## CS 150 (Closed-book) Midterm Test I

Oct. 29, Wednesday, 7:10-7:50pm, 2025 Total: 40 points

Name:

UCR Net ID:

QUESTION 1. [10 pts] Design a DFA to accept the following language:

 $L = \{x \mid x \in \{0,1\}^*, x \text{ contains at least one 0 and at most two 1's}\}$ 

Answer:

In the following DFA, the subscripts a, b in state  $q_{a,b}$  count the numbers of 0's and 1's in the input string, respectively.

	0	1
$\rightarrow q_{0,0}$	$q_{1,0}$	$q_{0,1}$
$*q_{1,0}$	$q_{1,0}$	$q_{1,1}$
$q_{0,1}$	$q_{1,1}$	$q_{0,2}$
$*q_{1,1}$	$q_{1,1}$	$q_{1,2}$
$q_{0,2}$	$q_{1,2}$	$q_{dead}$
$*q_{1,2}$	$q_{1,2}$	$q_{dead}$
$q_{dead}$	$q_{dead}$	$q_{dead}$

Either a state diagram or table would be acceptable. Give partial credits for DFAs with some relevant properties. E.g., we may deduct 2 or 3 pts for mis-handling the dead state.

QUESTION 2. [10 pts] Design an NFA or DFA to accept the following language:

 $L = \{x \mid x \in \{0,1\}^*, x \text{ represents a binary number that is greater than } 7\}$ 

Hint: For example, L contains strings 1000,0010010 and 011011, but it does not contain strings 111,000011 and 00110. You may want to consider the position (counting from the right) of the leftmost 1 in such binary numbers.

## Answer:

The following NFA checks if the input contains at 1 bit that is at least four positions away from the end:

	0	1
$\rightarrow q_0$	$\{q_0\}$	$\{q_0,q_1\}$
$q_1$	$\{q_2\}$	$\{q_2\}$
$q_2$	$\{q_3\}$	$\{q_3\}$
$q_3$	$\{q_4\}$	$\{q_4\}$
$*q_4$	$\{q_4\}$	$\{q_4\}$

Note that the answer may not be unique. The nondeterminism on state  $q_0$  can also be removed to make the model a DFA. In this case, the DFA checks if the first 1 bit in the input is at least four positions away from the end. Give partial credits for relevant constructs.

 ${\bf QUESTION~3.}~[10~{\rm pts}]$  Convert the following NFA to a DFA:

	0	1
$\rightarrow q_0$	$\{q_1\}$	$\{q_0,q_2\}$
$*q_1$	$\{q_0,q_2\}$	$\{q_2\}$
$q_2$	$\{q_1,q_2\}$	Ø

Answer:

	0	1
$\longrightarrow \{q_0\}$	$\{q_1\}$	$\{q_0,q_2\}$
$*{q_1}$	$\{q_0,q_2\}$	$\{q_2\}$
$q_2$	$\{q_1,q_2\}$	Ø
$\boxed{ \{q_0, q_2\} }$	$\{q_1,q_2\}$	$\{q_0,q_2\}$
$*\{q_1, q_2\}$	$\{q_0, q_1, q_2\}$	$\{q_2\}$
$*\{q_0, q_1, q_2\}$	$\{q_0, q_1, q_2\}$	$\{q_0,q_2\}$
Ø	Ø	Ø
$*\{q_0, q_1\}$	$\{q_0, q_1, q_2\}$	$\{q_0,q_2\}$

It's okay to exclude/include the inaccessible state  $\{q_0, q_1\}$ . Give partial credits for correct steps. Deduct 1 pt for missing the state  $\emptyset$ .

QUESTION 4. [10 pts] Give a regular expression for the following language:

$$L = \{x \mid x \in \{0,1\}^*, \ x \text{ does not end with } 101\}$$

Answer:

$$(0+1)^*0 + (0+1)^*11 + (0+1)^*001 + 01 + 1 + \epsilon$$

The regex is not unique. Give partial credits for regex's containing some correct components.