

UNIVERSITY OF CALIFORNIA, RIVERSIDE
Department of Computer Science and Engineering
Department of Electrical Engineering
CS/EE120A – Logic Design
Homework 2
Given May 7, Due May 14, 2001

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1. Use the tabulation method to simplify the function $f(w,x,y,z) = \Sigma(0,2,5,7,13,15)$. List all the PI's, EPI's, cover lists, and solutions. (4)

Answer:

| Group ID | Subcube Minterms | Subcube Value | | | | Subcube Covered |
|----------|------------------|---------------|---|---|---|-----------------|
| | | w | x | y | z | |
| G_0 | m_0 | 0 | 0 | 0 | 0 | ✓ |
| G_1 | m_2 | 0 | 0 | 1 | 0 | ✓ |
| G_2 | m_5 | 0 | 1 | 0 | 1 | ✓ |
| G_3 | m_7 | 0 | 1 | 1 | 1 | ✓ |
| | m_{13} | 1 | 1 | 0 | 1 | ✓ |
| G_4 | m_{15} | 1 | 1 | 1 | 1 | ✓ |

| Group ID | Subcube Minterms | Subcube Value | | | | Subcube Covered |
|----------|------------------|---------------|---|---|---|-----------------|
| | | w | x | y | z | |
| G_0 | $m_{0,2}$ | 0 | 0 | - | 0 | |
| G_2 | $m_{5,7}$ | 0 | 1 | - | 1 | ✓ |
| | $m_{5,13}$ | - | 1 | 0 | 1 | |
| G_3 | $m_{7,15}$ | - | 1 | 1 | 1 | |
| | $m_{13,15}$ | 1 | 1 | - | 1 | ✓ |



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|-----------------------------|
| 2 points for correct tables |
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| Group ID | Subcube Minterms | Subcube Value | | | | Subcube Covered |
|----------|------------------|---------------|---|---|---|-----------------|
| | | w | x | y | z | |
| G_2 | $m_{5,7,13,15}$ | - | 1 | - | 1 | |

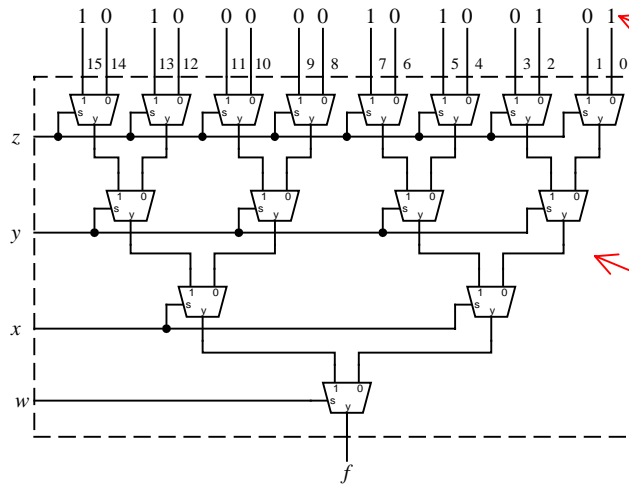
| Prime Implicant Name | Prime Implicant Expression | Implicant Minterms | Function Minterms | | | | | |
|-----------------------|----------------------------|--------------------|-------------------|---|---|---|----|----|
| | | | 0 | 2 | 5 | 7 | 13 | 15 |
| P_1 | $w'x'z'$ | (0,2) | ⊗ | ⊗ | | | | |
| P_2 | $xy'z$ | (5,13) | | | × | | × | |
| P_3 | xyz | (7,15) | | | | × | | × |
| P_4 | xz | (5,7,13,15) | | | × | × | × | × |
| EPI covered minterms: | | | 0 | 2 | | | | |
| Not covered minterms: | | | | | 5 | 7 | 13 | 15 |

PI list: $w'x'z', xy'z, xyz, xz$
 EPI list: $w'x'z'$
 cover list: $w'x'z', xz$
 $f = w'x'z' + xz$

2 points for correct PI, EPI and f .

2. Use only 2-to-1 multiplexers to implement the function $f(w,x,y,z) = \Sigma(0,2,5,7,13,15)$. Do not simplify it. (4)

Answer



2 points for correct connections to 0 and 1

2 points for correct circuit and labels

3. Use VHDL to design an 8-bit wide tri-state buffer. (4)

Answer

The VHDL code for an 8-bit wide tri-state buffer is shown below.

```

LIBRARY ieee;
USE IEEE.std_logic_1164.all;

ENTITY TriState_Buffer IS
    PORT(E: IN std_logic;
         D: IN std_logic_vector(7 downto 0);
         Y: OUT std_logic_vector(7 downto 0));
END TriState_Buffer;

ARCHITECTURE Behavioral OF TriState_Buffer IS
BEGIN
    IF E = '1' THEN
        Y <= D;
    ELSE
        Y <= (OTHERS => 'Z');      -- to get 8 Z values
    END IF;
END Behavioral;
    
```

4. Use basic gates to design a 3-to-8 decoder. (4)

Answer

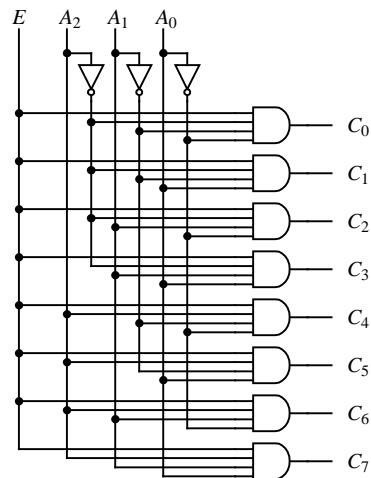
The truth table for the 3-to-8 decoder is as follows:

| E | A_2 | A_1 | A_0 | C_7 | C_6 | C_5 | C_4 | C_3 | C_2 | C_1 | C_0 |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 0 | × | × | × | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

The outputs C_i 's are dependent on E and the three address lines A_i 's. We have eight equations for the eight C_i 's.

$$\begin{aligned}
 C_0 &= EA_2'A_1'A_0' \\
 C_1 &= EA_2'A_1A_0 \\
 C_2 &= EA_2A_1A_0' \\
 C_3 &= EA_2A_1A_0 \\
 C_4 &= EA_2A_1'A_0' \\
 C_5 &= EA_2A_1'A_0 \\
 C_6 &= EA_2A_1A_0' \\
 C_7 &= EA_2A_1A_0
 \end{aligned}$$

The circuit is



4 points for correct circuit