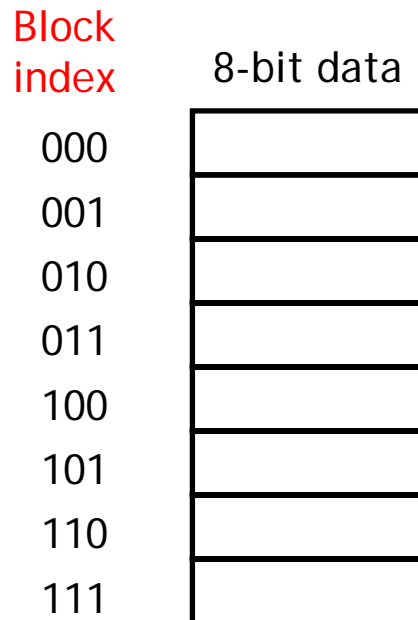


Definitions: Hits and misses

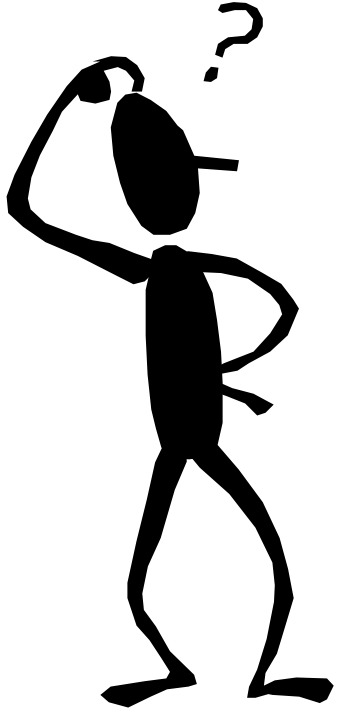
- ❑ A **cache hit** occurs if the cache contains the data that we're looking for. Hits are good, because the cache can return the data much faster than main memory.
- ❑ A **cache miss** occurs if the cache does not contain the requested data. This is bad, since the CPU must then wait for the slower main memory.
- ❑ There are two basic measurements of cache performance.
 - The **hit rate** is the percentage of memory accesses that are handled by the cache.
 - The **miss rate** ($1 - \text{hit rate}$) is the percentage of accesses that must be handled by the slower main RAM.
- ❑ Typical caches have a hit rate of 95% or higher, so in fact most memory accesses will be handled by the cache and will be dramatically faster.
- ❑ In future lectures, we'll talk more about cache performance.
 - Today we'll talk about implementation!

A simple cache design

- ❑ Caches are divided into **blocks**, which may be of various sizes.
 - The number of blocks in a cache is usually a power of 2.
 - For now we'll say that each block contains one byte. This won't take advantage of spatial locality, but we'll do that next time.
- ❑ Here is an example cache with eight blocks, each holding one byte.



Four important questions

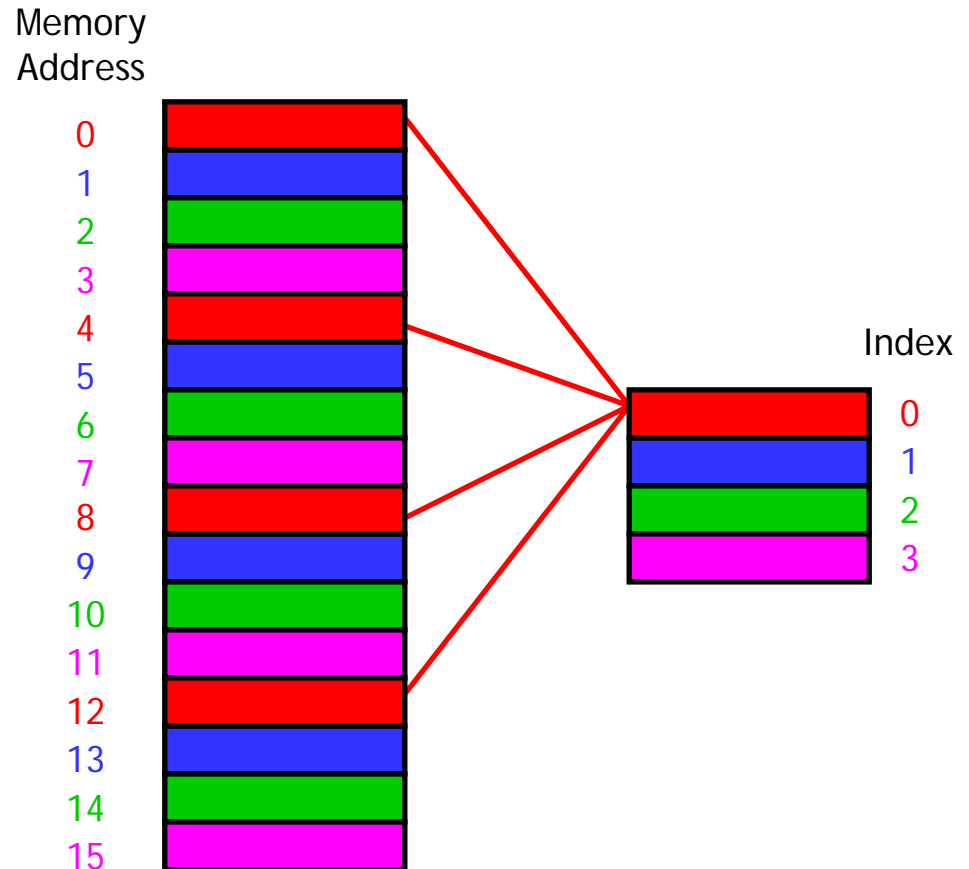


1. When we copy a block of data from main memory to the cache, **where** exactly should we put it?
2. How can we tell if a word is already in the cache, or if it has to be fetched from main memory first?
3. Eventually, the small cache memory might fill up. To load a new block from main RAM, we'd have to **replace** one of the existing blocks in the cache... which one?
4. How can **write** operations be handled by the memory system?

- Questions 1 and 2 are related—we have to know where the data is placed if we ever hope to find it again later!

Where should we put data in the cache?

- ❑ A **direct-mapped** cache is the simplest approach: each main memory address maps to exactly one cache block.
- ❑ For example, on the right is a 16-byte main memory and a 4-byte cache (four 1-byte blocks).
- ❑ Memory locations **0, 4, 8** and **12** all map to cache block **0**.
- ❑ Addresses **1, 5, 9** and **13** map to cache block **1**, etc.
- ❑ How can we compute this mapping?



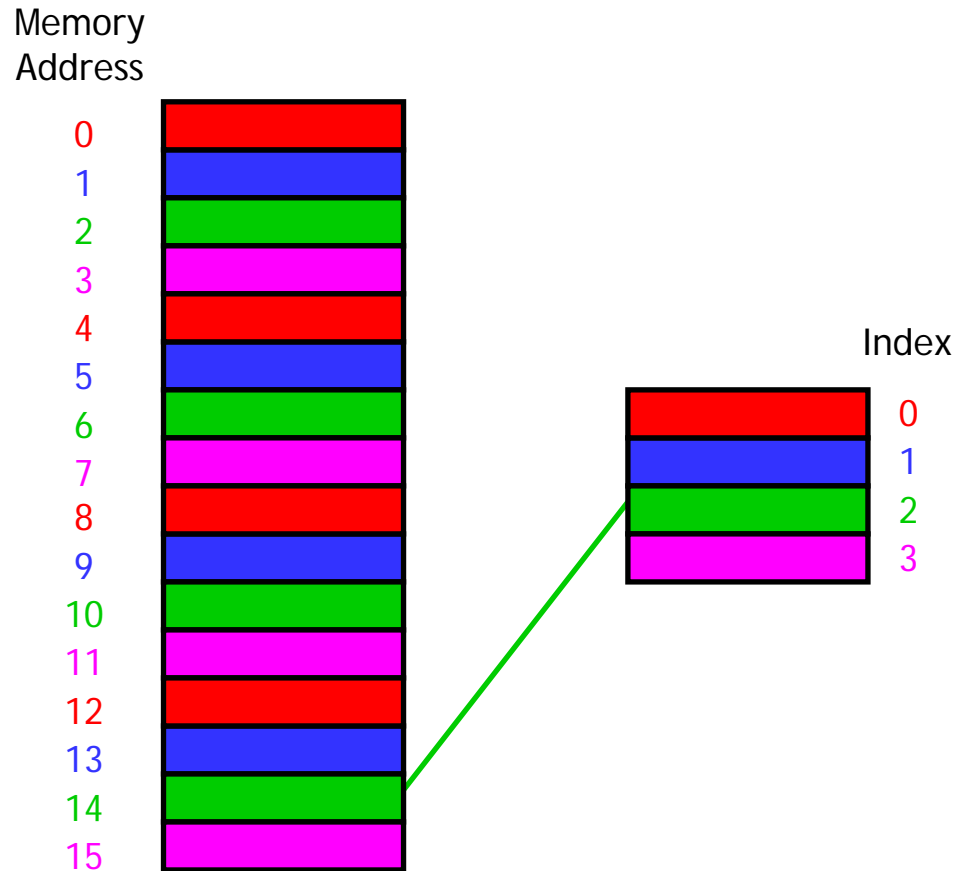
It's all divisions...

- ❑ One way to figure out which cache block a particular memory address should go to is to use the mod (remainder) operator.
- ❑ If the cache contains 2^k blocks, then the data at memory address i would go to cache block index

$$i \bmod 2^k$$

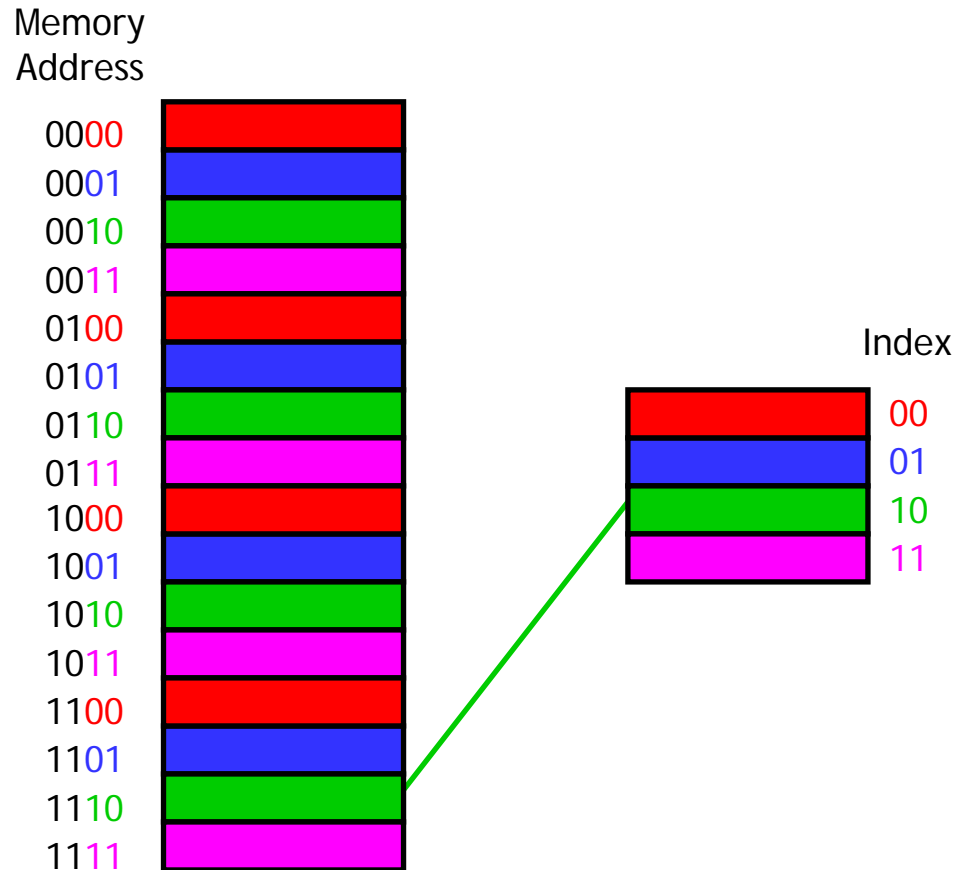
- ❑ For instance, with the four-block cache here, address 14 would map to cache block 2.

$$14 \bmod 4 = 2$$



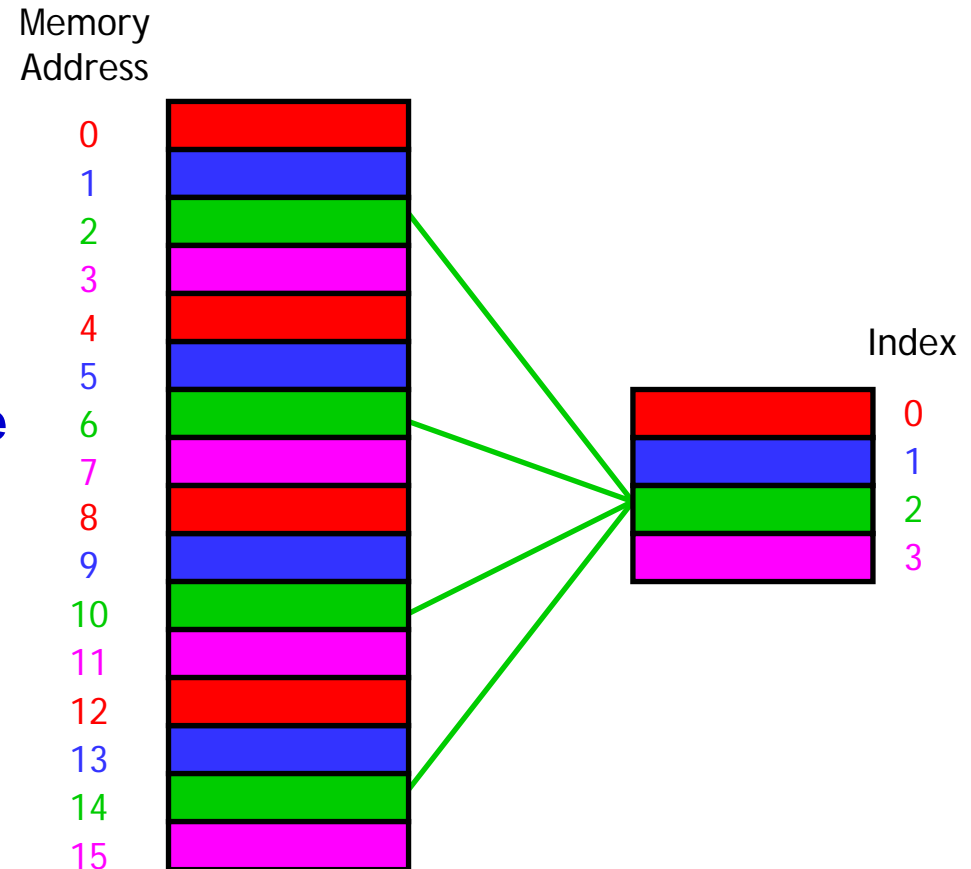
...or least-significant bits

- ❑ An equivalent way to find the placement of a memory address in the cache is to look at the **least significant k** bits of the address.
- ❑ With our four-byte cache we would inspect the two least significant bits of our memory addresses.
- ❑ Again, you can see that address 14 (11**10** in binary) maps to cache block 2 (**10** in binary).
- ❑ Taking the least k bits of a binary value is the same as computing that value mod 2^k .



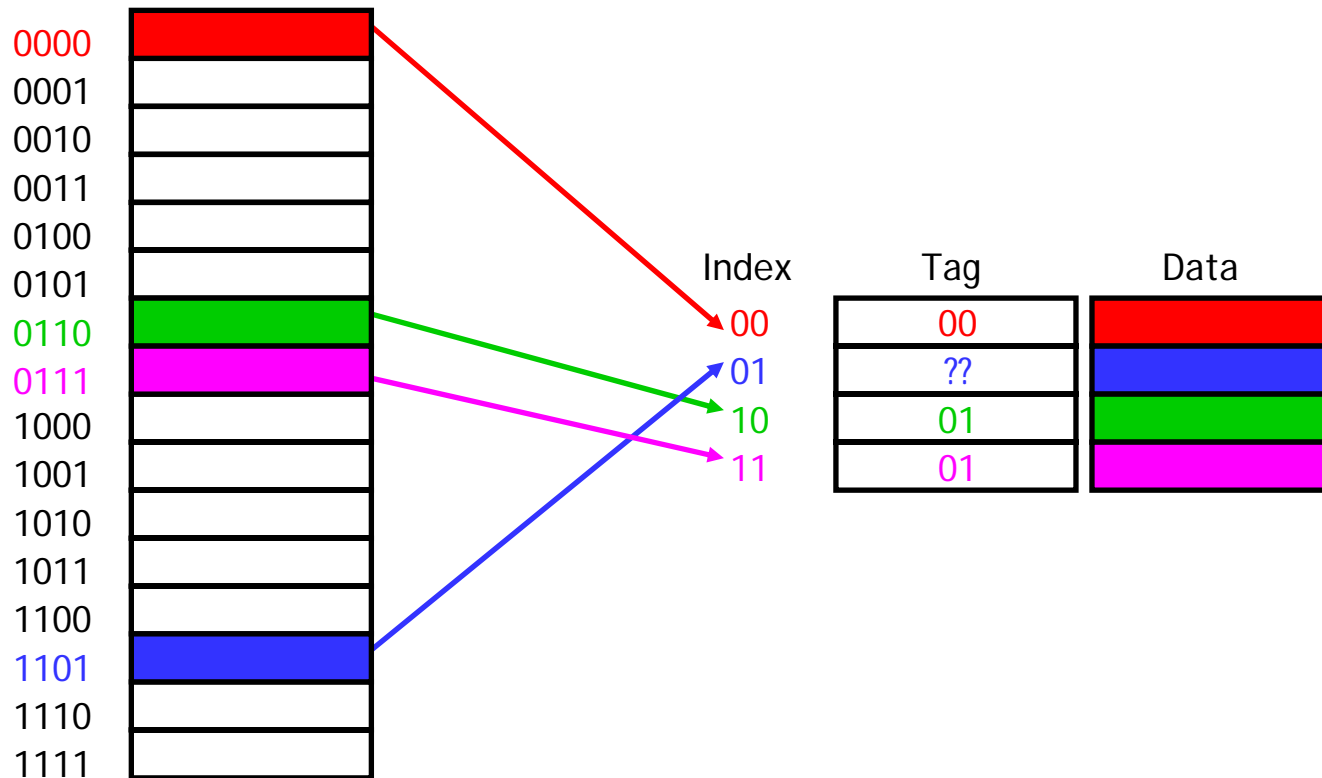
How can we find data in the cache?

- ❑ The second question was how to determine whether or not the data we're interested in is already stored in the cache.
- ❑ If we want to read memory address i , we can use the mod trick to determine which cache block would contain i .
- ❑ But other addresses might *also* map to the same cache block. How can we distinguish between them?
- ❑ For instance, cache block 2 could contain data from addresses 2, 6, 10 or 14.



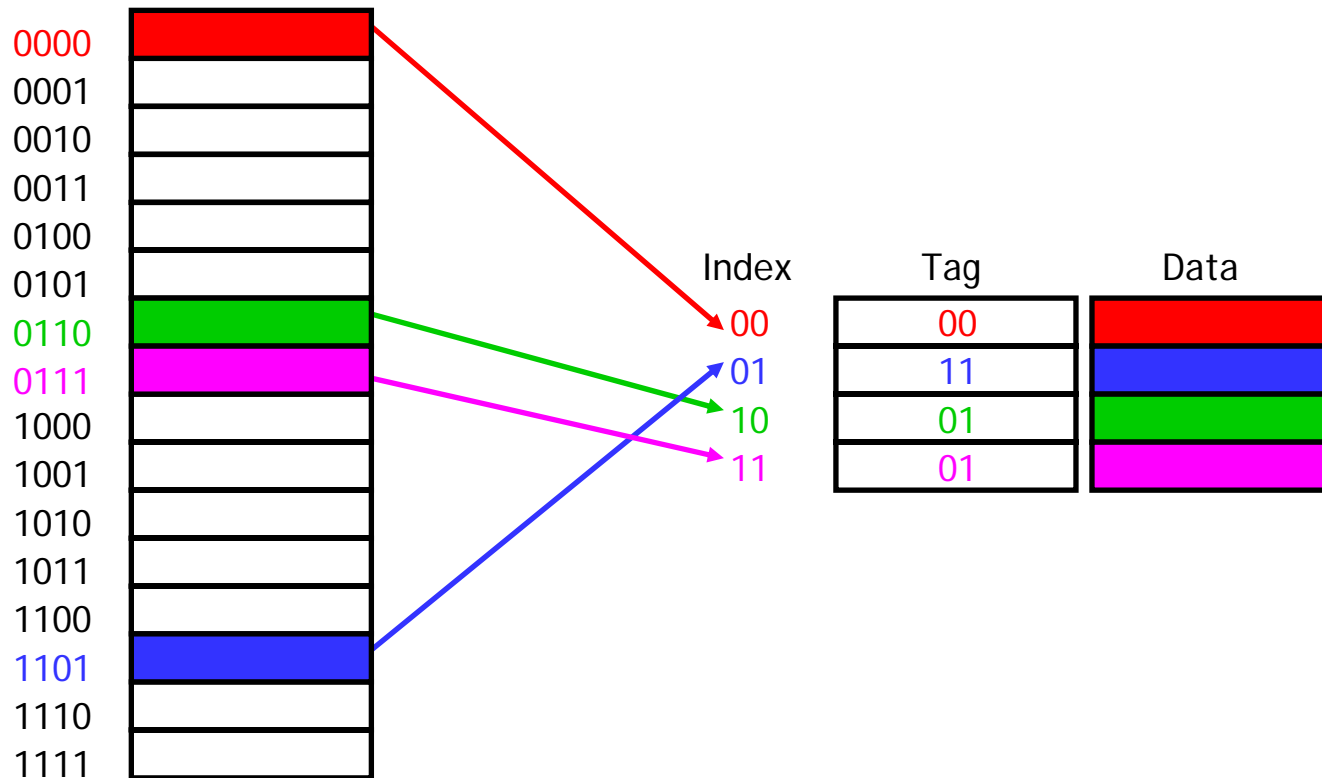
Adding tags

- We need to add **tags** to the cache, which supply the rest of the address bits to let us distinguish between different memory locations that map to the same cache block.



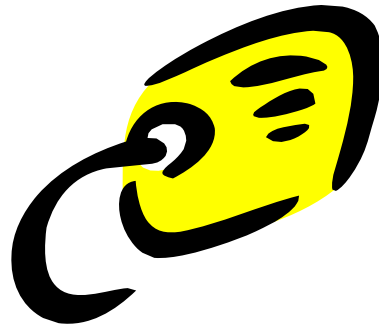
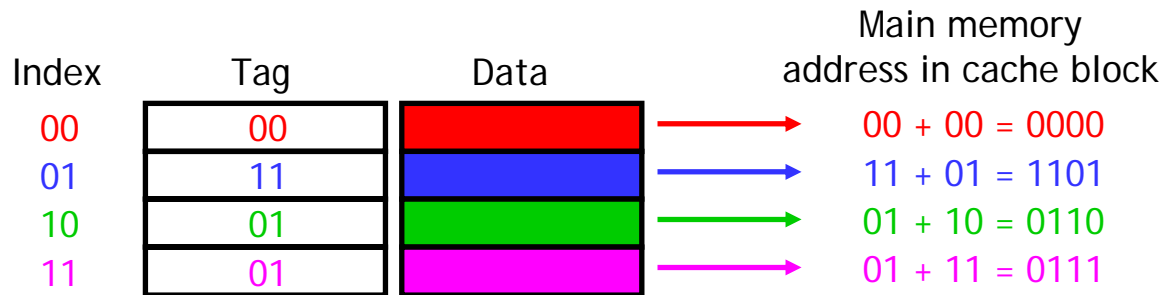
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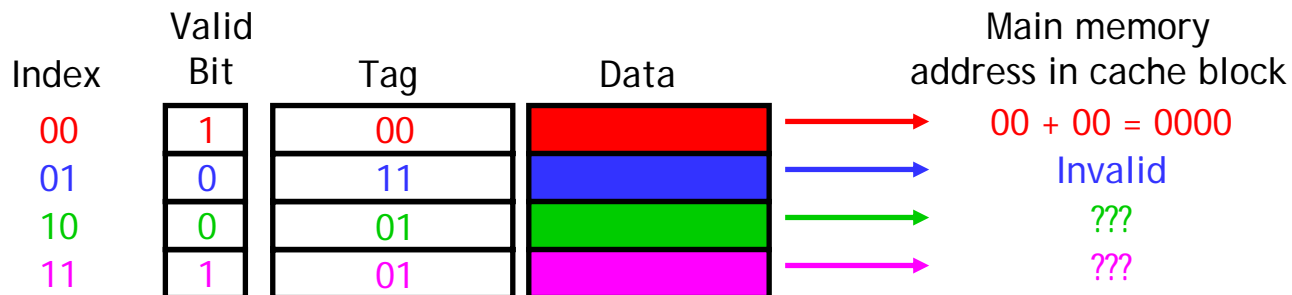
Figuring out what's in the cache

- Now we can tell exactly which addresses of main memory are stored in the cache, by concatenating the cache block tags with the block indices.



One more detail: the valid bit

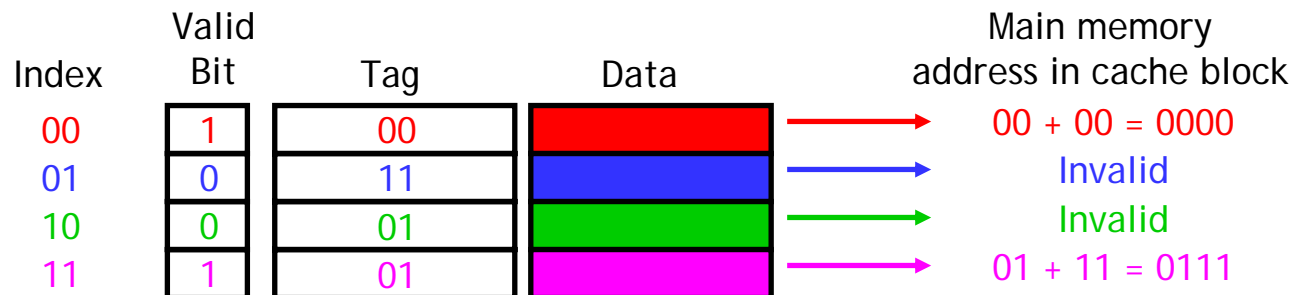
- ❑ When started, the cache is empty and does not contain valid data.
- ❑ We should account for this by adding a **valid bit** for each cache block.
 - When the system is initialized, all the valid bits are set to 0.
 - When data is loaded into a particular cache block, the corresponding valid bit is set to 1.



- ❑ So the cache contains more than just copies of the data in memory; it also has bits to help us find data within the cache and verify its validity.

One more detail: the valid bit

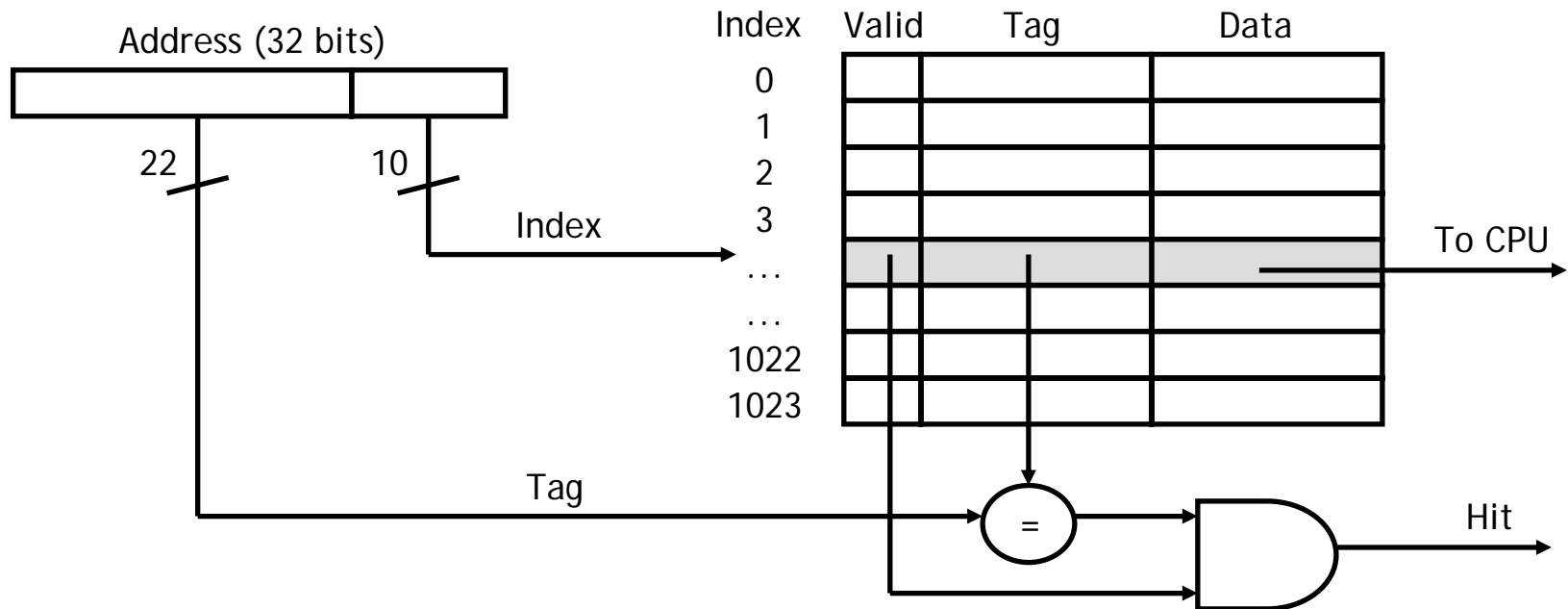
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- ❑ So the cache contains more than just copies of the data in memory; it also has bits to help us find data within the cache and verify its validity.

What happens on a cache hit

- ❑ When the CPU tries to read from memory, the address will be sent to a **cache controller**.
 - The lowest k bits of the address will index a block in the cache.
 - If the block is valid and the tag matches the upper $(m - k)$ bits of the m -bit address, then that data will be sent to the CPU.
- ❑ Here is a diagram of a 32-bit memory address and a 2^{10} -byte cache.



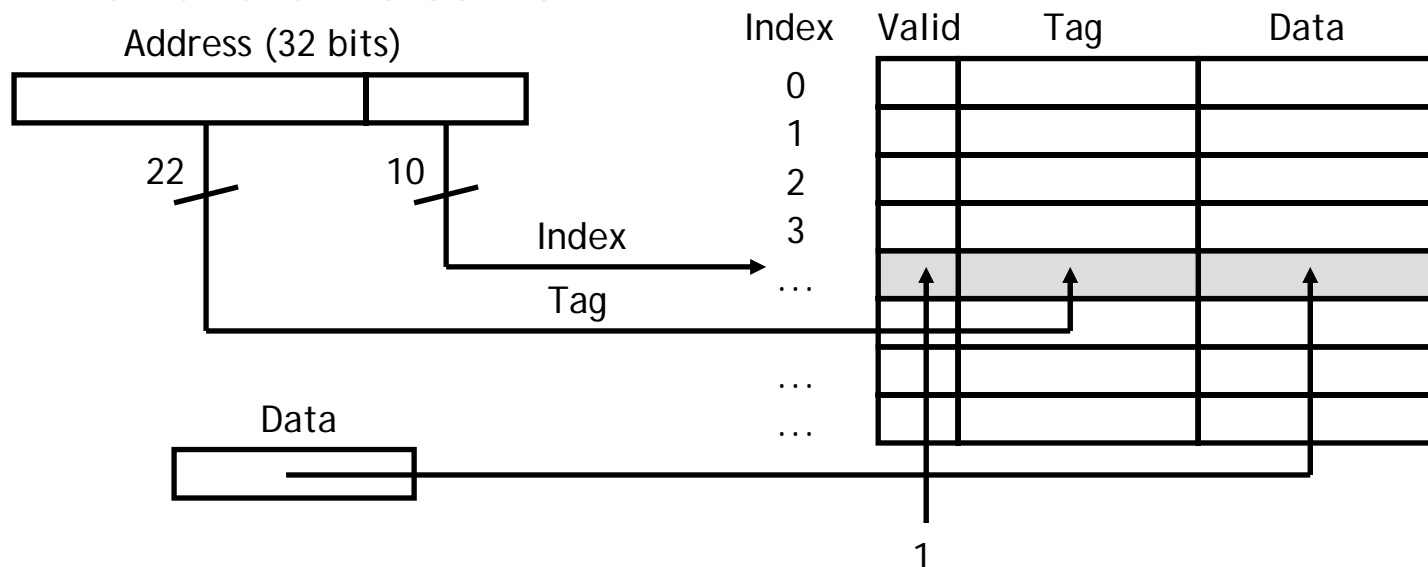
What happens on a cache miss

- ❑ **The delays that we've been assuming for memories (e.g., 2ns) are really assuming cache hits.**
 - **If our CPU implementations accessed main memory directly, their cycle times would have to be much larger.**
 - **Instead we assume that most memory accesses will be cache hits, which allows us to use a shorter cycle time.**

- ❑ **However, a much slower main memory access is needed on a cache miss. The simplest thing to do is to stall the pipeline until the data from main memory can be fetched (and also copied into the cache).**

Loading a block into the cache

- ❑ After data is read from main memory, putting a copy of that data into the cache is straightforward.
 - The lowest k bits of the address specify a cache block.
 - The upper $(m - k)$ address bits are stored in the block's tag field.
 - The data from main memory is stored in the block's data field.
 - The valid bit is set to 1.



What if the cache fills up?

- ❑ Our third question was what to do if we run out of space in our cache, or if we need to reuse a block for a different memory address.
- ❑ We answered this question implicitly on the last page!
 - A miss causes a new block to be loaded into the cache, automatically overwriting any previously stored data.
 - This is a **least recently used** replacement policy, which assumes that older data is less likely to be requested than newer data.
- ❑ We'll see a few other policies next week.

Summary

- ❑ Today we studied the basic ideas of **caches**.
 - By taking advantage of **spatial and temporal locality**, we can use a small amount of fast but expensive memory to dramatically speed up the average memory access time.
 - A cache is divided into many **blocks**, each of which contains a **valid bit**, a **tag** for matching memory addresses to cache contents, and the data itself.
- ❑ Next week we'll look at some more advanced cache organizations and see how to measure the performance of memory systems.

