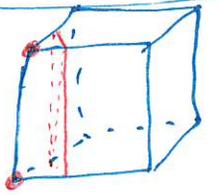


Table filling transforms

hard-code
once:



24 table entries: 12 edges, 2 colors

* how many permutations are possible? (so both have same case)

$$\begin{array}{ccc}
 8 & \cdot & 3 & \cdot & 2 & = & \boxed{48} \\
 \uparrow & & \uparrow & & \uparrow & & \\
 \text{first vertex} & & \text{neighbor vertex} & & \text{color flip} & &
 \end{array}$$

* need a simple, small set of transformations to generate all of them

→ rotate x axis (or y or z)

→ rotate $\begin{matrix} x & \nearrow & y \\ & \searrow & z \end{matrix}$ (about diagonal)

→ flip $x \rightarrow -x$ (or y or z)

→ color inversion

→ need rot + flip + color

eg: rot-x rot-y flip-x color-swap

→ just needs to generate everything, does not need to be efficient

→ (but rotations preferred)

algorithm

fill (case c, triangulation t)

if c done, return true
fill(c) = t, done(c) = true
 $(c_1, t_1) \leftarrow \text{rot } x(c, t)$

fill(c, t)

$(c_2, t_2) \leftarrow \text{rot } y(c, t)$

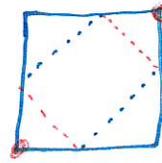
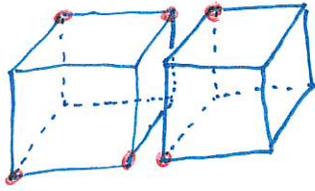
fill(c, t)

$(c_3, t_3) = \text{flip } x(c, t)$

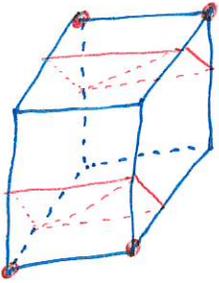
fill(c, t)

~~(c, t) = flip color(c, t)~~
if not ambiguous
 $(c_4, t_4) = \text{flip color}(c, t)$; fill(c, t)

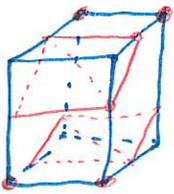
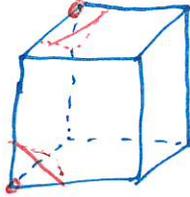
* Marching cubes ambiguity



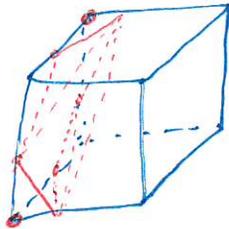
ambiguous face
both cubes must agree • vs •



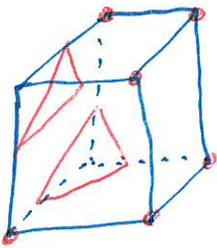
green connected



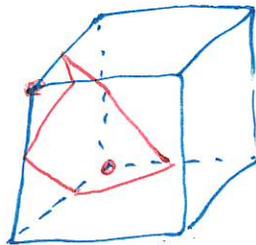
red connected



* many ways to resolve. eg, always connect the red vertices



vs

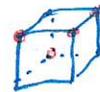


* when filling the table, some transformations do not preserve the resolution

ok
rotation
flip

breaks resolution
color flip

* must create both triangulations for these:



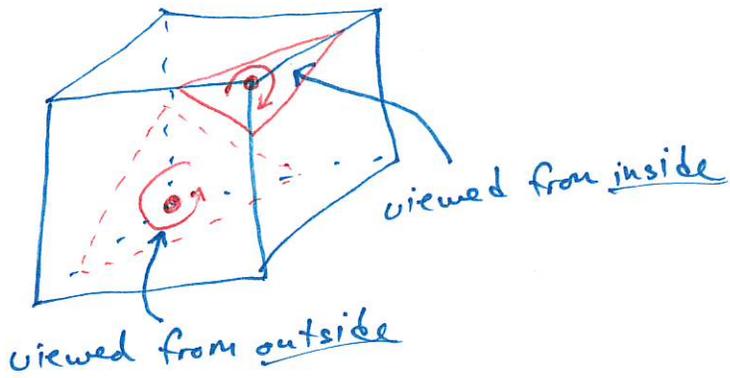
↕ (flip)

but not these:

* check for ambiguous face before doing color flip

Translation and orientation

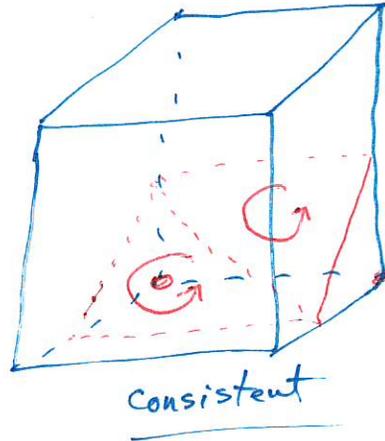
* CCW viewed from outside (• = inside)



* transformations may reverse this!

→ preserve
rotate

flip orientation
flip
color flip

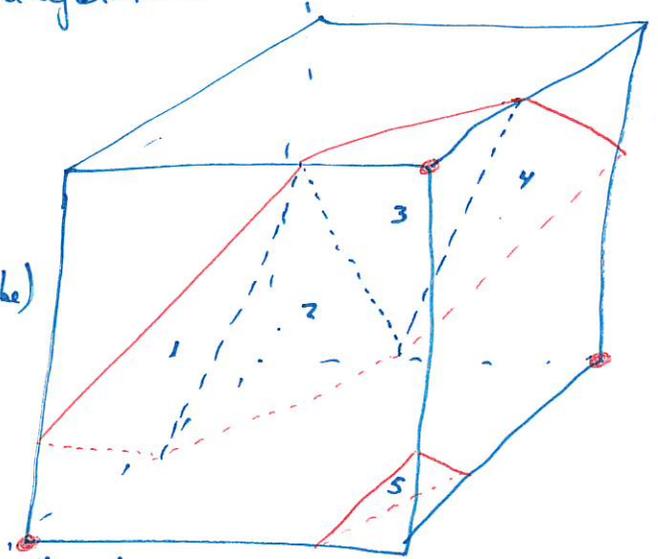


Other notes

- * choose edge numbering wisely - it helps!
- * for each xform, make a lookup table mapping ① old vertex to new vertex & ② old edge to new edge
- * use table ① to compute the new case
- * use table ② to compute the new triangulation
- * no tables needed for color flip

* compact representation

- 5 triangles (max)
- 3 vertices per triangle (each an edge/cube)
- 12 edges → 4 bits
- $4 \cdot 3 \cdot 5 = 60$ bits
- 64-bit long per case encodes everything!



→ 64-bit = 8 byte • 256 cases = 2KB table (small!)