Image Mining of Historical Manuscripts to Establish Provenance

Bing Hu Thanawin Rakthanmanon Bilson Campana Abdullah Mueen Eamonn Keogh

University of California, Riverside

{bhu002, rakthant, bcampana, mueen, eamonn}@cs.ucr.edu

ABSTRACT



he recent digitization of more than twenty million books has been led by initiatives from countries wishing to preserve their cultural heritage and by commercial endeavors, such as the Google Print

Library Project. Within a few years a significant fraction of the world's books will be online. For millions of intact books and tens of millions of loose pages, the provenance of the manuscripts may be in doubt or completely unknown, thus denying historians an understanding of the context of the content. In some cases it may be possible for human experts to regain the provenance by examining linguistic, cultural and/or stylistic clues. However, such experts are rare and this investigation is clearly a time-consuming process. One technique used by experts to establish provenance is the examination of the ornate initial letters appearing in the questioned manuscript. By comparing the initial letters in the manuscript to annotated initial letters whose origin is known, the provenance can be determined.

In this work we show for the first time that we can reproduce this ability with a computer algorithm. We leverage off a recently introduced technique to measure texture similarity and show that it can recognize initial letters with an accuracy that rivals or exceeds human performance. A brute force implementation of this measure would require several years to process a single large book; however, we introduce a novel lower bound that allows us to process the books in minutes.

Keywords

Image Similarity, Classification, Clustering, Texture

1. INTRODUCTION



he last decade has seen the digitizization of twenty million historical texts [6][23][30], and an even greater number of individual manuscripts, including maps, playing cards,

posters and most frequently, orphaned pages that have been separated from their original books (often due to theft [1][3][8]). The majority of such texts published before the 1830s are ascribed to the *Hand-Press period*. The Hand-Press period started with Gutenberg's invention around 1450, ushering in the advent of mechanized presses. This period is characterized by the use of wood blocks [33] with a relief (negative) carving on it, to print the ornamental letters at the beginning of chapters. Figure 1 shows some representative examples.



Figure 1: Decorative initials are large letters illuminated with tendrils, figures and hatching. These four examples hint at their diversity



or some books from this period, the provenance of the texts is known down to the name of the printer who physically printed it and the day it was printed. However, for many texts (especially those

missing the frontispiece) and most single page documents, the provenance may be as uncertain as "probably printed somewhere in Germany or Austria in the late sixteenth or early seventeenth century."

There are at least two reasons why we may wish to determine the provenance of such manuscripts:

- There is a huge market for stolen manuscripts, especially of individual pages. In several recent high profile cases, individuals have been caught stealing pages from libraries in Europe and the Middle East and brazenly selling them on EBay [1][3]. In just one criminal case, thousands of individual pages worth millions of dollars were involved [1]. This represents a tragic loss of national identity for the affected countries. As noted by Lord Renfrew, a leading advocate against art crime, "the single largest source of destruction of heritage today is through looting... ...for commercial profit" [8]. Clearly establishing the provenance of a suspect document is the first step in a criminal investigation [10].
- For historians and linguists, knowing the provenance of a manuscript is critical to understanding the evolution of ideas and the process of cultural transmission [2].



n some cases it may be possible for human experts to regain the provenance of unannotated manuscripts by examining linguistic, cultural, and/or stylistic clues.

However, such experts are rare and this is clearly a time consuming and expensive process. One of the most important clues used by human experts are the initial letters present in the text, which is sometimes referred to as the "fingerprint" of the printer. We propose using data mining techniques to examine initial letters and thereby automate the discovery of provenance. The legal/technical model of fingerprint biometrics is actually a good analogy for what we are proposing. It is the computer's task simply to eliminate the countless true negatives and to bring to the attention of a human expert a handful of candidate examples, hopefully including any true positives.

This is essentially what we are proposing. In fact, fingerprint biometrics is an example of *impression evidence* [21] and initial letters are also *literal* examples of impression evidence. Just as a person's finger can make multiple impressions during their lifetime, wood blocks were also used to create multiple impressions throughout their usage (which may have been several decades or more). Likewise, fingerprint recognition may be difficult because the two impressions we wish to link may have been made decades apart; the finger may have picked up additional scars or blemishes in the interim. This is also true of our initial letters, which receive constant wear and possibly occasional repairs during their lifetime.

The obvious difference between our task and fingerprint recognition is that the latter, because of its legal and commercial importance, has received a huge amount of research effort [21], whereas our task is relatively understudied. As historical manuscript expert Dr. Jean-Marc Ogier, who has spent over a decade studying this problem recently bemoaned, "*There is little known on how to compute invariants for indexing documents on this kind of features.*" [22]

We have surveyed all the relevant literature [5][9][11][22][25] and we argue that none of the current techniques are able to scale to web sized collections of manuscripts and, more critically, none of them are likely to be accurate and robust enough for the task at hand. While there is some tentative evidence of accurate measures, there is also evidence that some of the results can be attributed to careful cherry-picking of test datasets, *manual* extraction of the initial letters, careful parameter tuning and (perhaps) overfitting.

We propose to solve this problem by leveraging off a recently introduced parameter-free distance measure called the CK1 measure [7]. As we shall show, the CK1 measure is extraordinarily effective for matching problems in historical manuscripts, with discrimination abilities that rival human experts. While the CK1 measure is relatively efficient, a naive search method based on it would take several months to test an entire large book for the occurrence of a pattern; however, we introduce in this work a novel lower bound that allows us to process such books in hours or less.

The rest of this paper is organized as follows. In Section 2, we introduce all the necessary definitions and notation. In Section 3 we review the CK1 measure that is at the heart of our technique. Section 4 introduces our lower bound algorithms for the CK1 measure and a search algorithm that exploits it. We evaluate our ideas in Section 5 and offer conclusions and directions for future work in Section 6.

2. DEFINITIONS AND NOTATION

We begin by introducing all necessary notation and definitions. Whether we are mining archives of books, maps, single page manuscripts, etc., we can simply generalize our data source as *pages*:

Definition 1: A *page*, *P*, is represented as an $M \times N$ matrix. Each pixel of the page corresponds to an element in the matrix, where *M* and *N* are the width and height of the page, respectively.

As noted in [14], "Most classical methods (to process historical manuscripts) need a binarization step." Our method does not require a binarization step to produce high quality results. For example, the results reported later in Figure 4 and Figure 12 used the original gray-scale images. However, as we will show in Section 4, we can exploit an *internal* binarized representation to produce lower bounds to make our search algorithms significantly faster. To binarize a page P we transform the grayscale page into black or white using a simple binary threshold filter [15].

To identify the provenance of an unlabeled *page*, experts compare any existing initial letters, as shown in Figure 1, in the *page* to the reference initial letters. We call such reference initial letters *annotated initial letters*.

Definition 2: *Annotated initial letters* are the initial letters whose provenances have been firmly established.

Because of the increasing interest in cultural heritage there are many digital repositories that have huge collections of carefully annotated initial letters [30]. Many of these sources have on the order of thousands of annotated initial letters. Since the goal of our work is to establish the provenance of historical manuscripts by using just small sub-regions of a page containing initial letters, we compare *all* candidate regions within a page to the annotated initial letters. We call these small regions *windows*.

Definition 3: A *window W* of pixels *d* is a rectangular area inside a *page*.

$$W_{x, y} = \{ d_{i, j} \in P \mid i \in [x, x+m) \land j \in [y, y+n) \},\$$

where m and n are the width and height of the window, respectively.

The window size is determined by the size of the annotated initial letters.

For the page shown in Figure 2.*right*, the fine/blue square is an example of a *window*. The full set of all possible windows is obtained by sliding a *window* from the left to the right, and the top to the bottom of the *page*. For a *page* with size *M* by *N*, given a target initial

letter size *m* by *n*, the number of windows is $(M-m+1) \times (N-n+1)$.



Figure 2: *left*) The zoom-in of the bold/red box shown in page from *Comediae*, published in 1552. *right*). The bold/red box is the target, an initial letter. The fine/blue box is a *window*

Note that while our choice of an axis parallel rectangle as our primitive window shape is clearly based on how wood block initial letters are typically presented, it is not a limiting assumption. As we later show, our algorithm is oblivious to minor violations of the axisparallel assumptions (such as the rotated letters shown in Figure 12). Moreover, our algorithms can be trivially adapted to be optimized to other shapes, such as the typically round shape of Japanese mon (the Japanese equivalent of European heraldic shields [34]). At the heart of our provenance attribution scheme is the ability to compare candidate windows with initial letters from our reference library. We will use the recently introduced CK1 distance measure [7] for this task:

Definition 4: The *distance* between a *window* and an annotated initial letter is denoted as dist(W, IL). Thus, the *distance* is: $dist(W, IL) = CK1_dist(W, IL)$

In Section 3, we give a more detailed explanation of how the CK1 distance measure works and our reasons for using it rather than the dozens of rival techniques.

As hinted at above, while the CK1 measure can work with either grayscale or binary images, for the purpose of allowing lower bounding search, we need to use an internal binarized representation. Note that this does not preclude working directly with the grayscale images; it is only the *internal* search algorithm that must work with the internal binarized representation.

To support this internal representation, we define the *black pixel density* of a window.

Definition 5: The *black pixel density* of a binarized image is the total number of pixels that are '0', divided by the total number of pixels in this image.

Note that we assume that in a binary image, '0' represents a black pixel and '1' represents a white pixel. The *black pixel densities* of the three images in Figure 3 (from left to right) are 70.9%, 38.1% and 18.6%, respectively. From these results, we can see that there is a large difference in black pixel density between an initial letter and the typical plain text in a page (Figure

3.*right*). In Section 4, we will explain how to exploit this property to create tight lower bounds.



rition (Lusrin vis qui at, blandus est; ille qui us; & tamen vierque) esfius, qu'àm Chrenes f cheniens at fußticiofus? I chetinus inop: antini àm Pradria cum morbo

Figure 3: *left*). A "*dense*" initial letter. *center*). A "sparse" initial letter. *right*). The zoom-in of the window marked by the light/blue square in Figure 2

3. A REVIEW OF THE CK1 MEASURE

As noted in the previous section, we intend to use the recently introduced CK1 distance measure [7] to compare *windows* from historical texts to initial letters from our reference collections. We begin by giving the reader a hint of the utility of CK1 in this domain. In Figure 4 we cluster twelve initial letters known to come from three classes, including two classes that have just the subtlest of differences.



Figure 4: Twelve ornamental initial letters, from three classes that represent the letter 'S', are clustered using CK1 with complete linkage hierarchical clustering

As we can see, the CK1 distance measure is able to robustly recognize very subtle distinctions.

Surprisingly, as shown in Table 1, computing the CK1 distance between two images *x* and *y* is accomplished with just a *single line* of parameter-free Matlab code:

Table 1: CK1 distance measure

function dist = $CK1_{Distance}(x, y)$
dist = ((mpegSize(x,y) + mpegSize(y,x))/(mpegSize(x,x) + mpegSize(y,y)))-1;

The distance range for the CK1 measure is from zero to a "soft" one. That is to say, the distance between an object and itself is exactly zero, and the distance between two very dissimilar objects is expected to be one, but can be slightly larger.

We refer the reader to the original paper [7] for more details on this measure. However, we briefly note that it is a measure that follows the framework developed by Li and Vitányi (and colleagues [20]) which states that two objects can be considered similar if information garnered from one can help compress the other [17].

There are three main reasons why we chose the CK1 distance measure over dozens of alternatives. First, it is a parameter-free measure. Compared to parameterladen algorithms [25], the CK1 measure is more likely to be adopted by historians who will be unable or unwilling to carefully tune parameters. Second, as shown by the original authors and confirmed by experiments below, the CK1 measure is very accurate. Thirdly, compared to other algorithms [9], the measure is very robust to distortions on images. Historical documents are often represented by a single surviving instance and have a lot of variability. For example, the images may be faded, printed with the rotation askew, be inconsistently illuminated, have insect damage, be poorly scanned, etc. As we shall show, the CK1 measure is largely robust to these variances.

3.1 Accuracy and Robustness of CK1

We claimed above that the CK1 measure is very accurate and robust for our domain. This will be implicitly shown in our experiments in Section 5, and was hinted at in Figure 4. However, we take this opportunity to *explicitly* demonstrate this here.

We have conducted an experiment¹ to illustrate how well CK1 works as a distance measure in our domain. Using a subset² of the dataset created by [4] which contains nineteen classes of 16^{th} -century ornamental letters, with 578 images (including those shown in Figure 4), we conducted leave-one-out cross-validation classification. The error rate is 0.00%. Recall that we had no parameters to tune; thus, these results are highly likely to generalize. As the largest class (the letter 'A') has 82 members, the default error rate is 85.8%.

We also tried two rival approaches. One was specifically designed for initial letters by a team with more than a decade of experience working in this area [9]. The error rate of that approach is 39.42%. The second rival approach is based on the ubiquitous scale-invariant feature transform (SIFT) algorithm [29]. While we are not aware of any papers that use SIFT for initial letter classification, a very recent paper proposes SIFT for the highly related task of segmenting historical manuscripts (into *margin, text, figures, initial letters,*

etc.) [12]. SIFT features (each of them is a 128dimensional vector) are first extracted from the query and candidate images using Lowe's SIFT algorithm [19]. Then the number of matched features/key points is used as the similarity measure between two images. The more features that are matched, the more similar two images are adjudged. The error rate of the leaveone-out cross-validation classification when using SIFT is 10.21%.

We note that we attempted just one SIFT-based distance measure. While the literature is replete with others, most of them require several parameters; this is exactly what we are trying to avoid.

The time taken for SIFT and CK1 are commensurate for this one-to-one matching problem³. However, as we shall later show, for the similarity search (one-to-all) problem we are interested in, we can speed up CK1 by many orders of magnitude. It is less clear that SIFT would yield to such optimizations.

Rare manuscripts are almost always digitized by hand [13]. Digital archivists usually place some kind of photomacrographic scale at the end of a book in order to record the size of the original pages (and normalize the color values). Figure 5 shows two representative examples.



Figure 5: Two examples of historical manuscripts digitized with scales to allow accurate recording of size

Nevertheless, the size of the manuscripts still may have some small amount of uncertainty because of affine transformations during the digitization processes. This is especially true for historical texts, which are typically not contact scanned, because that requires laying the book flat on the glass and damaging the spine. Instead, such manuscripts are photographed in special rigs.

To check the robustness of the CK1 measure to scale variability, we have conducted the following experiment. After randomly resizing each image in the dataset mentioned above, in the range from 90% to 110% (much larger variability than we actually observe in digital archives), we recomputed the leave-one-out cross-validation error rate and found it increased only very slightly, to just 3.81%.

¹We defer a detailed discussion of our experimental philosophy until Section 5; however, we briefly note that *all* our experiments are reproducible, and *all* code and data are available at [35].

² Just the *unique* initial letters were deleted.

³ SIFT was faster by about 30% when given unlimited main memory. If we force it to use a smaller memory footprint, it becomes significantly slower [19].

A small amount of rotation invariance is also required because the scanning process may have misaligned the manuscript. The initial letter wood block itself may have also been originally loose in the mold. We frequently observe misalignments of up to five or six degrees. We therefore have conducted an experiment to check the robustness of the CK1 measure on rotation variability. After randomly rotating each image individually from +10 degrees to -10 degrees, the classification error degrades to just 12.21%.

Before moving on, we will take a moment to emphasize how surprisingly good these results are by visually analyzing the dataset.

Figure 6 shows some sample letters from this data. Note that the 'O' looks very similar to the 'Q', and neither of them fits into a perfect axis parallel rectangle. While the two examples of 'C' were pressed from the same wood block, because of foreshortening during the scanning process, one version appears to be 13% wider than the other. Finally, from a quick glance, the 'L' seems to have as much in common with the center 'l' as the rightmost 'l' does.



Figure 6: Samples of images from the classification dataset hint at how difficult this problem is

It is important to note that this sanity-check *classification* experiment is significantly harder than our *recognition* task at hand. As such, the results above suggest that we may be able to approach perfect precision/recall for our purposes.

Based on these and subsequent experiments (c.f. Section 5), we feel that the CK1 measure is perfect for our task at hand. The one drawback of CK1 distance is that it is not a metric, and thus we cannot use classic spatial tree indexing algorithms such as the R-tree. However, as we shall see, we can mitigate even this weakness.

Having introduced the necessary notation and definitions, and having justified our choice of the CK1 measure, in the next section we can formally define the problem and our solution to it.

4. SEARCH ALGORITHMS

For an unlabeled *page P*, we want to identify its provenance by comparing initial letters on the page with annotated initial letters of known provenance from our reference library. This is a binary decision problem. For a single annotated initial letter from our

reference library, either a page contains a letter stamped from the same wood block or it does not. To sharpen the reader's intuition for our ultimate solution, we begin by explaining the brute force search algorithm.

4.1 Brute Force Search Algorithm

For ease of exposition, we assume that there is just one annotated initial letter in the reference library, and that we are examining a single page. The generalizations to multiple letters and multiple pages are trivial [35].

Given a single annotated initial letter *IL*, of size m by n, and a distance threshold t, we want to know if there exists an initial letter, pressed from the same wooden block, on *page P*. We defer a discussion of how the threshold t is learned until Section 4.3.

Because the window size is determined by the query size, the window size is also m by n. We show the search algorithm in Table 2.

 Table 2: Brute Force Search Algorithm

Algorithm: Brute Force Search			
Inpı	it: P, A page		
	IL, Target annotated initial letter		
	t, The threshold		
Output: exists-flag, Wi // Where Wi encodes location			
1	W = the set of all possible windows in P		
2	for $i = 1$ to $ W $		
3	<pre>current_dist = CK1_dist(W_i, IL);</pre>		
5	<pre>if current_dist < t</pre>		
6	disp('initial letter found at', W_i);		
7	break; // algorithm terminates		
8	endif		
9	endfor		
10	<pre>disp('target initial letter not found');</pre>		

Note that the program will terminate and report that the annotated initial letter exists as soon as a distance smaller than the given threshold is encountered. Under realistic conditions it will take approximately 48 hours to calculate the distances of an annotated initial letter with all the possible *windows* in a page. Thus, for a dataset pool with 6,000 annotated initial letters [30], it will take about 32 years to finish. Furthermore, the size of the dataset pool keeps growing with continuing digitization of historical manuscripts [30]. Recall that these figures are for a *single* page; a single manuscript may have several hundred pages. Thus, the brute force algorithm is clearly not tractable.

A common way to speed up a brute force search is to use a *lower bounding search* [34]. Assume for the moment that we have some lower bounding function for the CK1 measure, which we denote LB. Table 3 shows an algorithm that can exploit such a lower bound for a faster search.

Assuming only that the lower bound is effective and efficient-that is to say, it is reasonably *tight* most of the time, and much *faster* to calculate than the CK1 measure-then we should expect the algorithm shown in

Table 3 to be significantly faster than the brute force search. Since this is critical to our problem, we devote the next section to a discussion of lower bounding the CK1 measure.

Table 3: Lower Bounding Search Algorithm

Algorithm: Lower Bound Algorithm		
Input	2: P, A page	
	IL, Target annotated initial letter	
	t, A threshold	
Outpu	t: exists-flag, W_i // Where W_i encodes location	
1	W = set of all possible windows in P	
2	for i = 1: W	
3	<pre>if LB(W_i, IL_{lower_bound_info}) < t</pre>	
4	<pre>current_dist = CK1_dist (W_i, IL);</pre>	
5	<pre>if current_dist < t</pre>	
6	disp('initial letter found at', W_i);	
7	break; // algorithm returns	
8	endif	
9	endif	
10	endfor	
11	<pre>disp('target initial letter not found');</pre>	

4.2 Lower Bounding the CK1 Measure

4.2.1 CK1 cannot be exactly lower bounded

Lower bounds are known for many expensive distance measures, including Dynamic Time Warping [18], Earth Movers Distance [27], string edit distance, etc. Can the CK1 measure be lower bounded? The greatest strength of the CK1 distance is its "black box" nature. The user does not have to extract any features from the two images to be compared. The two images are simply handed over to the CK1 algorithm in Table 1. However, this is also a great weakness, since most lower bounds work by measuring a "relaxed" distance on features derived from the data [27].

Recall that for a lower bound to be useful, it must have two properties: it must be *tight* (it must have a value that is reasonably close to the true value for at least a significant fraction of comparisons) and it must be significantly *faster* than the true measure. We can naively produce a *perfectly* tight lower bound to the CK1-distance by simply using the CK1-distance distance function itself. Likewise, we can clearly produce a fast (indeed, *constant time*) lower bound by simply hard coding the bound to be zero. However, can we produce a tight *and* fast lower bound?

Let us take a moment to contemplate the *speed* requirement. Because video compression is so ubiquitous and commercially important, MPEG-1 encoders are among the most tightly optimized compression methods available [28]. So producing code that can model even one aspect of their behavior (e.g. the output file size), and be, say, 100 times faster is a daunting challenge. The problem is compounded by the complexity of MPEG encoding. To lower bound the CK1 measure we need to predict the minimum (for the

numerator of the CK1 equation) and maximum (for the denominator) possible final file size of a compression algorithm that uses a plethora of tricks, including the Discrete Cosine Transform, quantization, truncation, block searching [28], etc. A recent paper on the related, but *much* simpler problem of estimating the compressed size of a JPEG image had errors of up to 24.8% even in the best cases [24].

In summary, the current authors, after carefully considering the problem and consulting many image and video compression experts, are unable to come up with a fast *and* tight lower bound for CK1; we strongly suspect that none exists. However, as we shall show in the next section, it is possible to create an *approximate* lower bound that is fast, close to the true value, and *empirically* never fails to be a true lower bound even after tens of millions of empirical tests.

4.2.2 An Approximate Lower Bound of CK1

Our approximate lower bound algorithm exploits the *black pixel density* introduced in Definition 5. As shown in Figure 3, there is typically a large difference in the black pixel density between a window that contains an initial letter and a window that contains plain text or the page margin, etc. In Figure 7, we show the black pixel density distribution of a typical page. The "peak" in the contour map in Figure 7 is the black pixel density corresponding to an initial letter, which begins the last paragraph of column two in the page shown above it. Based on this observation, we suspect that a lower bound algorithm might somehow exploit this easy-to-compute black pixel density.



Figure 7: A page from *Comediae* (1552), with its black pixel density distribution shown as a contour map. Note that the region containing an initial letter shows up as a distinct peak

Our idea is that for any particular initial letter *IL*, we can build a *lookup function* that maps the black pixel density of a candidate window to the *minimum* possible (i.e., the lower bound) CK1 distance between that window and IL. The blue "V" shaped curved line in Figure 8 is the lookup function we learned for the IL shown in Figure 8.c.



Figure 8: A lower bound curve that maps the black pixel density of a candidate window to the minimum distance to IL. c) shows the original image IL, (b)/(a) shows the result of randomly removing pixels, whereas (d)/(e) shows the result of randomly adding pixels

But how can we create this lower bound function? The reader may have already realized that we can trivially compute one point on the curve. The IL in question (Figure 8.c) has a black pixel density of 41%, so an arbitrary window that also has a black pixel density of exactly 41% could have a CK1 distance of zero, since it could be a pixel-for-pixel exact match. This point corresponds to the deepest part of the 'V' shape in Figure 8.

We can calculate the value of the curve one pixel to the left (right) of this special point by testing the CK1distance between IL and all possible variations of IL with a single pixel added (removed) and choosing the minimum value over multiple runs.

Exactly computing the rest of the curve in this manner is impossible due to the combinatorial explosion in the number of ways it is possible to add (remove) K pixels to IL. However, for each pixel density represented in the X-axis we can simply create 1,000 random images that differ from IL by the requisite number of pixels, and compute all their true CK1 distances, recording only the minimum value as the lookup function. For example, the image shown in Figure 8.b is created by randomly changing 50% of the black pixels in the original initial letter to white. The image shown in Figure 8.d is created by randomly changing 50% of the white pixels to black. The last point of this curve is the distance between the original initial letter and a completely black image, as shown in Figure 8.e. The algorithm used for calculating this lower bound distance is shown in Table 4.

Note that we must learn a lower bound for *each* letter in our reference library. This requires tens of thousands of CK1-distance measures, and thus on the order of tens of seconds. However, this only has to be done once, and it is done offline.

Recall that in the brute force search algorithm in Table 2, we used a threshold distance to decide if a candidate

window should be considered a match to a reference internal letter.

Table 4: Lower Bound Function Creation

Algorithm: Lower Bound Function Creation			
Input: IL, One annotated initial letter			
Out	put: lower_bound_dist		
1	<pre>num_black_pixel = find(IL ==0);</pre>		
2	<pre>num_white_pixel = find(IL ==1);</pre>		
3	<pre>flip_black2white=[1:0.01:0] * num_black_pixel;</pre>		
4	<pre>flip_white2black=[0.01:1] * num_white_pixel;</pre>		
5	<pre>pixels_flipped =[flip_black2white,flip_white2black];</pre>		
6	<pre>for i = 1: 1,000 // minimum over some large constant</pre>		
7	<pre>for j = 1: pixels_flipped // pure white to pure black</pre>		
8	<pre>noise_image = change_pixels(IL,pixels_flipped(j));</pre>		
9	<pre>lower_bounds(i,j) = CK1_dist(IL,noise_image);</pre>		
10	endfor		
11	endfor		
12	<pre>lower_bound_dist = min(lower_bounds); // a vector</pre>		

We are now in the position to introduce a technique to learn this threshold distance.

4.3 Learning the threshold distance

We have deliberately glossed over the problem of setting the threshold t until now. A t that is too large decreases the risk of a false negative, but at the expense of decreasing the pruning power. In contrast, a t that is too small will make our search faster, but will also increase the possibility of false dismissals.

In most cases the task of learning *t* is greatly simplified by the fact that in our *annotated initial letter* database there are typically many images for each initial letter. This is because, apart from the fact that the same initial letter often appears multiple times in a single book, the wood block that impressed the initial letter could have been used for many decades in a given printing house. Figure 9 shows ten examples of an initial letter "L" pressed from the same wood block, from a single manuscript. As it happens, this 'L' appears 109 times in just this one text.



Figure 9: Ten examples of '∟' from the book "Les Oeuvres pharmaceutiques du Sr Jean de Renou, Conseiller & Medecin du Roy" published in 1626 [26]

Note that even in these images from a single book there is some amount of variability in (apparent) size, rotation, contrast, etc. We can thus use this data to learn the threshold. In essence, for each initial letter IL, we want to set a threshold t, such that most letters pressed from the same block are less than t from IL, and most other images encountered in historical texts are

greater than t. At first we imagined that this might require careful tuning to balance the false positive/false negative tradeoff. However, using the CK1 measure, these two groups are so well separated that we can use a simple method to assign t. We calculate the CK1 distances between all the annotated initials that are from the same wood block. Then, the mean value of these pairwise distances plus three standard deviations is chosen as the threshold distance for all members of that class. As discussed in Section 4.2.2, the blue/thick line in Figure 8 is the lower bound distances for the initial letter shown in Figure 8.c. This figure is augmented in Figure 10 with a horizontal red/dashed line, which is the threshold learned from the twenty-one examples of the same 'N' from the book *Comediae*.

We can use this example to show how four candidate windows (labeled a, b, c and d) will be processed by our search algorithm. We computed their lower bounds with the initial letter in Figure 8.c to see if they warrant further comparison with the more expensive CK1 measure. The leftmost window (a) in Figure 10 contains only about 12% of black pixels and its lower bound distance is 0.96, as shown on the curve. Since this is greater than the threshold, we do not further examine it. In contrast, Figure 10.b contains about 38% black pixels and its lower bound is 0.32, which is less than the threshold, so we invoke the CK1 measure to find the true distance (denoted by a green dot) to be 0.89. This means it was a *false* positive produced by the lower bound, but converted to a true negative by a refining pass with the CK1 distance. Figure 10.c contains 42% black pixels, so it also has its true CK1 measure calculated; the CK1 distance is just 0.41, so it is a *true* positive. This suggests that the letters shown in Figure 10.c and Figure 8.c are from the same wood block.



Figure 10: Four windows have their lower bounds to the image shown in Figure 8.c). Both (a) and (d) have lower bounds that exceed the threshold (horizontal red line) and are thus pruned, while (b) and (c) have small lower bound values and therefore the true distance (shown as dots) must be calculated. After the true CK1 distance was calculated, (b) was discarded while (c) was found to be a true positive

Finally, Figure 10.d contains 72% black pixels. Its lower bound is 0.98, much larger than the threshold, and thus it is also pruned without further consideration.

This method assumes that we have enough data to learn the threshold. Suppose, however, that this is not the case? For example, in the same text considered in Figure 9, we find that there is a single instance of the initial letter 'K', as shown in Figure 11.left.

We have two solutions to the scarce training data problem. The first is to simply take the thresholds learned for common letters in a given text (in this text, 'L', 'O', 'C', etc.) and use the mean of those values as the threshold for the rare initial letters from the same text (here, 'K', 'A', 'M', etc.).

Our second solution is inspired by [31], which also faced the problem of scarce training data in historical manuscripts. As shown in Figure 11.*right*, we can take singleton or rare initial letters and produce slightly distorted versions of them. We can then use this large synthetic dataset to learn the threshold.



Figure 11: *left*) The single example of an initial letter 'K' from the text considered in Figure 9. *right*) Six examples of artificially distorted versions of the letter

As we shall see in our experiments, the exact setting of the threshold is *not* a critical parameter, and thus we omit further details here and refer the reader to [35].

5. EXPERIMENTAL EVALUATION

We have designed all experiments to be completely reproducible. To this end, all datasets and code are permanently archived at [35]. In addition, this website contains many additional experiments that are omitted here for brevity.

In our experiments we wish to show that our ideas are accurate, robust to realistic conditions, and scalable to large datasets. Note that we are in a near unique position of not having to test robustness to parameter choices, since our method requires essentially no parameters to be set.

5.1 A Sanity Check for Robustness of CK1

The results discussed in Section 2 already hint at the effectiveness of the CK1 distance for the task at hand. In order to understand, and also to *demonstrate*, the robustness of our chosen distance measure to various problems often encountered in real manuscripts, we conducted extensive experiments where we synthetically introduced "flaws" in the images and examined the effect on the CK1 distance. In Figure 12.top we show the clustering of four pairs of initial letters pressed from the same wood block. There is no reason to expect much structure at the highest level of

the dendrogram, but gratifyingly, at the lowest level the branches are arranged in pairs.



Figure 12: *top*) A clustering of four pairs of the same initial letter. *bottom*) The clustering repeated after randomly introducing various "distortions"

According to our observations and a survey of the literature [11][12][14][22][25], the most commonly encountered difficulties in processing historical manuscripts are "occlusions", such as white holes in the text due to insect damage or black dots caused by ink or candle wax drips; misalignment due to rotation, from either at the time of scanning or in the original text; and size uncertainty due to the scanning process. We simulated all of these distortions and applied them to the initial letters seen in Figure 12.top. The representative clustering result shown in Figure 12.bottom suggests that our proposed measure achieves significant invariance to these difficulties.

5.2 A Sanity Check for the Lower Bound

We conducted an experiment to test the robustness of the lower bound algorithm shown in Table 3. If there are occasional violations of our approximate lower bound (i.e., false negatives) this may not affect the overall accuracy of our system. Consider that we may have twenty examples from a particular publisher in our reference library. Even if we incorrectly rejected one match due to a failure of the lower bound, we still have nineteen chances for a correct match and any of those nineteen would establish provenance. For example, if while searching for an initial letter 'A' we incorrectly rejected a match due to false rejection caused by an overly optimistic lower bound, we still have a chance for a true positive with 'B', 'C', etc. As it happens, this discussion is somewhat moot, since in over 100 million experiments we did not observe a single false positive.

Concretely, we learned the lower bound functions for the ten diverse initial letters shown in Figure 13. For each initial letter, we calculated both the lower bounds and the CK1 distances between each letter and ten million randomly chosen windows from historical manuscripts. Among these 100 million CK1 distance calculations, *not a single violation* of the lower bound was observed.



Figure 13: Ten initial letters used to test the accuracy of our approximate lower bound

5.3 Experiments on Historical Manuscripts

In this section we will illustrate how we use our lower bound approach to identify the provenance of historical manuscripts with significant speedup.

We learned the lower bound and threshold distances for every unique initial letter that exists in the book *Les Histoires universelles de Trogue Pompee, abbregees par Justin Historien*, published in 1559 [16]. The number of distinct initial letters in this book is twelve, but the number of different wood blocks used in this book was fifteen; e.g., the printer used two different wood blocks (with different backgrounds) for the initial letter 'A', etc. It was not uncommon for a printer to have multiple versions of the same letter because it allowed multiple pages to be printed in parallel and, in any case, it is logically possible that a single page could require two initial letters with the same character.

We use these fifteen initial letters to search two books, using the search algorithm introduced in Table 3. One is a 619-page book, *L'Architecture*, published in 1576; the other is a 452-page text, *Epistres des Princes*, which was published in 1572.

Recall that the algorithm will terminate if the existence of the same initial letter is detected; otherwise, it will continue to search over the entire book by using all available annotated initial letters. If none of the reference initial letters are discovered, the program will report this nonexistence after searching the entire book. For the book published in 1576, we started the search by using the most frequent initial letter observed in the earlier text, which was the letter 'A'. After scanning 47 pages, the program detects the first appearance of an initial letter 'A' on the page shown in Figure 14.right. The two 'A's are found to be impressed from the same wood block, which indicates that the two books are related. As the reader may have anticipated, the book L'Architecture is known to be related to our target text Les Histoires universelles de Trogue Pompee, abbregees par Justin Historien. Both were printed by a well-known 16th-century Parisian printer [30]. In this experiment 98.04% of the candidate windows were pruned by the lower bound, meaning that our search was about fifty times faster than that of the brute force search.

The pruning ratio, and hence the speedup, depend on the number of windows not pruned by the lower bound distance curve (shown in Figure 10). For this experiment the tested book is about architecture, so there are many dense architectural images and thus our obtained speedup is perhaps pessimistic.

To further test the algorithm, we again searched the book with the letter 'M', which is the only letter that appears in the reference text but not in the searched text. There are 88 initial letters in the text that *might* have been found as false positives, but were not. The algorithm searched the entire book and reported 'target letter not found'. For this experiment, 98.06% of the windows were pruned.



Figure 14: *left*) initial letters from the book published in 1559. *right*) the first appearance of the initial letter was detected on page 47 of the later book published in 1576

As a sanity check we conducted an experiment that had a much larger probability to produce false positives. We found a text that was similar in age, style, language and use of initial letters, but published by a different Parisian printer. The text is *Epistres des Princes*, published in 1572. After searching the whole book using all fifteen reference initial letters, we found that our algorithm did not report any false positives. This is in spite of the fact that, as shown in Figure 15, there are many possibilities for false positives to occur.



Figure 15: top) Sample letters from our reference set. Our algorithm correctly classifies the somewhat similar letters from different printers (bottom) as true negatives

5.4 Robustness to the Threshold Setting

We noted earlier that one of the strongest points of our algorithm is that it has no parameters to set. However, there is one *choice* we made: to set the threshold to be the *mean plus three standard deviations* of the interclass distance. Suppose we had made a different choice? We tested to see what effect this would have by exactly repeating the experiment in the previous section but with the threshold instead set to the mean plus *two* standard deviations and the mean plus *four* standard deviations of the interclass distance. In the former case the algorithm's slightly more aggressive pruning resulted in a speedup of 1.2%, but critically, the output of the algorithm was identical. In the latter the slightly less aggressive pruning resulted in the search taking 2.3% longer, and (as logically must be the case), the results were identical. These results, and similar experiments archived at [35], strongly suggest that the threshold setting is not a critical parameter.

5.5 A Test for Robustness to Page Condition

To test the robustness of our algorithm to both the condition of the original manuscript and to various choices made by the digital archivists (resolution, image format, camera settings etc.) we conducted the following experiment.

We took the page shown in Figure 14.*right* and printed it using a standard off-the-shelf HP LaserJet 4300 at 600 dpi. We then randomly scribbled on the printout with a red pen, ensuring the scribble passed through the initial letter at least ten times. Finally, we crumpled the page into a tight ball. We recovered the page by opening the crumpled ball of paper and scanning it with a Canon LIDE70 scanner to scan at 300dpi; the result is in Figure 16.*right*.





If we simply replace the original page of the text with this highly corrupted version, it makes no perceptible difference to the search process. We still find the matching initial letter in the same amount of time.

Since the corruptions we added to this page dwarf the problems we have encountered with real historical manuscripts [13], this experiment bodes well for the robustness of our approach.

5.6 Large Scale Experiments

To further test the algorithm, we conducted an experiment by using twenty books from the 15th and 16th centuries [35]. We learned the lower bound and threshold distances for every unique initial letter that exists in the book *Bellum Christianorum principium*, *praecipue Gallorum*, *contra Saracenos*, published in 1533. The number of distinct initial letters in this book is sixteen, but the number of different wood blocks used

in this book was twenty-four. We used these learned initial letters to test another nineteen books. We found that there are two books that share the same initial letters with the book published in 1533. These two books were published in 1538 and 1557, respectively. After checking the provenance of the true positives, we found that these two books and the book published in 1533 were printed by the same printer, Heinrich Petri.

There are a total of 6,956 pages in these twenty books. By using the lower bound algorithm, the pruning ratio is 99.38%, meaning we are about 160 times faster than a brute force search. These experiments did not report any false positives.

6. RUNNING TIME

The speedup produced by our algorithm is impressive, but is it enough to allow real-time processing? For the texts we are interested in, the careful handing required for scanning requires at least an hour per book [14]. Thus, we are about a factor of ten away from real-time processing for realistic collections of reference initial letters. We could gain this factor of ten with more/better hardware. However, below we show that we could also mitigate this gap with a simple down-sampling idea.

We repeated the classification experiment in Section 3.1 for various levels of down-sampling, recording both the speedup and error rates. As shown in Figure 17, using a 50% sample size, the error rate is only 4.33%. However, the running time is sixteen times faster. This is because the speedup comes from two factors. First, the running time for calculating CK1 distances is four times faster if we down-sample the images by half [7]. Moreover, in the experiment shown in Section 5.3 and Section 5.6, the number of windows that need to calculate the CK1 distance decreases by one-fourth. Combining these two factors, a dramatic speedup can be achieved by sacrificing a small amount of accuracy. Recall that *classification* is actually a harder problem than our recognition problem. Thus, we expect (and have confirmed in [35]) that we can use this simple down-sampling trick to gain a ten to twenty-fold increase with a near-zero chance of a false negative.



Figure 17: Running time VS classification error rate. The bold/red line is the running time for downsampling the image size from 100% to 30%. The thin/blue line is the classification error rate

7. DISCUSSION

We did not directly compare to any other technique in the experimental section; here we explain this omission. Recall that in Section 3.1 we did compare *classification* accuracy with a benchmark dataset that other researchers had created. As we achieved zero error (without tuning any parameters) and the two most obvious rivals achieved significant errors (RLE 39.42% [9], SIFT 10.21% [19]), we felt that further comparisons to these techniques are pointless.

There are a handful of other image matching techniques optimized for initial letters that we do not compare to here. For example, [15] proposes a method that works by segmenting the initial letters, using a Zipf Law distribution to label the segmented regions, measuring four features of these regions, constructing a graph of these regions and finally using (an approximation of) the graph edit distance to measure the similarity between two images in their graph representation. We do not compare to this work because there are more than eight parameters that must be set, and there is little guidance on setting them. Moreover, as the mean number of nodes *n* for an initial letter is reported at 108, and their graph edit distance approximation method uses the O (n^3) Hungarian method as a subroutine, this method will be conservatively tens of thousands of times slower than our proposed method.

There is significant work on texture analysis for historical manuscripts; see [14][22] and the references therein. However, texture is typically only used for layout analysis and segmentation, not for classification. Much of this work suffers from the difficulty of parameter setting; for example, [5] uses Gabor filters for texture analysis and the user must decide the best values for scales, orientations, and filter mask size parameters in addition to several other parameters. It is not clear how well these parameters will generalize from book to book or even from page to page within a single manuscript. Recently, some researchers have begun to apply SIFT to problems in historical manuscripts, but again only to the problems of layout analysis and segmentation [11]. It is not clear that these results would generalize to our task at hand, and our results in Section 3.1 suggest that SIFT may have difficulty with some of the very subtle distinctions that must be made.

8. CONCLUSION AND FUTURE WORK

We have defined a new problem: determining the provenance of historical manuscripts by searching for occurrences of initial letters from a reference library of annotated letters of known provenance. We have shown a technique based on learned approximate lower bounds that is robust, fast and accurate, and has the important advantage of having essentially no parameters to tune.

While our algorithm is fast, there are still significant avenues for further speedup. Currently, each initial letter is searched independently; however, for similar problems in text, time series [32], XML, etc., researchers have shown that it is possible to group together similar elements (for example, grouping 'O' and 'Q', then conducting a single search for the group representative). This idea may be tenable with some modifications for our (nonmetric) CK1 measure.

We also plan to explore other possible uses of empirically learned approximate lower bounds.

Finally, we have made *all* code and datasets publicly available [35] in order to encourage replication and extension of our results, and possible adoption of our ideas for other historical manuscript data mining tasks.

9. ACKNOWLEDGMENTS

We thank all the digital archivists who produced the vast amounts of data that made this work possible, and Dr. Ioanna Kakoulli of UCLA for inspiring this effort and pointing to relevant literature. This work was funded by NSF awards 0803410 and 0808770.

10. REFERENCES

- K. Alderman, *Thieves Take a Page Out of Rare Books* and *Manuscripts*, ART & CULTURAL HERITAGE L. NEWSL. Vol I, Issue V, Spring 2009.
- [2] S. Atran, J. Henrich, *The Evolution of Religion: How Cognitive by-products, Adaptive Learning Heuristics, Ritual Displays, and Group Competition Generate Deep Commitments to Prosocial Religions.* Biological Theory: Integrating Development, Evolution, and Cognition, 5, pp.18-30, 2010.
- [3] E. Bronner, Stolen Manuscripts Plague Israeli Archives. New York Times. August 20th, 2008.
- [4] E. Baudrier, S. Busson, S. Corsini, M. Delalandre, J. Landre, F. Morain-Nicolier, *Retrieval of the Ornaments from the Hand-Press Period: An Overview*, 10th ICDAR 2009.
- [5] P. Basa, P. S. Sabari, R. Nishikanta, A.G Ramakrishnan, *Gabor Filters for Document Analysis in Indian Bilingual Documents*, International Conference on Intelligent Sensing and Information Processing, pp.123-126, 2004.
- [6] Consortium of European Research Libraries www.cerl.org/web/ 2011.
- [7] B. Campana, E. Keogh, *A Compression Based Distance Measure for Texture*, SDM, 2010.
- [8] S. Calvani, Frequency and Figures Of Organised Crime In Art And Antiquities, ISPAC Conference, 2008.
- [9] M. Delalandre, J. M. Ogier, and J. Llados, A Fast CBIR System of Old Ornamental Letter, Workshop on Graphics Recognition, LNCS, pp. 135–144, 2008.
- [10] INTERPOL, Stolen Works of Art. (Accessed 7th July 2011). www.interpol.int/Public/WorkOfArt/woafaq.asp
- [11] A. Garz, M. Diem, R. Sablatnig, *Local Descriptors for Document Layout Analysis*. In Proc' of Addison-Wesley series in statistics., pp. 29-38, 2010.
- [12] A. Garz, M. Diem, R. Sablatnig, Layout Analysis of Ancient Manuscripts Using Local Features. In Eikonopoiia. Digital Imaging of Ancient Textual Heritage, 2011.
- [13] Ancient Greek Manuscripts Hit the Internet, www.foxnews.com/scitech/2010/09/27/british-libraryposts-greek-manuscripts-web/

- [14] N. Journet, V. Eglin, J.Y Ramel, R. Mullot, *Dedicated Texture Based Tools For Characterisation Of Old Books*. In Proceedings of the 2nd DIAL, April, 2006.
- [15] S. Jouili, M. Coustaty, S. Tabbone, J. M. Ogier, NAVIDOMASS: Structural-Based Approaches Towards Handling Historical Documents. ICPR, pp. 946-959, 2010.
- [16] T. P. Justin. Histoire universelle de Trogues Pompée, réduite en abrégé par Justin. 1559.
- [17] E. Keogh, S. Lonardi, C. A. Ratanamahatana, L. Wei, S. Lee, J. Handley, *Compression-Based Data Mining of Sequential Data*, DMKD. 14(1), pp. 99-129, 2007.
- [18] E. Keogh: Exact Indexing of Dynamic Time Warping. VLDB, pp.406-417, 2002.
- [19] D. G. Lowe. Distinctive Image Features from Scale-Invariant Key Point, International Journal of Computer Vision, vol. 60, pp. 91-110, 2004.
- [20] M. Li, X. Chen, X. Li, B. Ma, Paul M. B. Vitányi: *The Similarity Metric*. IEEE Transactions on Information Theory (TIT) 50 (12): 3250-3264 2004.
- [21] D. Maltoni, D. Maio, A. K. Jain, and S. Prabhakar, Handbook of Fingerprint Recognition, Springer 2003.
- [22] J. M. Ogier, K. Tombre, Document Image Analysis Techniques for Cultural Heritage Documents, Proceedings of 1st EVA Conference, pp 107–114, 2006.
- [23] Ornaments typographical, www.ornements-typomouriau.be/
- [24] S. Pigeon, S. Coulombe: Very Low Cost Algorithms for Predicting the File Size of JPEG Images. DCC, pp.538, 2008.
- [25] J. Y. Ramel, S. Leriche, M. L. Demonet, S. Busson, User-Driven Page Layout Analysis of Historical Printed Books, IJDAR, pp. 243–261, 2007.
- [26] J. Renou, Les Oeuvres Pharmaceutiques du Sr Jean de Renou, Conseiller & Medecin du Roy. 1626.
- [27] Y. Rubner, C. Tomasi, L. Guibas, A Metric for Distributions with Applications To Image Databases. In Proceedings of the IEEE ICCV pp. 59–66, 1998.
- [28] Q. Tang, P. Nasiopoulos, Efficient Motion Re-Estimation with Rate-Distortion Optimization for MPEG-2 to H.264/AVC Transcoding. IEEE Trans. Circuits Syst. Video Techn. 20. pp. 262-74, 2010.
- [29] A. Vedaldi (2011). www.vlfeat.org/~vedaldi/index.html
- [30] Virtual Library Humanist Program *www.bvh.univ-tours.fr/index.htm.* 2011.
- [31] X. Wang, L. Ye, E. J. Keogh, C. R. Shelton, Annotating Historical Archives of Images, JCDL, pp. 341-350, 2008.
- [32] L. Wei, E. Keogh, H. Van Herle, A. Mafra-Neto: Atomic Wedgie: Efficient Query Filtering for Streaming Times Series. ICDM, 2005.
- [33] Victoria and Albert Museum: Woodcut Printing (video) www.youtube.com/watch?v=mgCYovlFRNY
- [34] Q. Zhu, E. Keogh, Mother Fugger: Mining Historical Manuscripts with Local Color Patches. ICDM, 2010.
- [35] B. Hu, supporting URL for this paper, www.cs.ucr.edu/~bhu002/IL/IL.html 2011.